



# **Advanced Databases and Data Mining (COMP3420)**

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# **Textbook: Data Mining: Concepts and Techniques — Introduction**

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**Ack:** most lecture slides are adopted from the authors' slides

# Introduction

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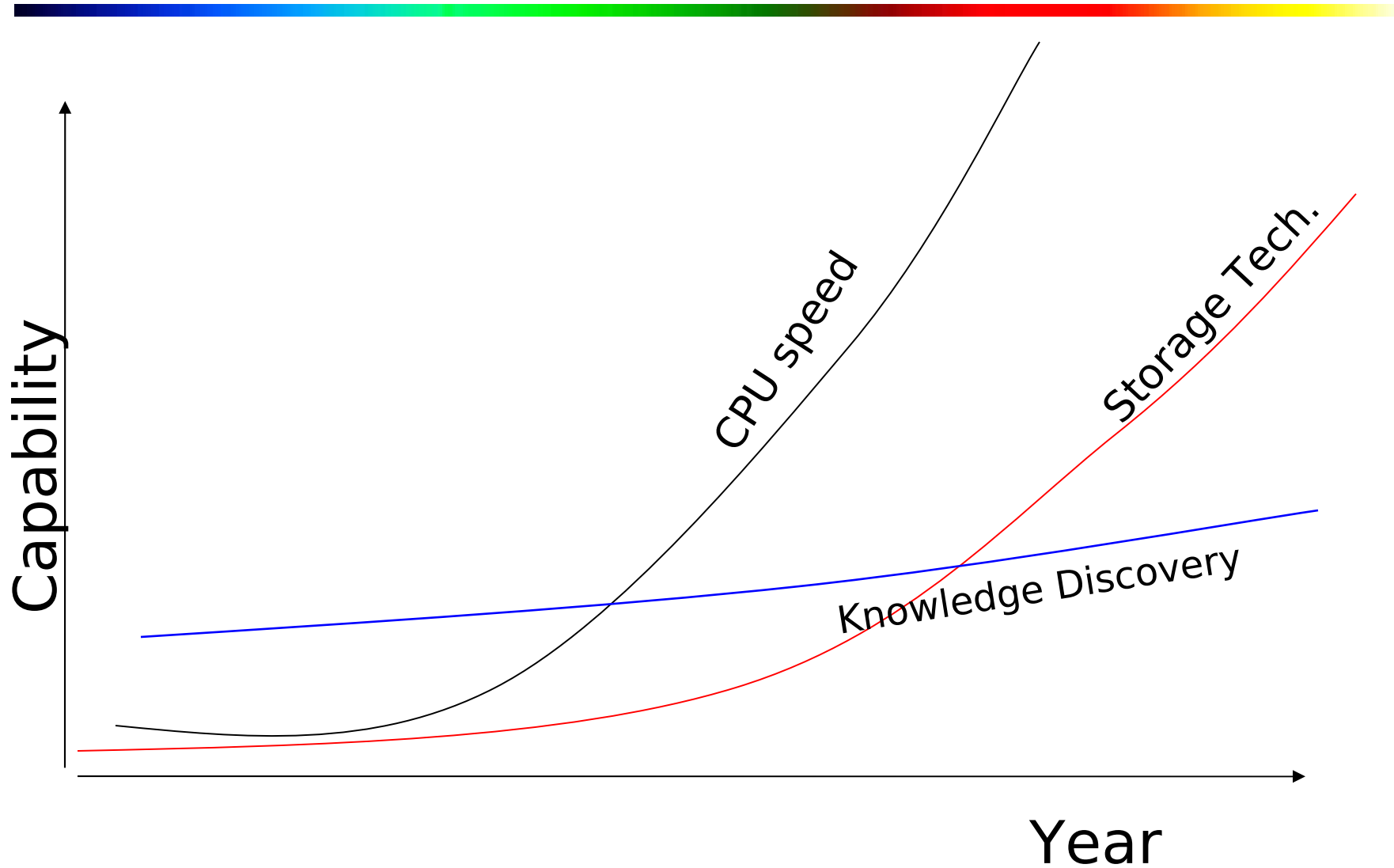
- Data Mining Overview (DM)
- Data Warehouse Overview (DW)
- The Relationship Between DW and DM

# Data Mining Overview

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- Motivation: Why data mining?
- What is data mining?
- Data Mining: On what kind of data?
- Data mining functionality
- Classification of data mining systems
- Major issues in data mining

# Computer Hardware VS Information Processing



# Evolution of Database Technology

- 1960s:
  - Data collection, database creation, IMS and network DBMS
- 1970s:
  - Relational data model, SQL, relational DBMS implementation
- 1980s (\*\*):
  - RDBMS, advanced data models (extended-relational, OO, deductive, etc.)
  - Application-oriented DBMS (spatial, scientific, engineering, etc.)
- 1990s:
  - Data mining, data warehousing, multimedia databases, and Web databases
- 2000s
  - Stream data management and mining
  - Data mining and its applications
  - Web technology (XML, data integration) and global information systems

# Why Data Mining?



- The Explosive Growth of Data: from terabytes to petabytes
  - Data collection and data availability
    - Automated data collection tools, database systems, Web, computerized society
  - Major sources of abundant data
    - Business: Web, e-commerce, transactions, stocks, ...
    - Science: Remote sensing, bioinformatics, scientific simulation, ...
    - Society and everyone: news, digital cameras, YouTube
- We are drowning in data, but starving for knowledge!
- “Necessity is the mother of invention”—Data mining—  
Automated analysis of massive data sets

# Why Data Mining?—Potential Applications

- Data analysis and decision making support
  - Market analysis and management
    - Target marketing, customer relationship management, market basket analysis, cross selling, etc
  - Risk analysis and management
    - Forecasting, customer retention, improved underwriting, quality control, competitive analysis
  - Fraud detection and detection of unusual patterns (outliers)
  - Text mining (news group, email, documents) and Web mining
  - Stream data mining
  - Bioinformatics and bio-data analysis

# Market Analysis and Management

- Where does the data come from?—Credit card transactions, loyalty cards, discount coupons, customer complaint calls, plus (public) lifestyle studies
- Target marketing
  - Find clusters of “model” customers who share the same characteristics: interest, income level, spending habits, etc.
  - Determine customer purchasing patterns over time
- Cross-market analysis—Find associations/co-relations between product sales, & predict based on such association
- Customer profiling—What types of customers buy what products (clustering or classification)
- Customer requirement analysis
  - Identify the best products for different groups of customers
  - Predict what factors will attract new customers
- Provision of summary information
  - Multidimensional summary reports
  - Statistical summary information (data central tendency and variation)

# Corporate Analysis & Risk Management

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- Finance planning and asset evaluation
  - cash flow analysis and prediction
  - contingent claim analysis to evaluate assets
  - cross-sectional and time series analysis (financial-ratio, trend analysis, etc.)
- Resource planning
  - summarize and compare the resources and spending
- Competition
  - monitor competitors and market directions
  - group customers into classes and a class-based pricing procedure
  - set pricing strategy in a highly competitive market

# Fraud Detection & Mining Unusual Patterns

- Approaches: Clustering & model construction for **frauds, outlier** analysis
- Applications: Health care, retail, credit card service, telecomm.
  - Auto insurance: ring of collisions
  - Money laundering: suspicious monetary transactions
  - Medical insurance
    - Professional patients, ring of doctors, and ring of references
    - Unnecessary or correlated screening tests
  - Telecommunications: phone-call fraud
    - Phone call model: destination of the call, duration, time of day or week.
  - Retail industry
    - Analysts estimate that 38% of retail shrink is due to dishonest employees
  - Anti-terrorism

# What Is Data Mining?

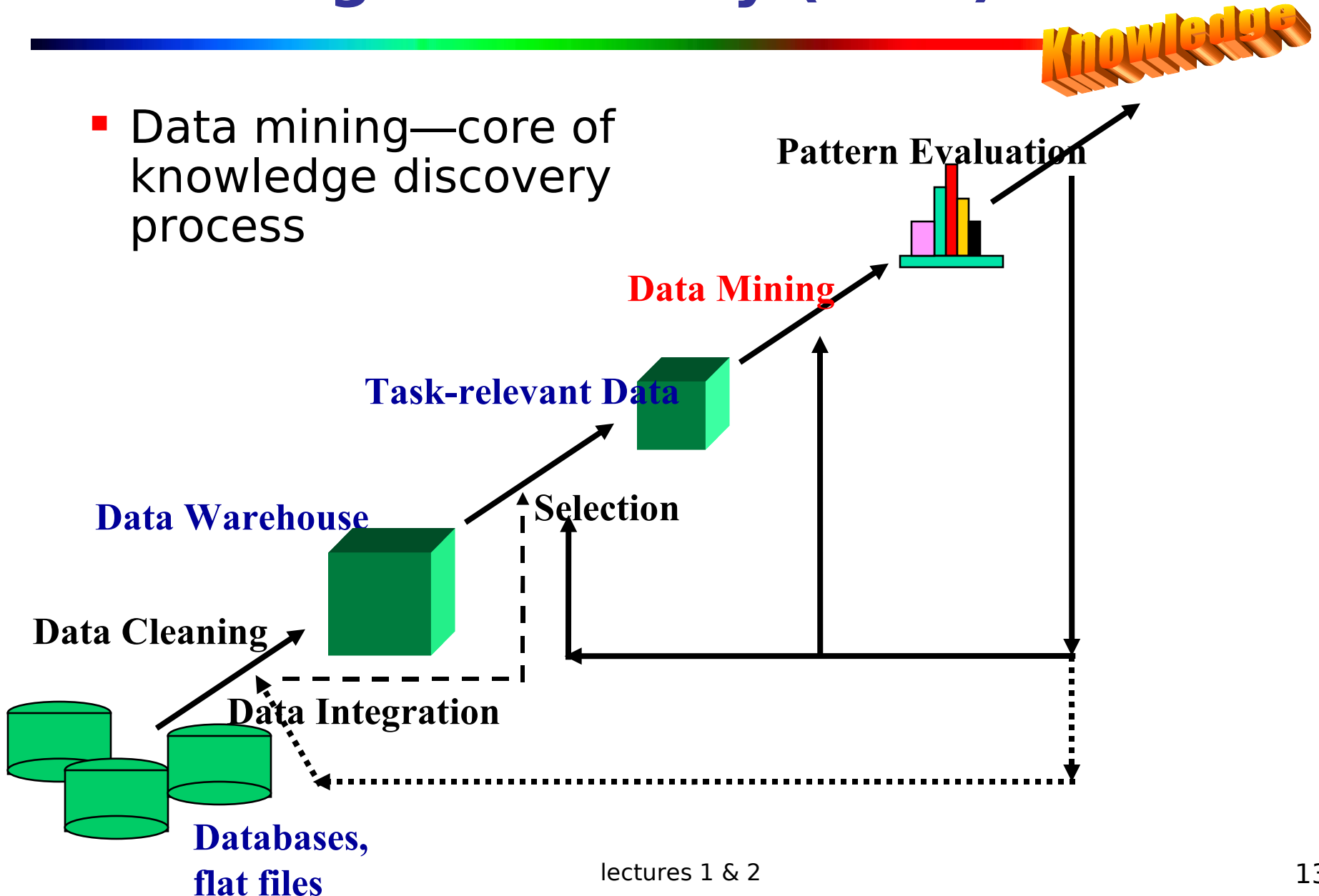


- Data mining (knowledge discovery from data)
  - Extraction of interesting (non-trivial, implicit, previously unknown and potentially useful) patterns or knowledge from huge amount of data
- Alternative names
  - Knowledge discovery (mining) in databases (KDD), knowledge extraction, data/pattern analysis, information harvesting, business intelligence, etc.
- *Watch out: Is everything “data mining”?*
  - *Simple search and query processing*
  - *(Deductive) expert systems*

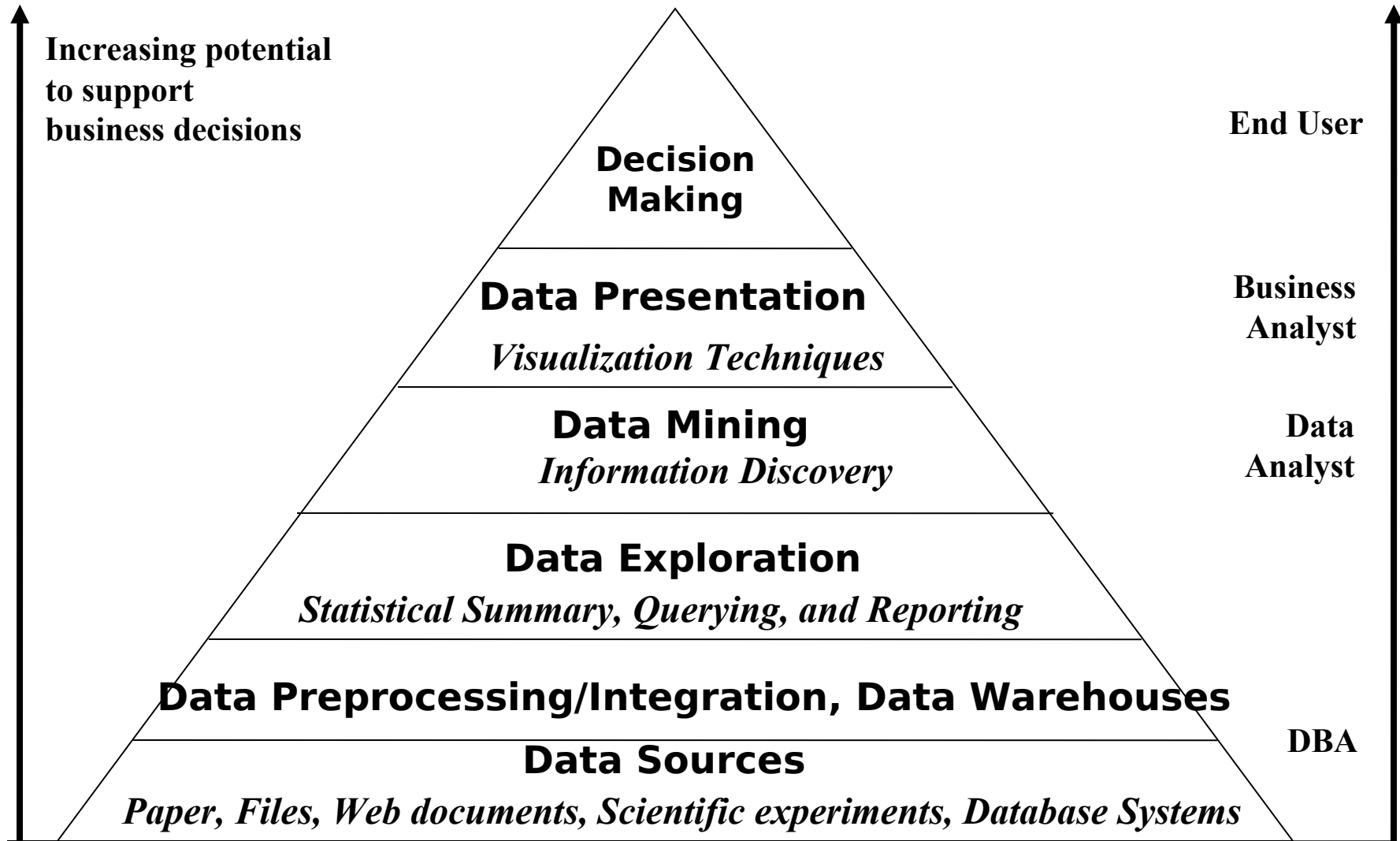


# Knowledge Discovery (KDD) Process

- Data mining—core of knowledge discovery process

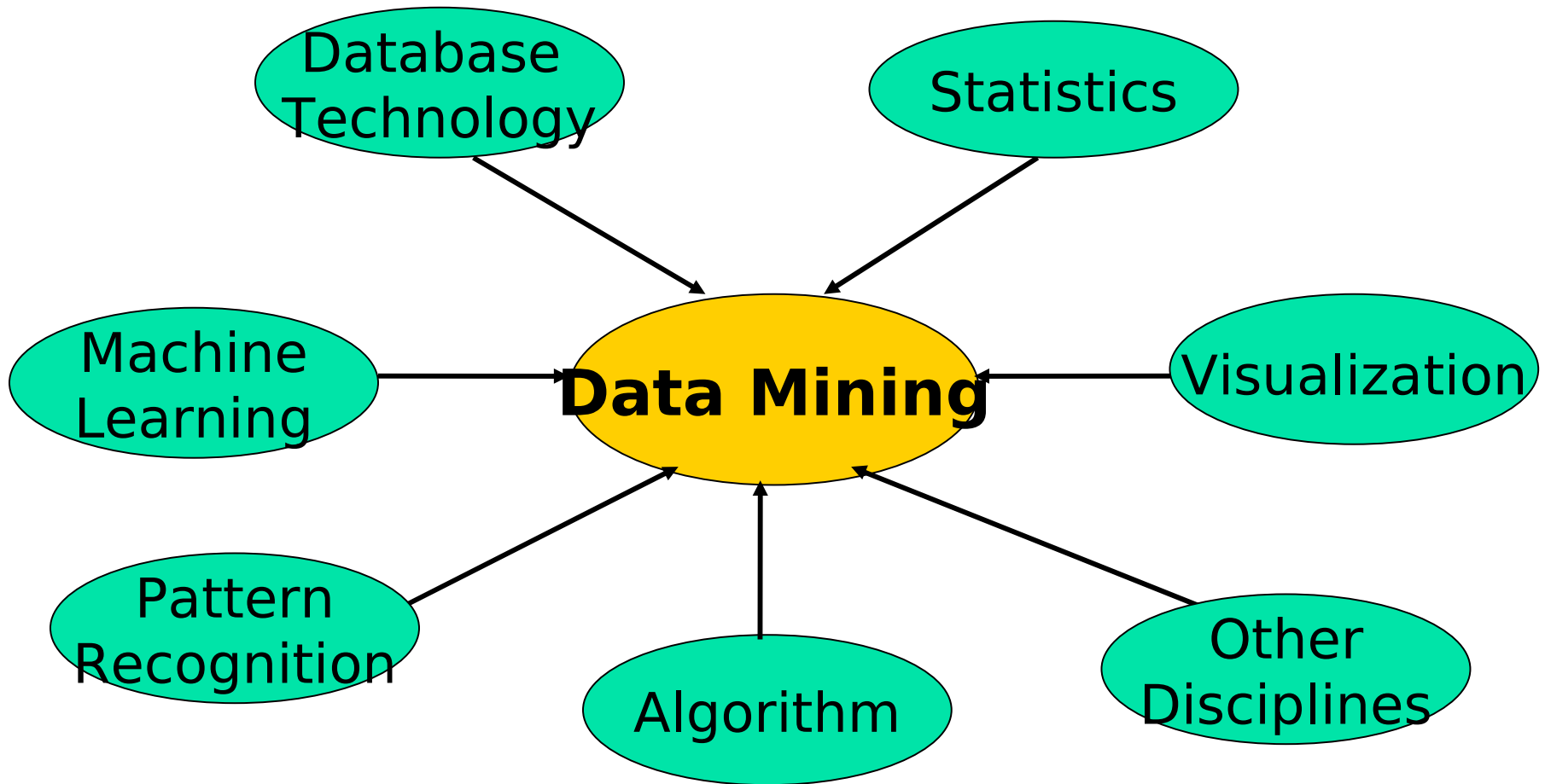


# Data Mining and Business Intelligence



# Data Mining: Confluence of Multiple Disciplines

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# Why Not Traditional Data Analysis?

- **Tremendous amount of data**
  - Algorithms must be highly **scalable** to handle such as terabytes of data
- **High-dimensionality of data**
  - Micro-array may have tens of thousands of dimensions
- **High complexity of data**
  - Data streams and sensor data
  - Time-series data, temporal data, sequence data
  - Structure data, graphs, social networks and multi-linked data
  - Heterogeneous databases and legacy databases
  - Spatial, spatiotemporal, multimedia, text and Web data
  - Software programs, scientific simulations

# Multi-Dimensional View of Data Mining

- **Data to be mined**
  - Relational, data warehouse, transactional, stream, object-oriented/relational, active, spatial, time-series, text, multimedia, heterogeneous, legacy, WWW
- **Knowledge to be mined**
  - Characterization, discrimination, association, classification, clustering, trend/deviation, outlier analysis, etc.
  - Multiple/integrated functions and mining at multiple levels
- **Techniques utilized**
  - Database-oriented, data warehouse (OLAP), machine learning, statistics, visualization, etc.
- **Applications adapted**
  - Retail, telecommunication, banking, fraud analysis, bio-data mining, stock market analysis, text mining, Web mining, etc.

# Data Mining: On What Kinds of Data?

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- Database-oriented data sets and applications
  - Relational database, data warehouse, transactional database
- Advanced data sets and advanced applications
  - Data streams and sensing data
  - Time-series data, temporal data, sequence data (incl. bio-sequences)
  - Structure data, graphs, social networks and multi-linked data
  - Object-relational databases
  - Heterogeneous databases and legacy databases
  - Spatial data and spatiotemporal data
  - Multimedia database
  - Text databases
  - The World-Wide Web

# Data Mining: Classification Schemes

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- General functionality
  - **Descriptive data mining** (describe individual classes and concepts in **summaried, concise and yet precise** terms. e.g. BigSpender)
  - **Predictive data mining** (Classification is the process of finding a **model** that describes and distinguishes data classes or concepts for the purpose of being able to use the model to predict the class of objects whose class label is unknown, e.g. good, mild, and no response )

# Data Mining: Classification Schemes (cont)

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- Different views lead to different classifications
  - **Data** view: Kinds of data to be mined
  - **Knowledge** view: Kinds of knowledge to be discovered
  - **Method** view: Kinds of techniques utilized
  - **Application** view: Kinds of applications adapted

# Data Mining Functionalities

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- **Multidimensional concept description: Characterization and discrimination**
  - Generalize, summarize, and contrast data characteristics, e.g., dry vs. wet regions
- **Frequent patterns, association, correlation vs. causality**
  - Diaper → Beer [0.5%, 75%] (Correlation or causality?)
- **Classification and prediction**
  - Construct models (functions) that describe and distinguish classes or concepts for future prediction
    - E.g., classify countries based on (climate), or classify cars based on (gas mileage)
  - Predict some unknown or missing numerical values

# Data Mining Functionalities (cont)

- Cluster analysis
  - Class label is unknown: Group data to form new classes, e.g., cluster houses to find distribution patterns
  - Maximizing intra-class similarity & minimizing interclass similarity
- Outlier analysis
  - Outlier: Data object that does not comply with the general behaviour of the data
  - Noise or exception? Useful in fraud detection, rare events analysis
- Trend and evolution analysis
  - Trend and deviation: e.g., regression analysis
  - Sequential pattern mining: digital camera → large SD card
  - Periodicity analysis
  - Similarity-based analysis
- Other pattern-directed or statistical analyses

# Major Issues in Data Mining

## ■ Mining methodology

- Mining different kinds of knowledge from diverse data types, e.g., bio, stream, Web
- Performance: efficiency, effectiveness, and scalability
- Pattern evaluation: the interestingness problem
- Incorporation of background knowledge
- Handling noise and incomplete data
- Parallel, distributed and incremental mining methods
- Integration of the discovered knowledge with existing one: knowledge fusion

## ■ User interaction

- Data mining query languages and ad-hoc mining
- Expression and visualization of data mining results
- Interactive mining of knowledge at multiple levels of abstraction

## ■ Applications and social impacts

- Domain-specific data mining & invisible data mining
- Protection of data security, integrity, and privacy

# Summary

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- Data mining: Discovering interesting patterns from large amounts of data. A natural evolution of database technology, in great demand, with wide applications
- A KDD process includes data cleaning, data integration, data selection, transformation, data mining, pattern evaluation, and knowledge presentation
- Mining can be performed in a variety of information repositories
- Data mining functionalities: characterization, discrimination, association, classification, clustering, outlier and trend analysis, etc.
- Major issues in data mining

# An Overview of Data Warehousing and OLAP Technology

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- What is a data warehouse?
- A multi-dimensional data model
- Data warehouse architecture
- Data warehouse implementation

# What is Data Warehouse?

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- Defined in many different ways, but not rigorously.
  - A decision support **database** that is maintained **separately** from the organization's operational database
  - Support **information processing** by providing a solid platform of *consolidated, historical data for analysis.*
- “A data warehouse is a subject-oriented, integrated, time-variant, and nonvolatile collection of data in support of management's decision-making process.”—**W. H. Inmon**
- Data warehousing:
  - The process of constructing and using data warehouses

# Data Warehouse—Subject-Oriented

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- Organized around major subjects, such as **customer, product, sales**
- Focusing on the modelling and analysis of data for decision makers, **not on daily operations or transaction processing**
- Provide **a simple and concise** view around particular subject issues by **excluding data that are not useful in the decision support process**

# Data Warehouse—Integrated

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- Constructed by integrating multiple, heterogeneous data sources
  - relational databases, flat files, on-line transaction records
- Data cleaning and data integration techniques are applied.
  - Ensure consistency in naming conventions, encoding structures, attribute measures, etc. among different data sources
    - E.g., Hotel price: currency, tax, breakfast covered, etc.
  - When data is moved to the warehouse,

# Data Warehouse—Time Variant

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- **The time horizon for the data warehouse is significantly longer than that of operational systems**
  - Data warehouse data: provide information from a historical perspective (e.g., past 5-10 years)
  - Operational database: current value data
- **Every key structure in the data warehouse**
  - Contains an element of time explicitly or implicitly, while the key of operational data may or may not contain “time element”

# Data Warehouse—Nonvolatile

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- A **physically separate store** of data transformed from the operational environment
- Operational **update of data does not occur** in the data warehouse environment
  - Does not require transaction processing, recovery, and concurrency control mechanisms
  - Requires only two operations in data accessing:
    - *initial loading of data* and *access of data*

# Data Warehouse vs. Heterogeneous DBMS

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- Traditional heterogeneous DB integration: A **query driven** approach
  - Build **wrappers/mediators** on top of heterogeneous databases
  - When a query is posed to a client site, a meta-dictionary is used to translate the query into queries appropriate for individual heterogeneous sites involved, and the results are integrated into a global answer set
  - Complex information filtering, compete for resources
- **Data warehouse: update-driven**, high performance
  - Information from heterogeneous sources is integrated in advance and stored in warehouses for direct query and analysis

# Data Warehouse vs. Operational DBMS

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- OLTP (on-line transaction processing)
  - Major task of traditional relational DBMS
  - Day-to-day operations: purchasing, inventory, banking, manufacturing, payroll, registration, accounting, etc.
- OLAP (on-line analytical processing)
  - Major task of data warehouse system
  - Data analysis and decision making
- Distinct features (OLTP vs. OLAP):
  - User and system orientation: customer vs. market
  - Data contents: current, detailed vs. historical, consolidated
  - Database design: ER + application vs. star + subject
  - View: current, local vs. evolutionary, integrated
  - Access patterns: update vs. read-only but complex queries

# OLTP vs. OLAP

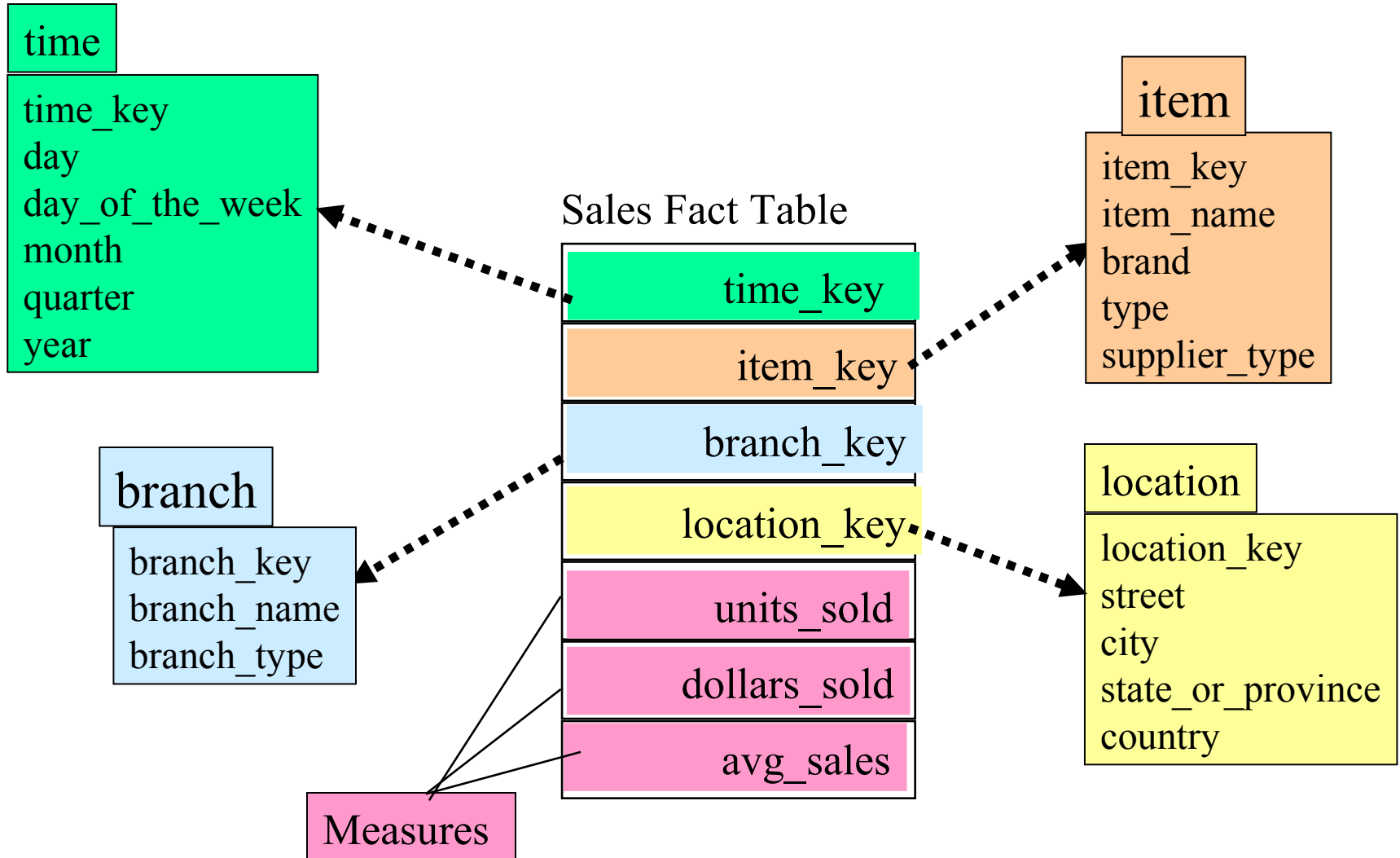
	<b>OLTP</b>	<b>OLAP</b>
<b>users</b>	clerk, IT professional	knowledge worker
<b>function</b>	day to day operations	decision support
<b>DB design</b>	application-oriented	subject-oriented
<b>data</b>	current, up-to-date detailed, flat relational isolated	historical, summarized, multidimensional integrated, consolidated
<b>usage</b>	repetitive	ad-hoc
<b>access</b>	read/write index/hash on prim. key	lots of scans
<b>unit of work</b>	short, simple transaction	complex query
<b># records accessed</b>	tens	millions
<b>#users</b>	thousands	hundreds
<b>DB size</b>	100MB-GB	100GB-TB
<b>metric</b>	transaction throughput	query throughput, response

# Conceptual Modeling of Data Warehouses

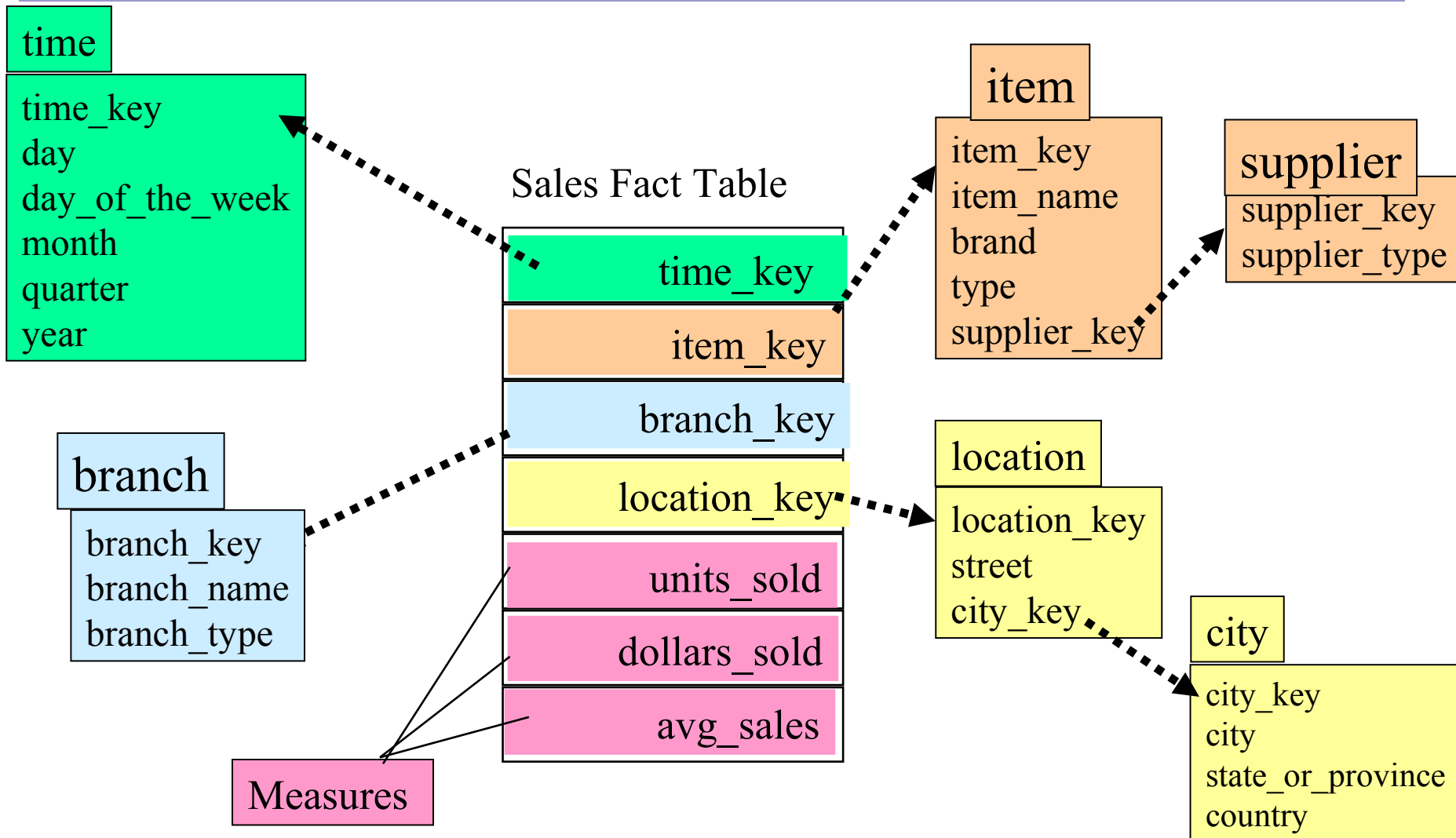
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- Modeling data warehouses: **dimensions** ( non-numeric attributes) & **measures** (numerical attributes)
  - Star schema: A fact table in the middle connected to a set of dimension tables
  - Snowflake schema: A refinement of star schema where some dimensional hierarchy is normalized into a set of smaller dimension tables, forming a shape similar to snowflake

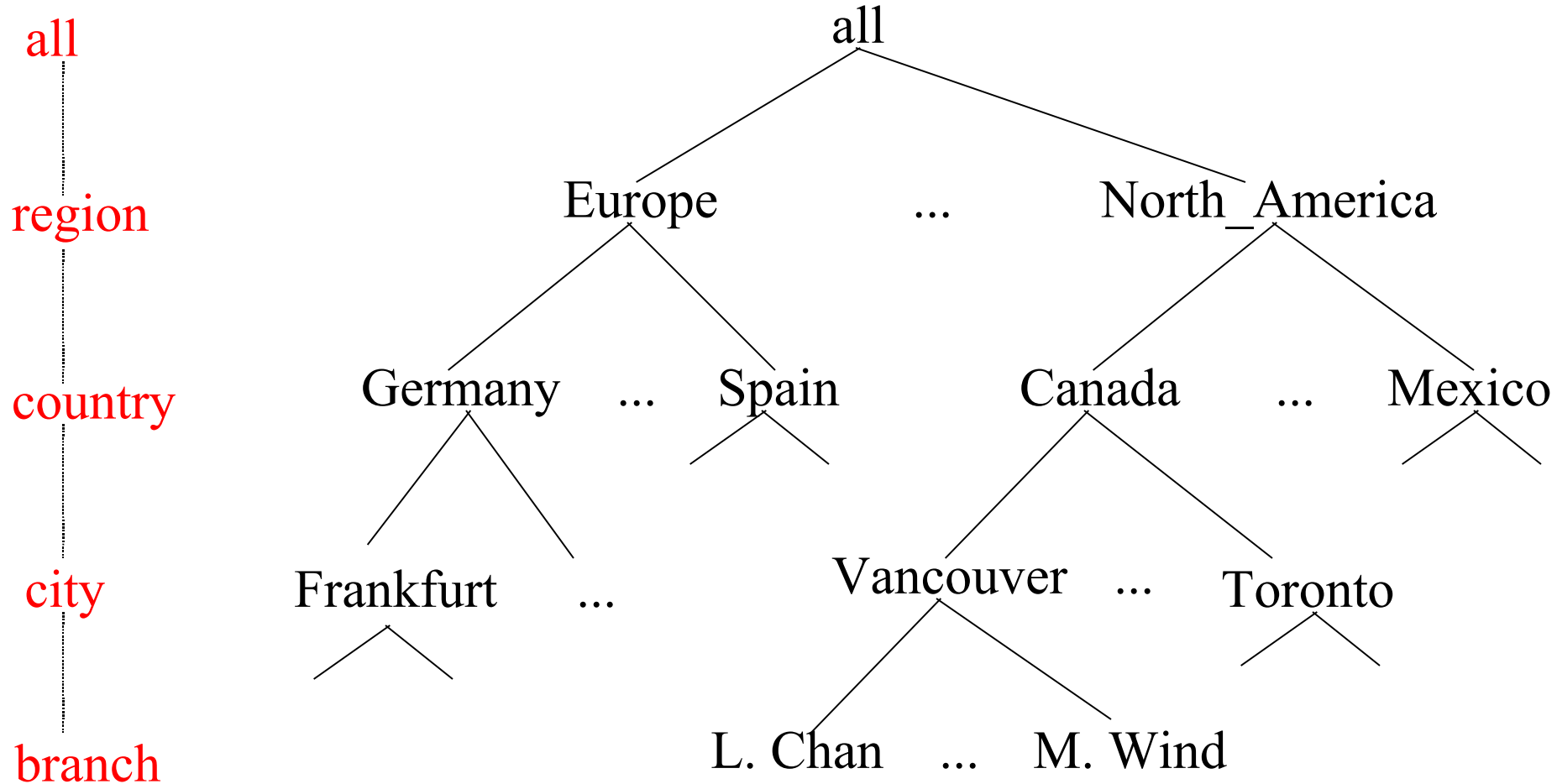
# Example of Star Schema



# Example of Snowflake Schema

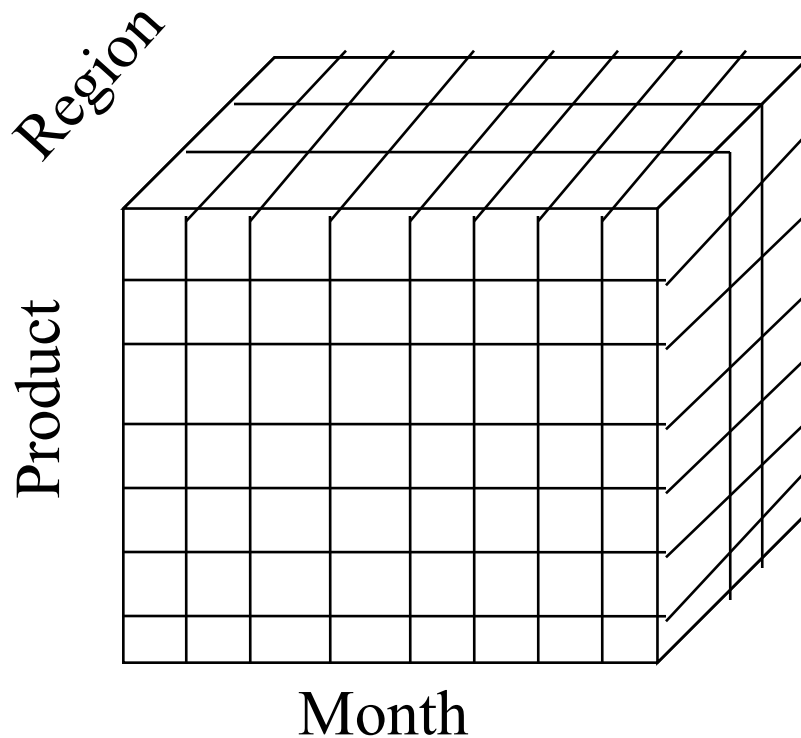


# A Concept Hierarchy: Dimension (location)

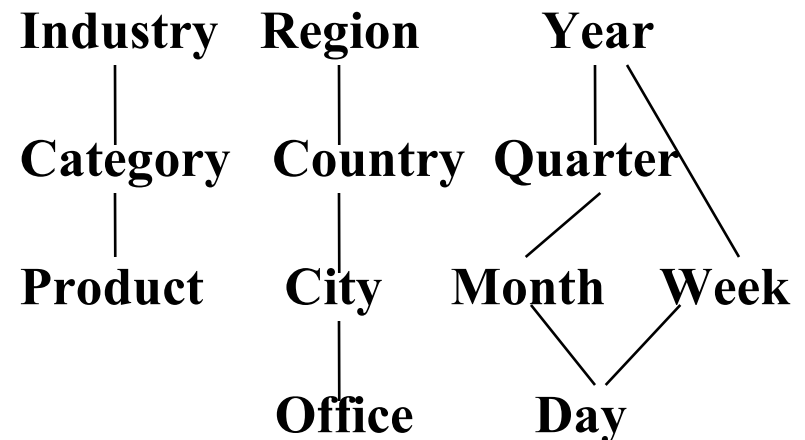


# Multidimensional Data

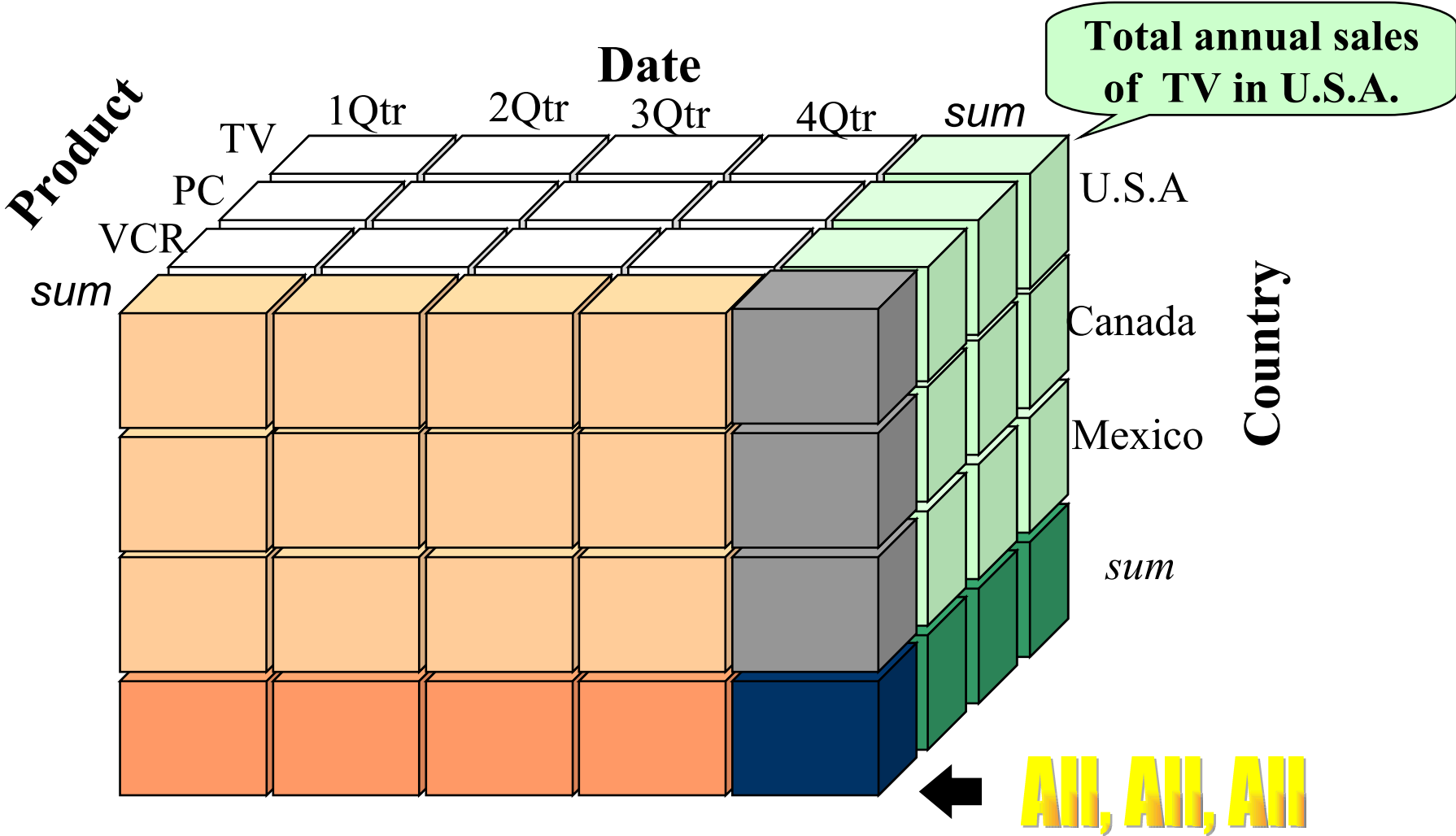
- Sales volume as a function of product, month, and region



**Dimensions: Product, Location, Time**  
**Hierarchical summarization paths**



# A Sample Data Cube



# Typical OLAP Operations

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- **Roll up (drill-up):** summarize data
  - by climbing up hierarchy or by dimension reduction
- **Drill down (roll down):** reverse of roll-up
  - from higher level summary to lower level summary or detailed data, or introducing new dimensions
- **Slice and dice:** project and select
- **Pivot (rotate):**
  - reorient the cube, visualization, 3D to series of 2D planes

# Typical OLAP Operations

## (CONT)

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- Other operations
  - **drill across:** involving (across) more than one fact table
  - **drill through:** through the bottom level of the cube to its back-end relational tables (using SQL)

# Design of Data Warehouse: A Business Analysis Framework

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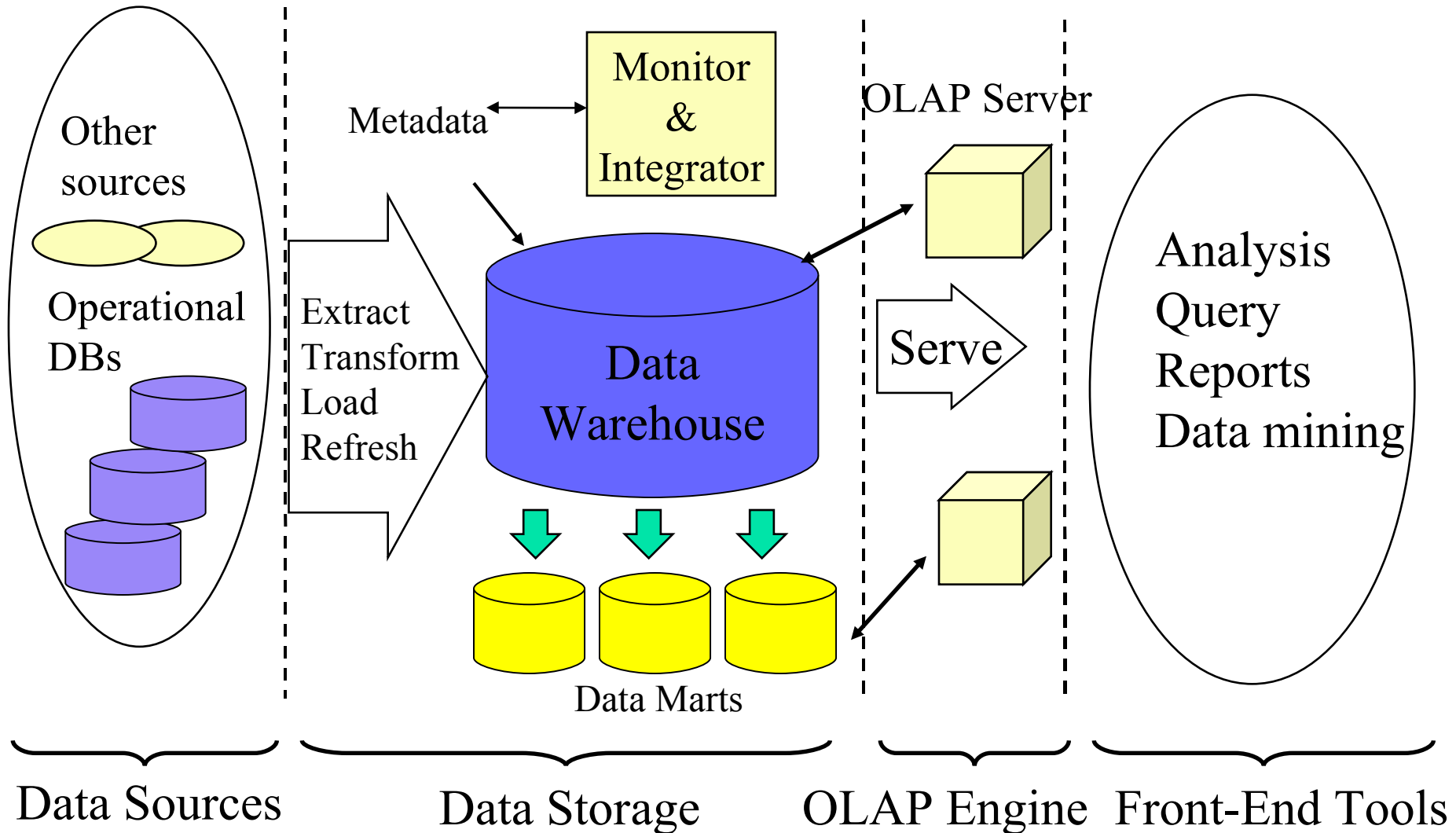
- Four views on the design of a data warehouse
  - **Top-down view**
    - allows selection of the relevant information necessary for the data warehouse
  - **Data source view**
    - exposes the information being captured, stored, and managed by operational systems
  - **Data warehouse view**
    - consists of fact tables and dimension tables
  - **Business query view**
    - sees the perspectives of data in the warehouse from the view of end-user

# Data Warehouse Design Process

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- Top-down, bottom-up approaches or a combination of both
  - Top-down: Starts with overall design and planning
  - Bottom-up: Starts with experiments and prototypes
- From software engineering point of view
  - Waterfall: structured and systematic analysis at each step before proceeding to the next
  - Spiral: rapid generation of increasingly functional systems, short turn around time, quick turn around
- Typical data warehouse design process
  - Choose a **business process** to model
  - Choose the ***grain (atomic level of data)*** of the business process
  - Choose the **dimensions** that will apply to each fact table record
  - Choose the **measure** that will populate each fact table record

# Data Warehouse: A Multi-Tiered Architecture



# Three Data Warehouse Models

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- **Enterprise warehouse**
  - collects all of the information about subjects spanning the entire organization
- **Data Mart**
  - a subset of corporate-wide data that is of value to a specific groups of users. Its scope is confined to specific, selected groups, such as marketing data mart
- **Virtual warehouse**
  - A set of views over operational databases
  - Only some of the possible summary views may be materialized

# Major Issues in Data Warehousing

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- Materialized View Selection and Maintenance (consistence, time and space constraints)
- Query Language Design
- Query Optimization (ad hoc queries)
- Data preprocessing and Integration
- User Interface Design

# Summary: Data Warehouse and OLAP Technology

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- Why data warehousing?
- A **multi-dimensional model** of a data warehouse
  - Star schema, snowflake schema
  - A data cube consists of dimensions & measures
- **OLAP** operations: drilling, rolling, slicing, dicing and pivoting
- Data warehouse architecture
- Data warehouse Implementation

# Data Warehouse and Data Mining Relationships

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- Data warehouse usage
- OLAP vs OLMP
- Integration of data warehousing and data Mining
- Major references (books, conferences, journals, and papers)

# Data Warehouse Usage

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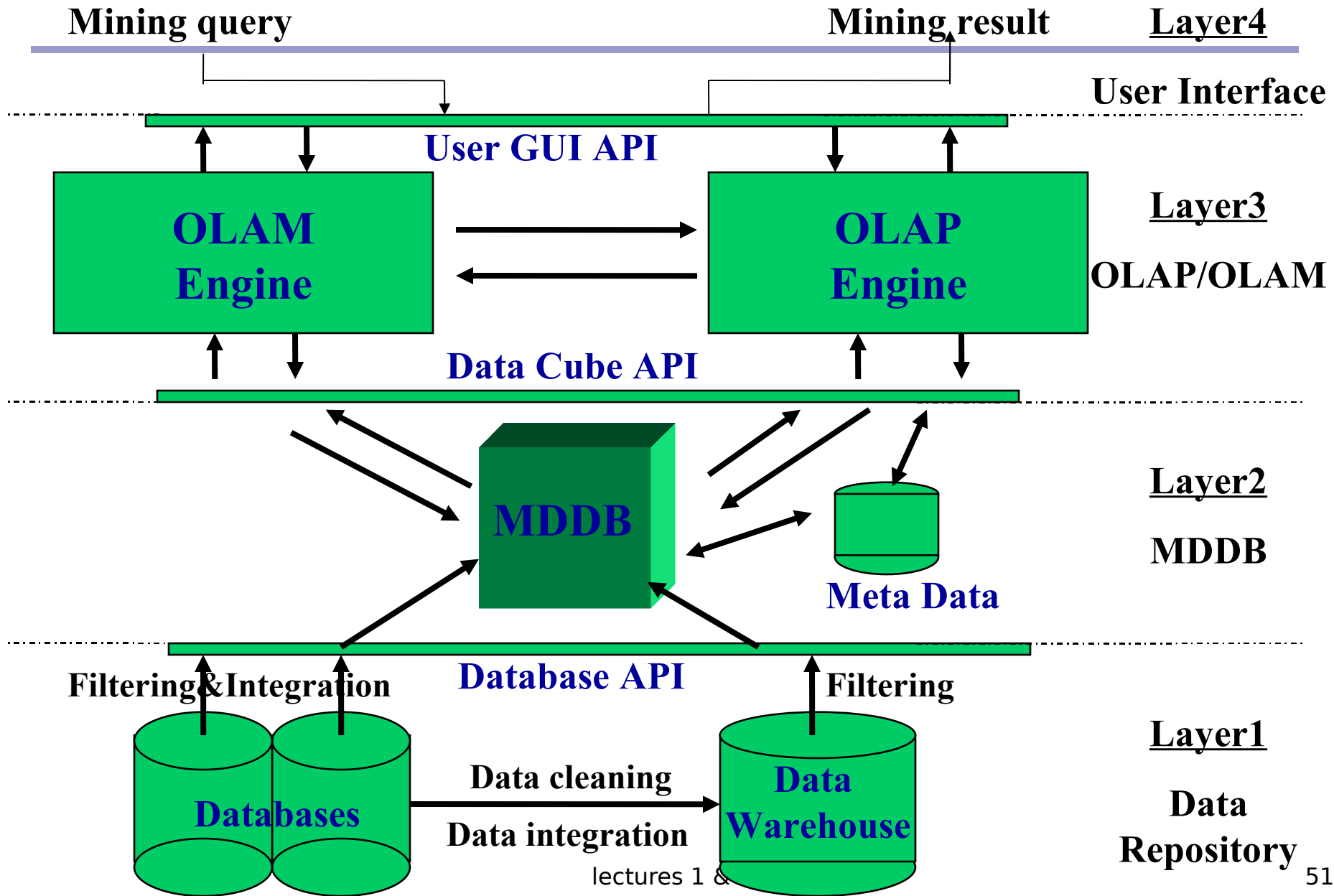
- Three kinds of data warehouse applications
  - **Information processing**
    - supports querying, basic statistical analysis, and reporting using crosstabs, tables, charts and graphs
  - **Analytical processing**
    - multidimensional analysis of data warehouse data
    - supports basic OLAP operations, slice-dice, drilling, pivoting
  - **Data mining**
    - knowledge discovery from hidden patterns
    - supports associations, constructing analytical models, performing classification and prediction, and presenting the mining results using visualization tools

# From On-Line Analytical Processing (OLAP) to On Line Analytical Mining (OLAM)

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- Why online analytical mining?
  - High quality of data in data warehouses
    - DW contains integrated, consistent, cleaned data
  - Available information processing structure surrounding data warehouses
    - ODBC, OLEDB, Web accessing, service facilities, reporting and OLAP tools
  - OLAP-based exploratory data analysis
    - Mining with drilling, dicing, pivoting, etc.
  - On-line selection of data mining functions
    - Integration and swapping of multiple mining functions, algorithms, and tasks

# An OLAM System Architecture



# Integration of Data Mining and Data Warehousing

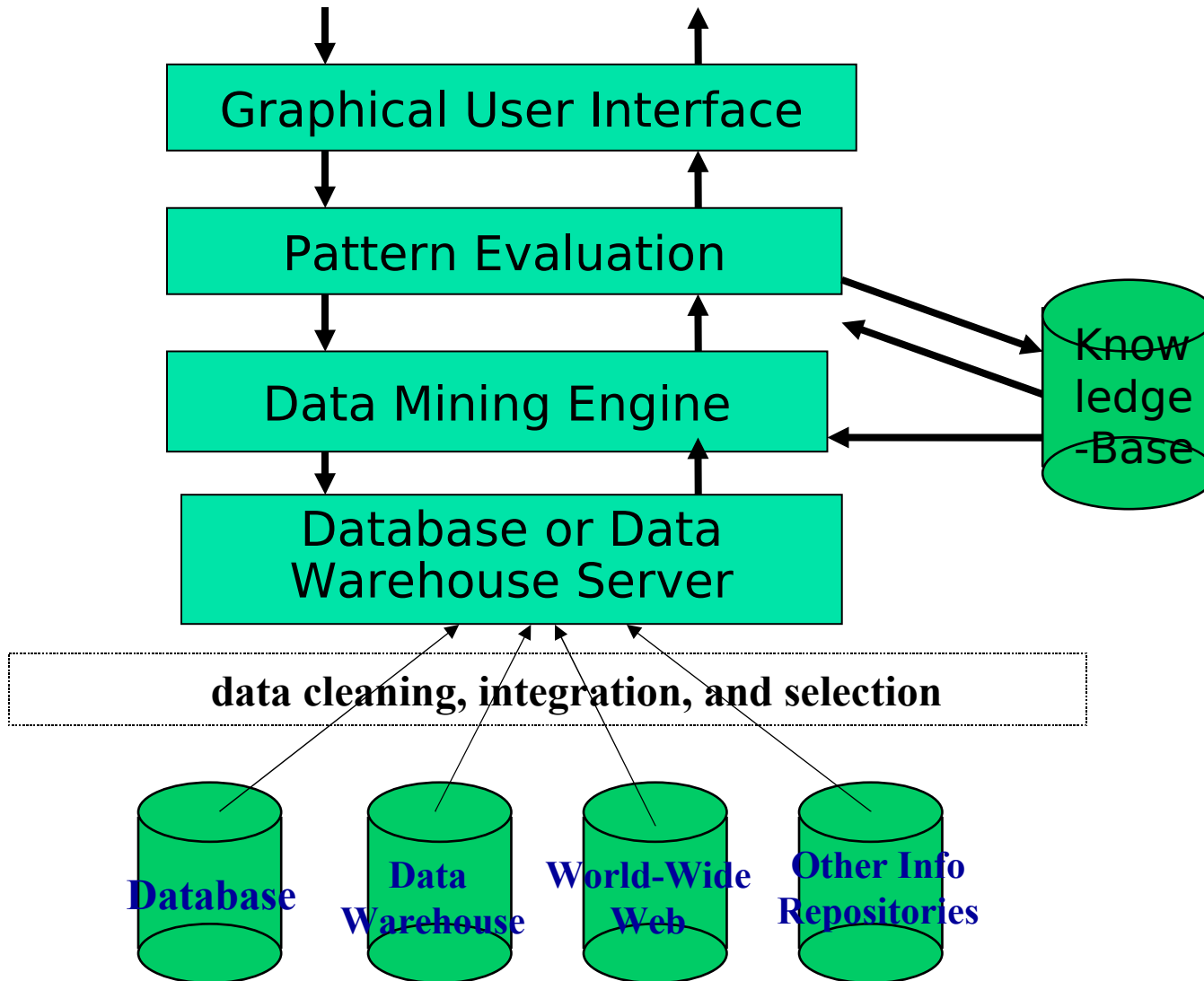
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- **Data mining systems, DBMS, Data warehouse systems coupling**
  - No coupling, loose-coupling, semi-tight-coupling, tight-coupling
- **On-line analytical mining data**
  - integration of mining and OLAP technologies
- **Interactive mining multi-level knowledge**
  - Necessity of mining knowledge and patterns at different levels of abstraction by drilling/rolling, pivoting, slicing/dicing, etc.
- **Integration of multiple mining functions**

# Coupling Data Mining with DB/DW Systems

- No coupling—flat file processing, not recommended
- Loose coupling
  - Fetching data from DB/DW
- Semi-tight coupling—enhanced DM performance
  - Provide efficient implement a few data mining primitives in a DB/DW system, e.g., sorting, indexing, aggregation, histogram analysis, multiway join, precomputation of some stat functions
- Tight coupling—A uniform information processing environment
  - DM is smoothly integrated into a DB/DW system, mining query is optimized based on mining query, indexing, query processing methods, etc

# Architecture: Typical Data Mining System



# Recommended Reference Books

- S. Chakrabarti. Mining the Web: Statistical Analysis of Hypertext and Semi-Structured Data. Morgan Kaufmann, 2002
- R. O. Duda, P. E. Hart, and D. G. Stork, Pattern Classification, 2ed., Wiley-Interscience, 2000
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- S. M. Weiss and N. Indurkha, Predictive Data Mining, Morgan Kaufmann, 1998
- J. H. Witten and E. Frank. Data Mining: Practical Machine Learning Tools and Techniques

# Conferences and Journals on Data Mining

- KDD Conferences
  - ACM SIGKDD Int. Conf. on Knowledge Discovery in Databases and Data Mining (**KDD**)
  - SIAM Data Mining Conf. (**SDM**)
  - (IEEE) Int. Conf. on Data Mining (**ICDM**)
  - Conf. on Principles and practices of Knowledge Discovery and Data Mining (**PKDD**)
  - Pacific-Asia Conf. on Knowledge Discovery and Data Mining (**PAKDD**)
- Other related conferences
  - ACM SIGMOD
  - VLDB
  - (IEEE) ICDE
  - WWW, SIGIR
  - ICML, CVPR, NIPS
- Journals
  - Data Mining and Knowledge Discovery (DAMI or DMKD)
  - IEEE Trans. On Knowledge and Data Eng. (TKDE)
  - KDD Explorations
  - ACM Trans. on KDD

# Where to Find References? DBLP, CiteSeer, Google

- Data mining and KDD (SIGKDD: CDROM)
  - Conferences: ACM-SIGKDD, IEEE-ICDM, SIAM-DM, PKDD, PAKDD, etc.
  - Journal: Data Mining and Knowledge Discovery, KDD Explorations, ACM TKDD
- Database systems (SIGMOD: ACM SIGMOD Anthology—CD ROM)
  - Conferences: ACM-SIGMOD, ACM-PODS, VLDB, IEEE-ICDE, EDBT, ICDT, DASFAA
  - Journals: IEEE-TKDE, ACM-TODS/TOIS, JIIS, J. ACM, VLDB J., Info. Sys., etc.
- AI & Machine Learning
  - Conferences: Machine learning (ML), AAI, IJCAI, COLT (Learning Theory), CVPR, NIPS, etc.
  - Journals: Machine Learning, Artificial Intelligence, Knowledge and Information Systems, IEEE-PAMI, etc.
- Web and IR
  - Conferences: SIGIR, WWW, CIKM, etc.
  - Journals: WWW: Internet and Web Information Systems,
- Statistics
  - Conferences: Joint Stat. Meeting, etc.
  - Journals: Annals of statistics, etc.
- Visualization
  - Conference proceedings: CHI, ACM-SIGGraph, etc.
  - Journals: IEEE Trans. visualization and computer graphics, etc.

# Data Warehousing References

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- S. Agarwal, R. Agrawal, P. M. Deshpande, A. Gupta, J. F. Naughton, R. Ramakrishnan, and S. Sarawagi. On the computation of multidimensional aggregates. VLDB'96
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