

Symbolic Execution for Automated Repair

[Prof. Abhik Roychoudhury](#)

National University of Singapore

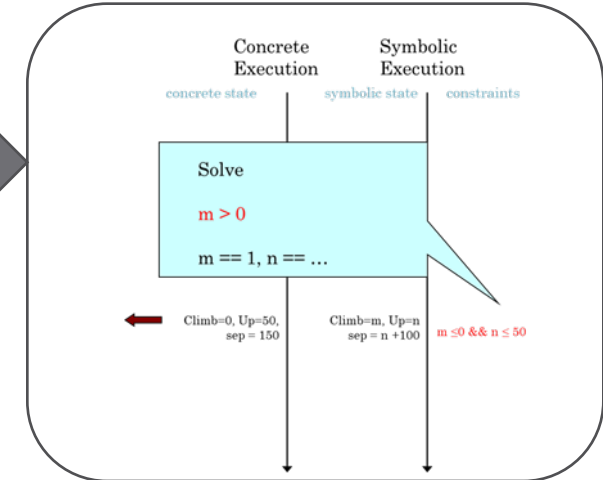
abhik@comp.nus.edu.sg

Recap: Use of Symbolic Execution

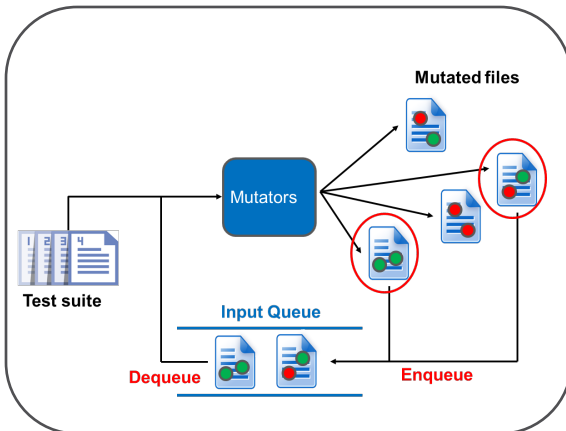
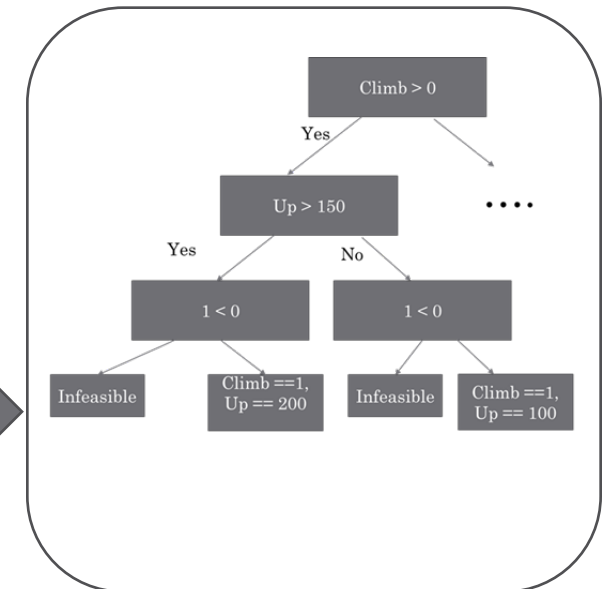


Bug Finding

- Concolic execution: supporting *real* executions [Directed Automated Random Testing]



- Symbolic execution tree construction e.g. KLEE [Modeling system environment]



- Grey-box fuzz testing for systematic path exploration inspired by concolic execution

AFLFast



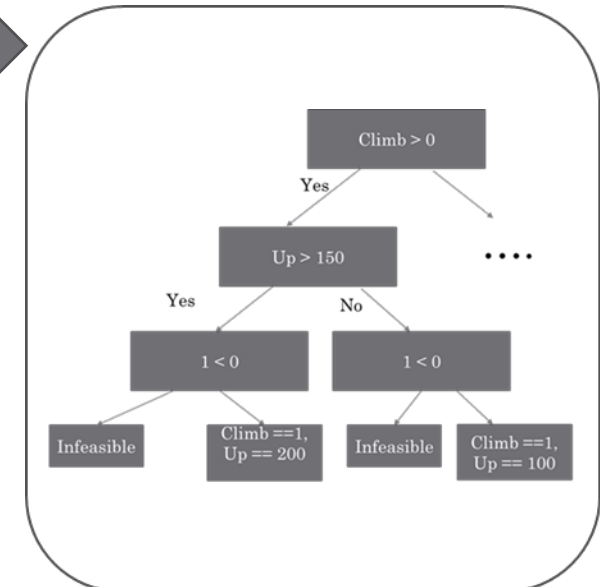
Recap: Use of Symbolic Execution



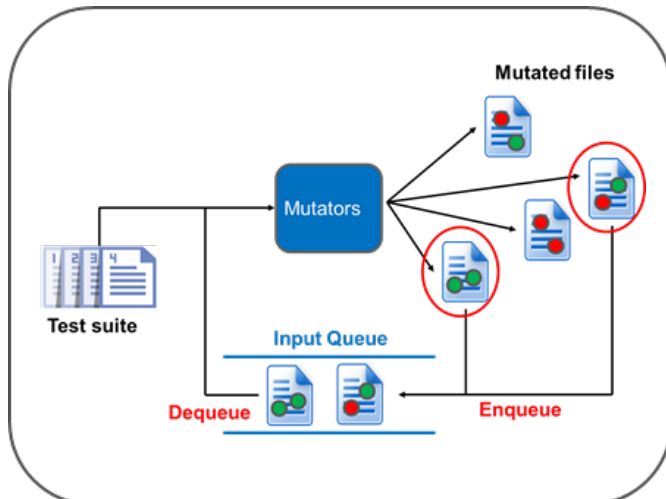
Reachability Analysis

Reachability of a location in the program

- Traverse the symbolic execution tree using search strategies e.g. KATCH



- Encode it as an optimization problem inside the genetic search of grey-box fuzzing **AFLGo**



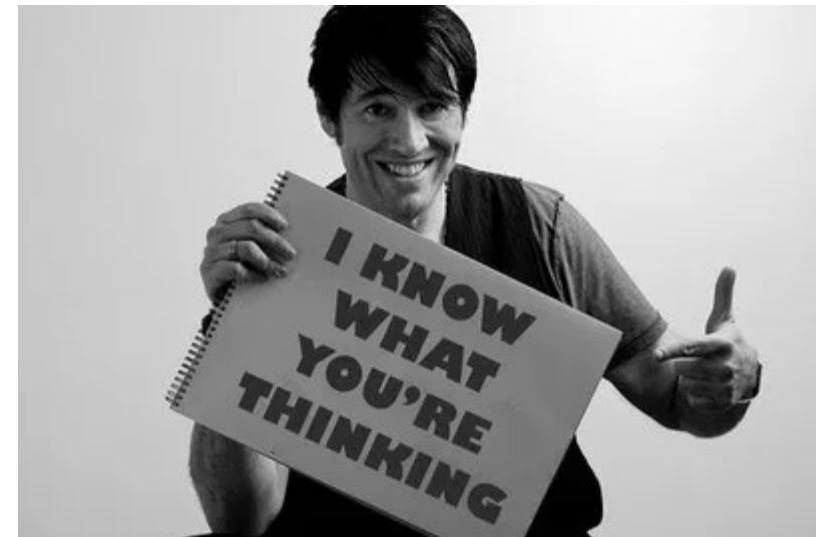
Reflections on Symbolic Execution



Specification Inference **(TODAY!)**

(application: localization, **repair**)

*In the absence of formal specifications,
analyze the buggy program and its artifacts
such as execution traces via various heuristics
to glean a specification about how it can pass
tests and what could have gone wrong!*



Bug Fixing

- Most software has many bugs.
- Security-related bugs should be fixed before they are exploited by malicious users.
- Oftentimes, bugs are not fixed even a few months after they were reported.
- E.g. Bug 18665 of glibc
 - Reported and responded on July 2015
 - Patched on Feb 2016
 - CVSS score: 8.1 / 10 (buffer overflow)
- *“Thanks for the bug report. Do you have a **test case** that triggers this scenario? Do you have a **patch** or suggested fix?”*

Background

- Why debugging is hard?
 - Huge search space ? OR ...
- What would make debugging easy?
 - Specification Inference
- Ideas in debugging which lead **to automated fixing**
 - Using implicit specification inference.

A quote from many years ago

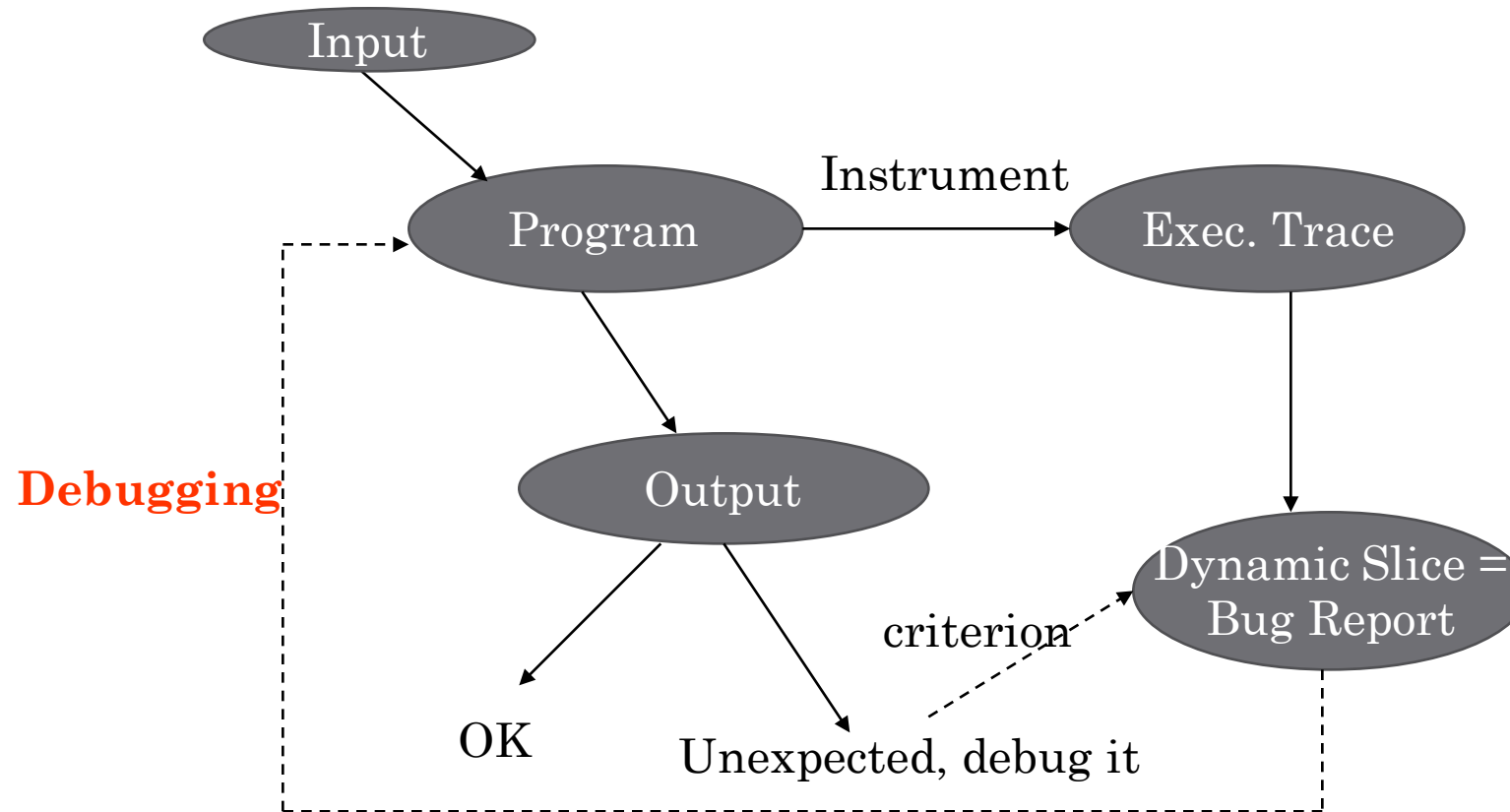
“Even today, debugging remains very much of an art. Much of the computer science community has largely ignored the debugging problem..... over 50 percent of the problems resulted from the time and space chasm between symptom and root cause or inadequate debugging tools.”

Hailpern & Santhanam, IBM Systems Journal, 41(1),
2002

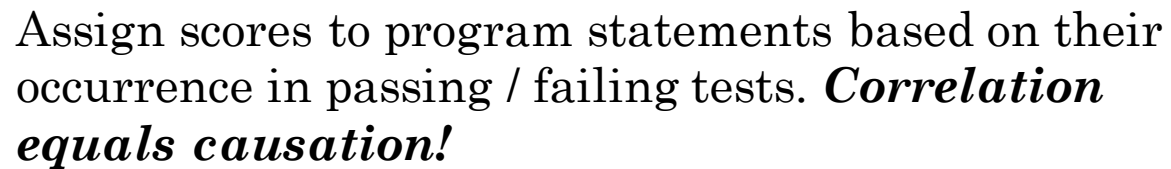
Any progress in 2002 – 2018?

How can symbolic execution help?

Dynamic slicing: a debugging aid

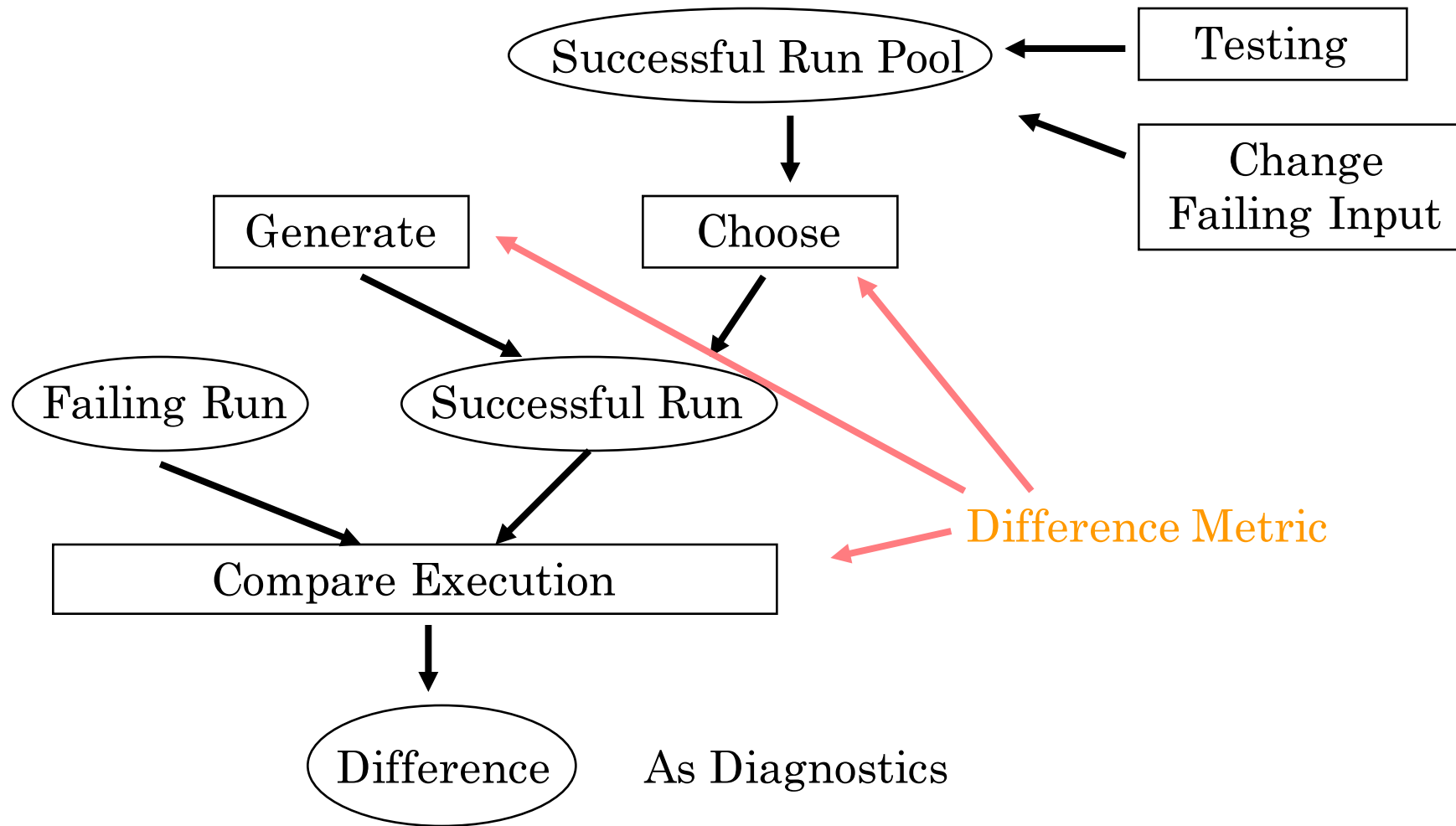


9



An example of scoring scheme [Tarantula]

Trace Comparison based Debugging



A moment's note for the students

- You have – buggy program, failing tests
 - You do not have **specification of intended behavior**, try to discover
 - [What the program is supposed to do]
-
- Compare this to software model checking
 - You have formal specification of intended behavior (temporal logic property)
 - You have the buggy program
 - You do not have failing tests (counter-examples), try to discover.

What is the intended behavior?

Only in the programmer's mind?

Assertions capturing programmer's intent at each statement

Too much overhead on programmer: almost as much work as a proof

Source of Information	Name of Symbolic Technique
Internal inconsistency	Cause Clue Clauses [PLDI 11] Error Invariants [FM 12]
Passing Tests	Angelic Debugging [ICSE 11]
Previous version / Golden implementation	Regression Debugging [FSE09, FSE10, FSE11]

Example

Input: `a, index`

1. `base = a;`
2. `sentinel = base;`
3. `offset = index;`
4. `address = base + offset;`
5. `output address, sentinel`

Test 1

`<a, index==10>`

`assert sentinel <=`
`address`

`assert address < a + 10`



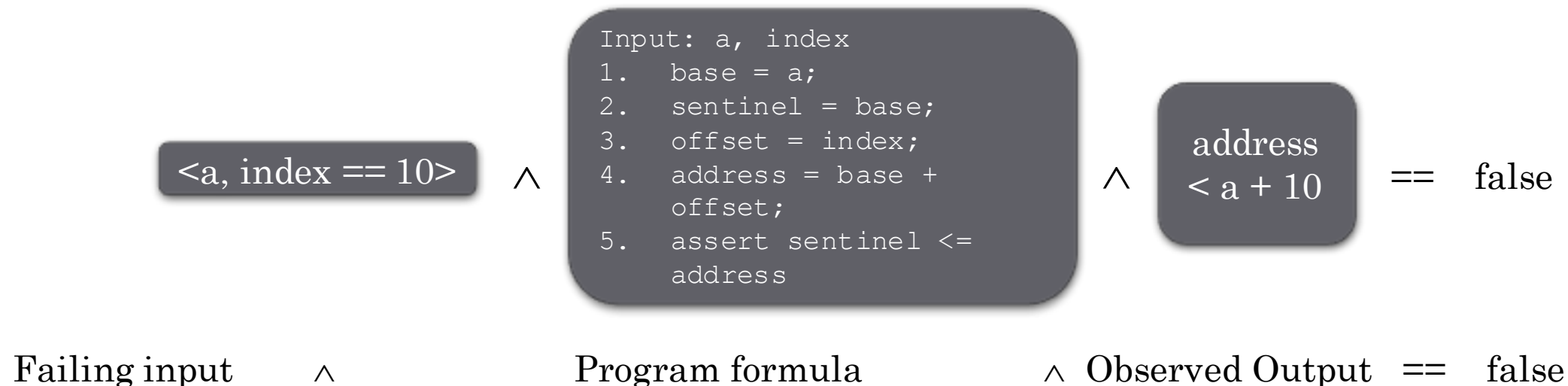
Test 2

`<a, index==9>`

`assert sentinel <=`
`address`

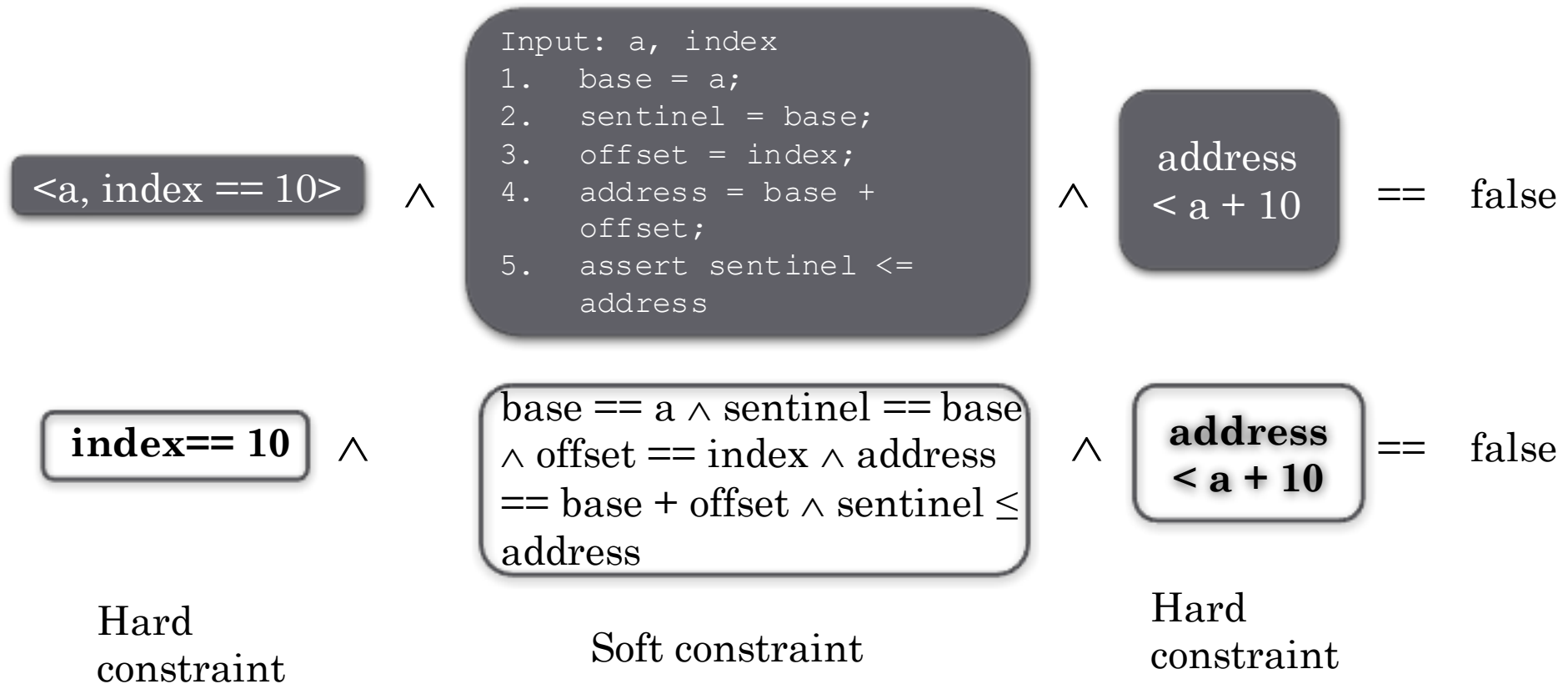
`assert address < a + 10`

CCC : General idea

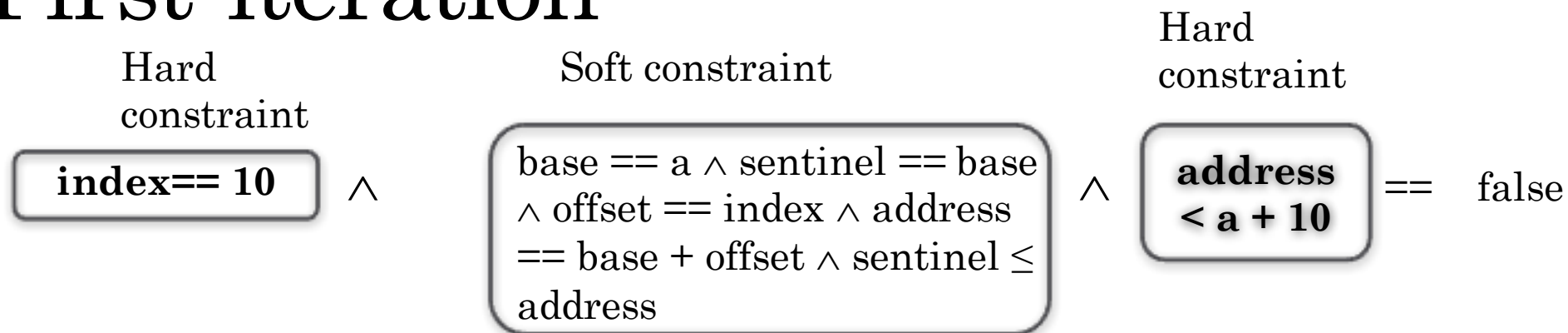


Cause Clue Clauses, Jose and Majumdar, PLDI 2011.

CCC: General idea



First iteration



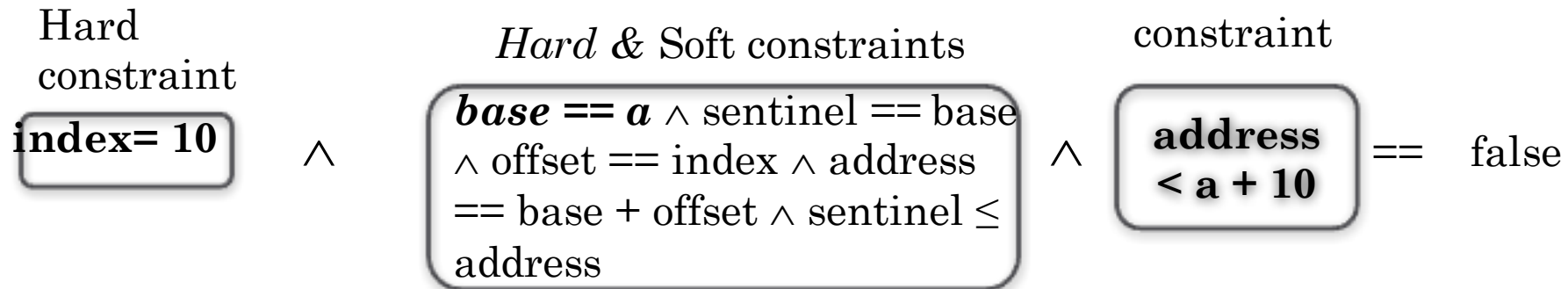
Running Partial MAXSAT, we get **base == a** as a soft constraint that can be removed.

Corresponds to the fix:

```

Input: a, index
1.  base = a - 1;
2.  sentinel = base;
3.  offset = index;
4.  address = base + offset;
5.  output address, sentinel
  
```


Moving further



We mark ***base == a*** as hard now, and run Partial MaxSAT again, to get **offset == index**.

Corresponds to the fix:

```
Input: a, index
1. base = a;
2. sentinel = base;
3. offset = index - 1;
4. address = base + offset;
5. output address, sentinel
```

The clause
 sentinel == base does
 not help (or hurt)

Fix determines fault

```
Input: a, index
1.  base = a;
2.  sentinel = base;
3.  offset = index;
4.  address = base + offset;
5.  output address, sentinel
```

Off-by-one
error

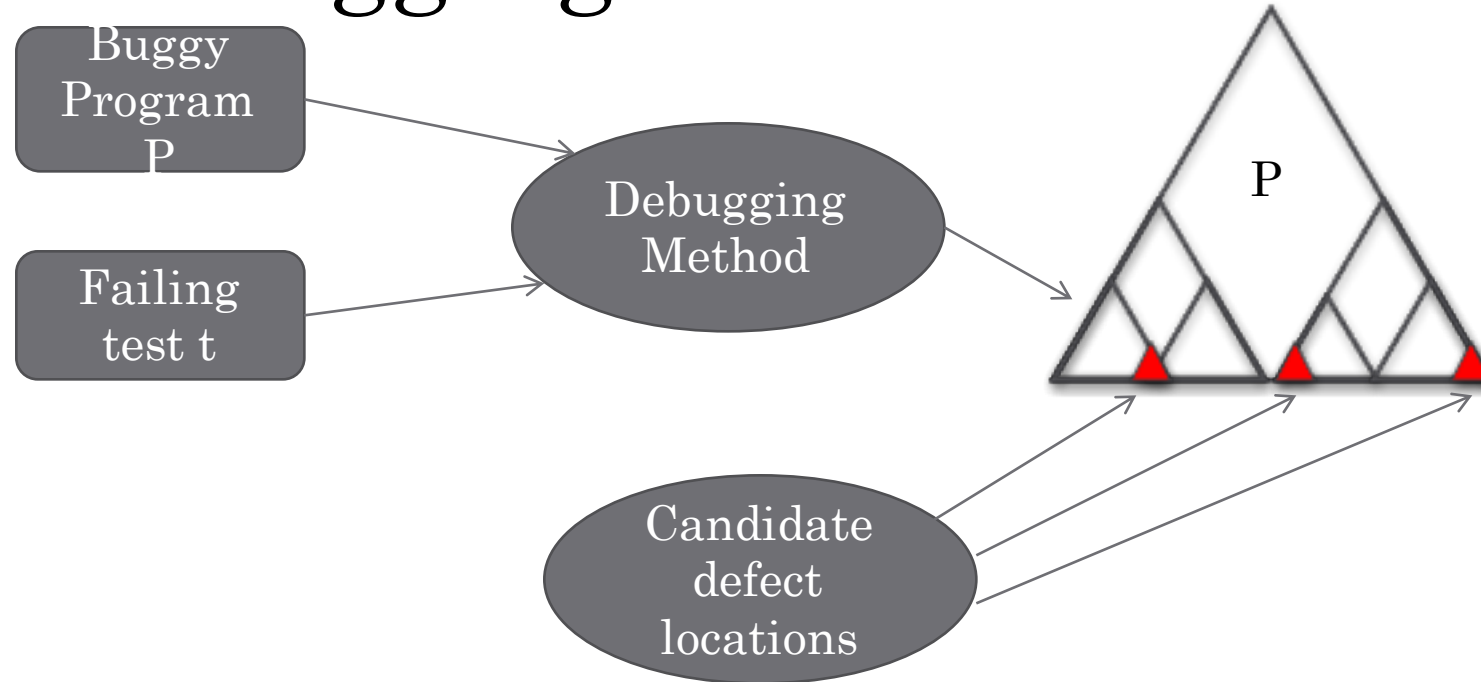
```
Input: a, index
1.  base = a - 1;
2.  sentinel = base;
3.  offset = index;
4.  address = base + offset;
5.  output address, sentinel
```

```
Input: a, index
1.  base = a;
2.  sentinel = base;
3.  offset = index - 1;
4.  address = base + offset;
5.  output address, sentinel
```

Specification discovery?

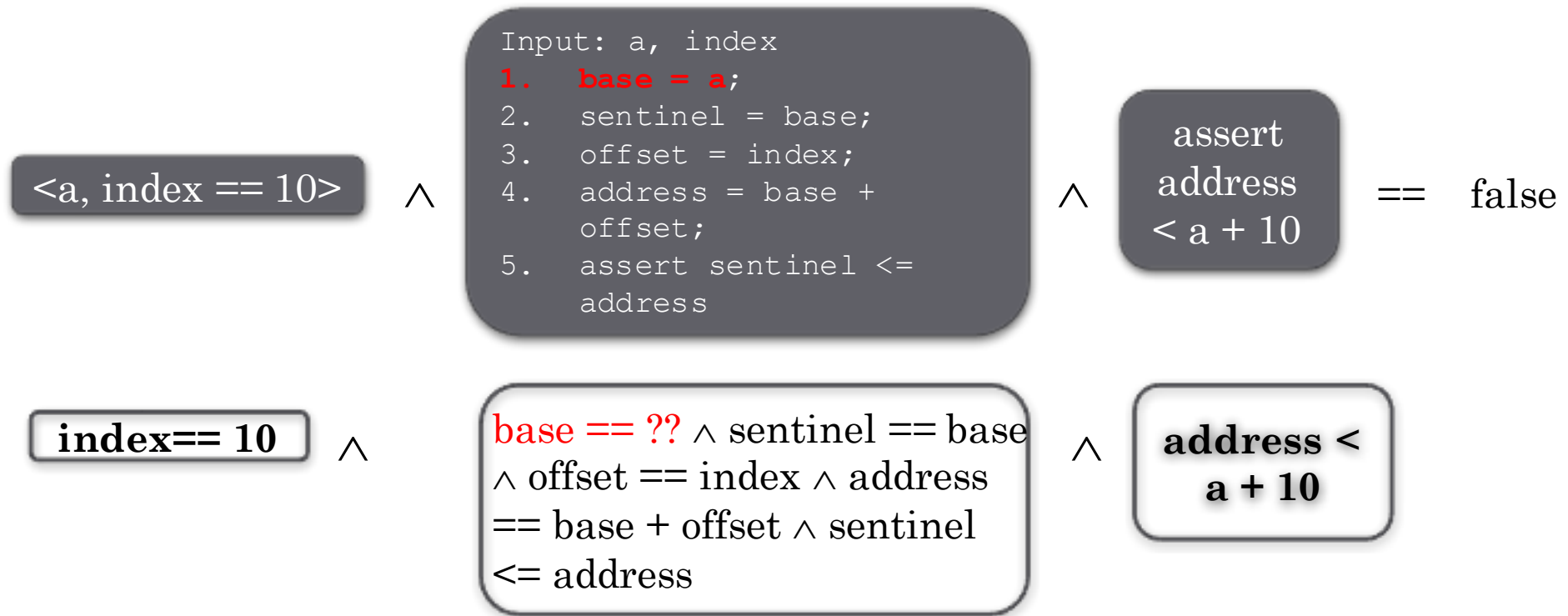
- Find statements that cause inconsistency in the failing execution
 - Removal of that inconsistency makes the error go away
 - Minimal inconsistency \rightarrow cause
 - Starting point for repair
- Simple specification discovery
 - Removing statement S causes error to disappear
 - **Do not know what S should have been!**

Angelic Debugging



Define possible defect locations by identifying expressions which can fix the fault!

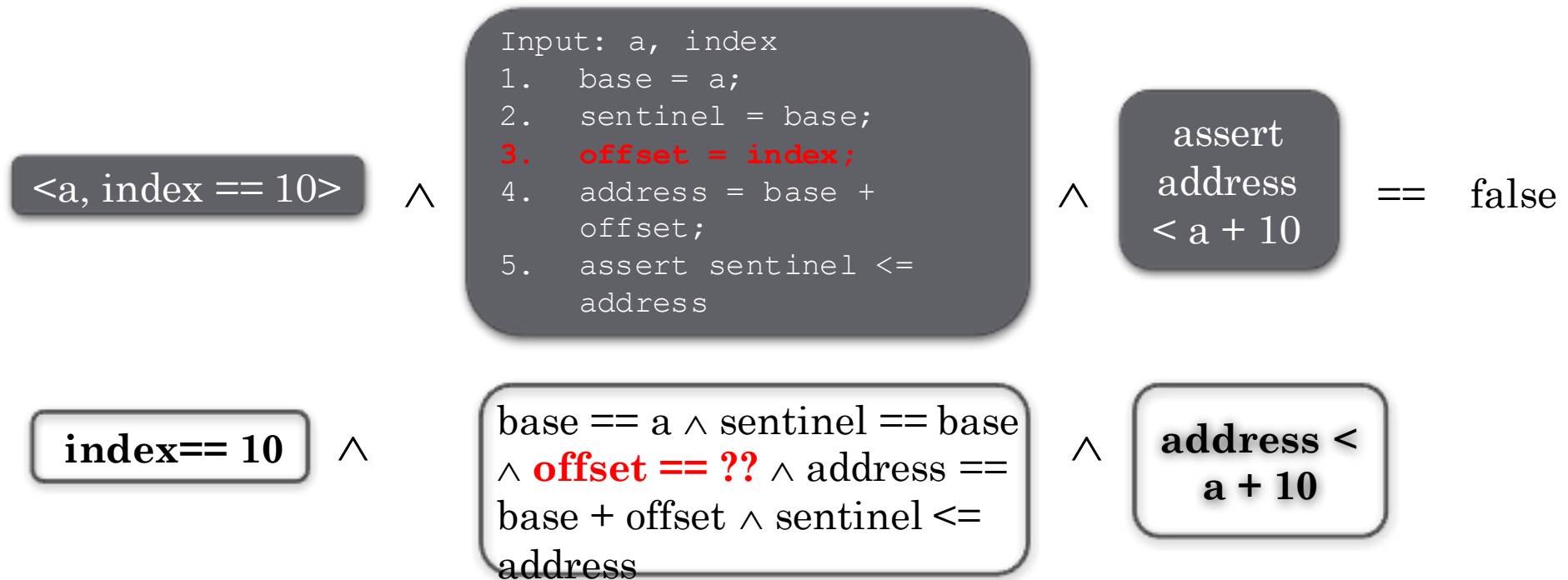
General idea – fix failing tests,...



base = a is a valid fix location.

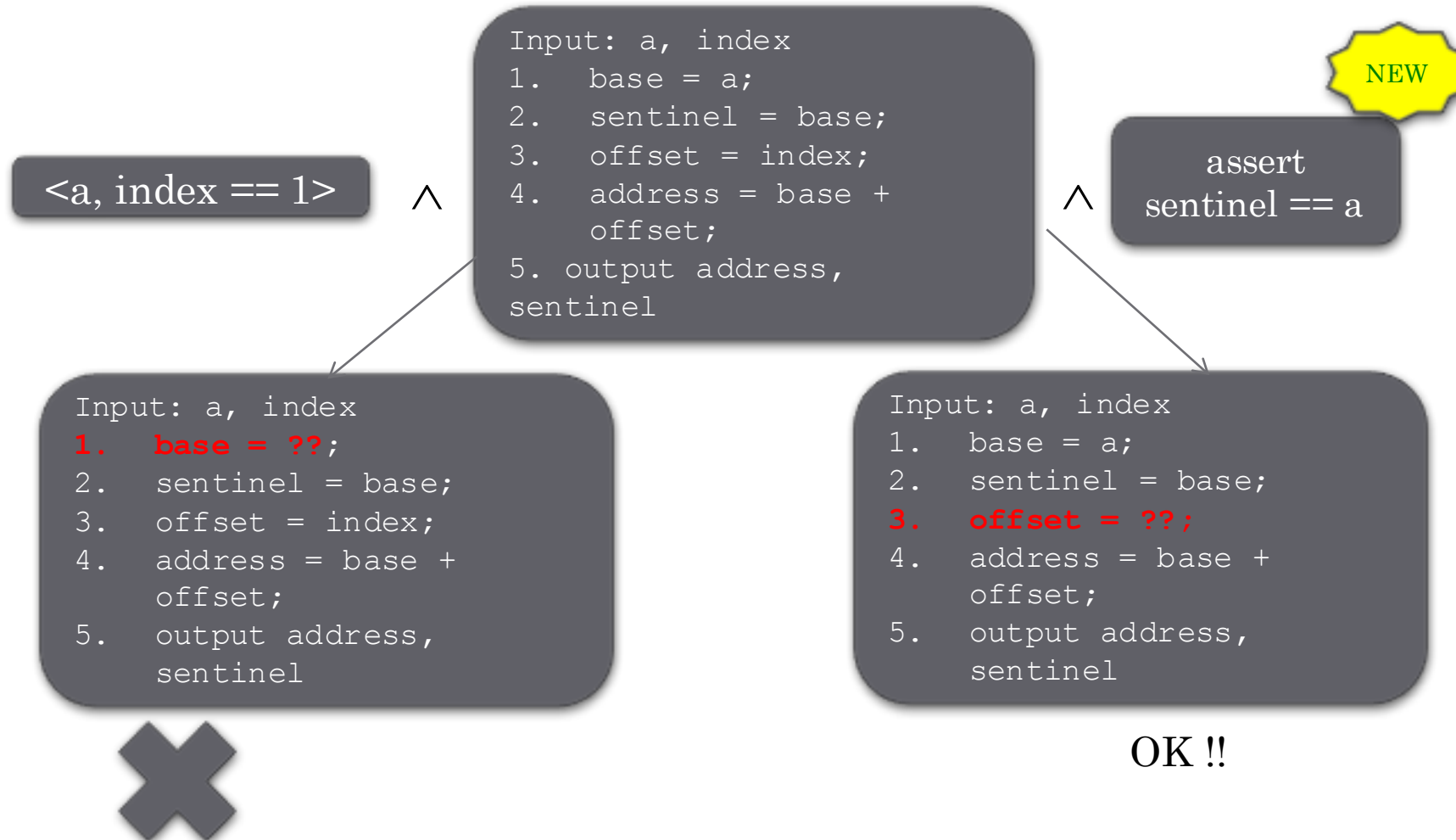
Note: Does not suggest the repaired statement `base = a - 1`.

Fix failing tests, ...



offset = index is another valid fix location.

..., and do not break passing tests



Specification discovery?

- Passing tests tell us which expressions are “inflexible”
 - The better your test suite is, the more you know!
- Therefore, the bug must be in one of the flexible expressions
- *Limitations*
 - Assumption of 1-fixable
 - Quality of filtering depends on the goodness of test suite
 - Subject to implementation of the symbolic analysis

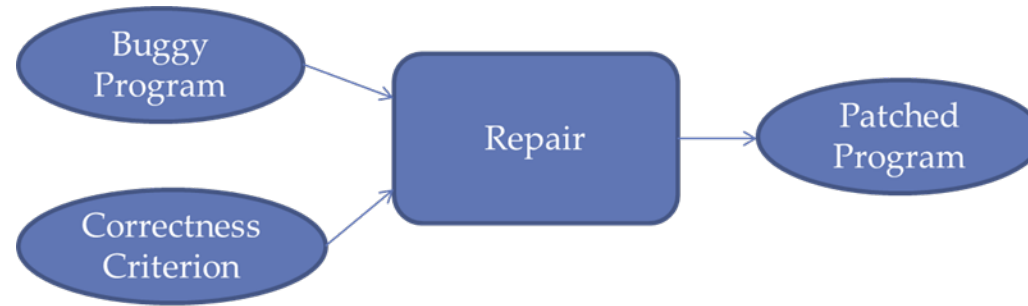
Retrospective

Debugging – some milestones

- Manual era: prints and breakpoints
- Statistical fault localization [e.g. Tarantula]
- Dynamic slicing [e.g. JSlice]
- Trace comparison and delta debugging
 - Look for workarounds – *how to avoid the error?*
- **Symbolic techniques**
 - Replace repeated experimentation with constraint solving.
 - Discover and (partially) infer intended semantics by symbolic analysis
- **The Future: repair (hints)**

Syntactic Program Repair

Automated Program Repair



- [OLD] *Large search space* of candidate patches for general-purpose repair tools.
- [NEW] Weak description of intended behavior / *correctness criterion* e.g. tests
- [FUTURE] Patch suggestions and *Interactive Repair*

Research Issues in Program Repair

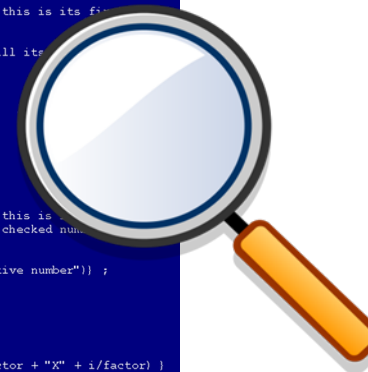
- [OLD] *Large search space* of candidate patches for general-purpose repair tools.
- -> *What should I use?*
- -> *Which search frameworks could we use?*
- -> *Syntactic Program Repair*
- [NEW] Weak description of intended behavior / *correctness criterion* e.g. tests
- -> *Overfitting of a patch candidate to tests?*
- -> *Extract specification from test executions to reduce overfitting.*
- -> *Do so, while still navigating the search space*
- -> *Semantic Program Repair*

Division of Labor

Syntactic Program Repair

```
function check(n)
{
  // check if the number n is a prime
  var factor; // if the checked number is not a prime, this is its factor
  var c;
  factor = 0;
  // try to divide the checked number by all numbers till its sqrt
  for (c=2; (c <= Math.sqrt(n)); c++)
  {
    if (n%c == 0) // is n divisible by c ?
    {
      factor = c; break;
    }
  }
  return (factor);
} // end of check function

function communicate()
{
  // communicate with the user
  var i; // i is the checked number
  var factor; // if the checked number is not a prime, this is its factor
  i = document.primestest.number.value; // get the checked number
  // is it a valid input?
  if ((isNaN(i)) || (i <= 0) || (Math.floor(i) != i))
  {
    alert ("The checked object should be a whole positive number");
  }
  else
  {
    factor = check (i);
    if (factor == 0)
    {
      alert (i + " is a prime");
    }
    else
    {
      alert (i + " is not a prime, " + i + " = " + factor + " * " + i/factor);
    }
  }
} // end of communicate function
```



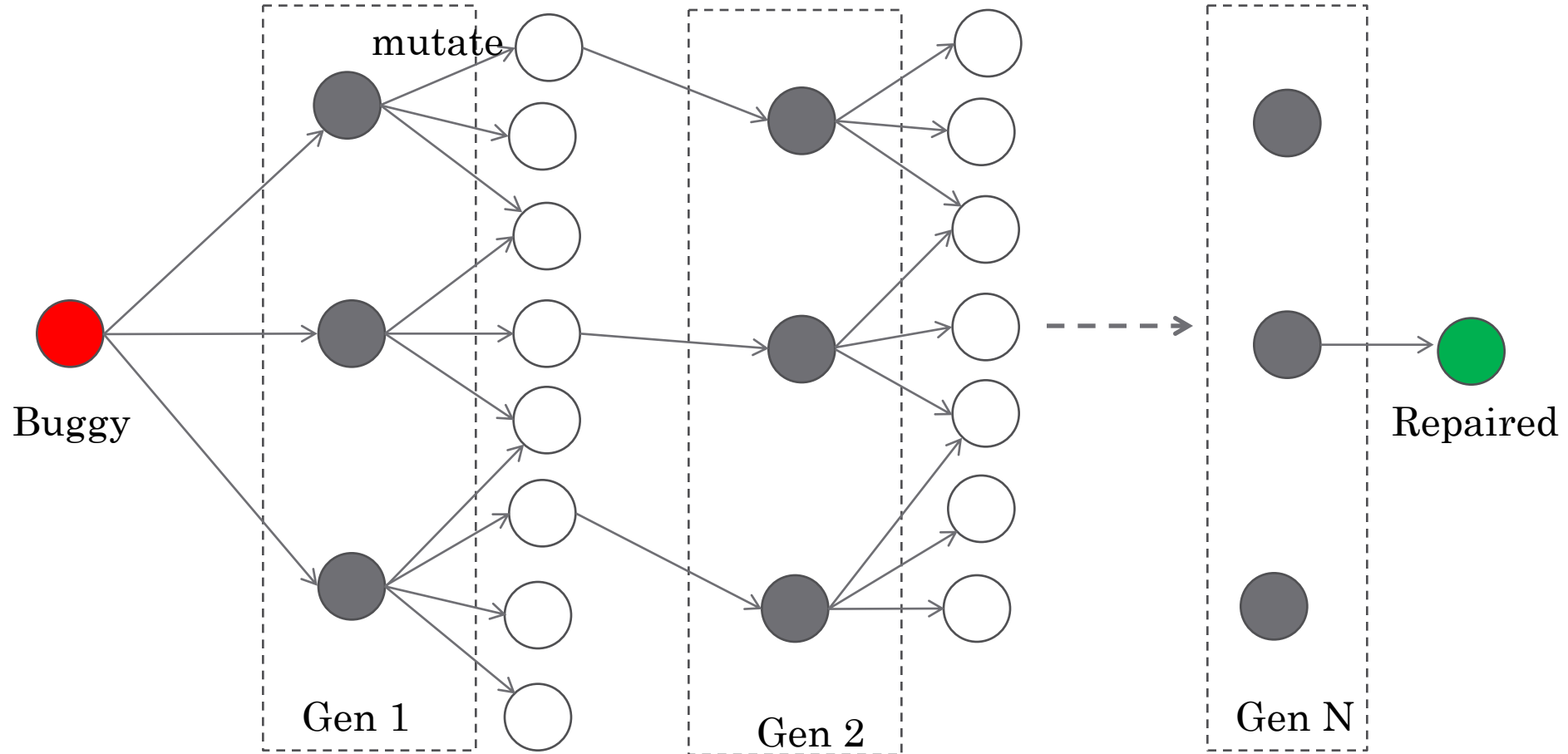
1. Where to fix, which line?
2. Generate patches in the candidate line
3. Validate the candidate patches against correctness criterion.

Semantic Program Repair

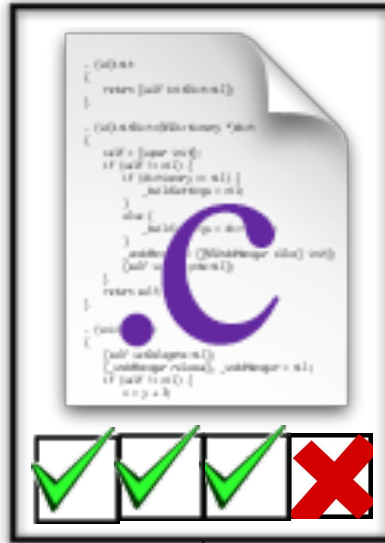
1. Where to fix, which line(s)?
2. What values should be returned by those lines, e.g. `<inp ==1, ret== 0>`
3. What are the expressions which will return such values?

GenProg – repair via search

(Ack: Claire Le Goues)



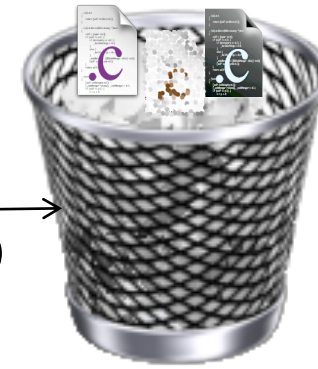
INPUT



EVALUATE FITNESS



DISCARD



ACCEPT



MUTATE



OUTPUT

Ack: Claire Le Goues (CMU)

> gcd(4,2)

> 2

>

> gcd(1071,1029)

> 21

>

> gcd(0,55)

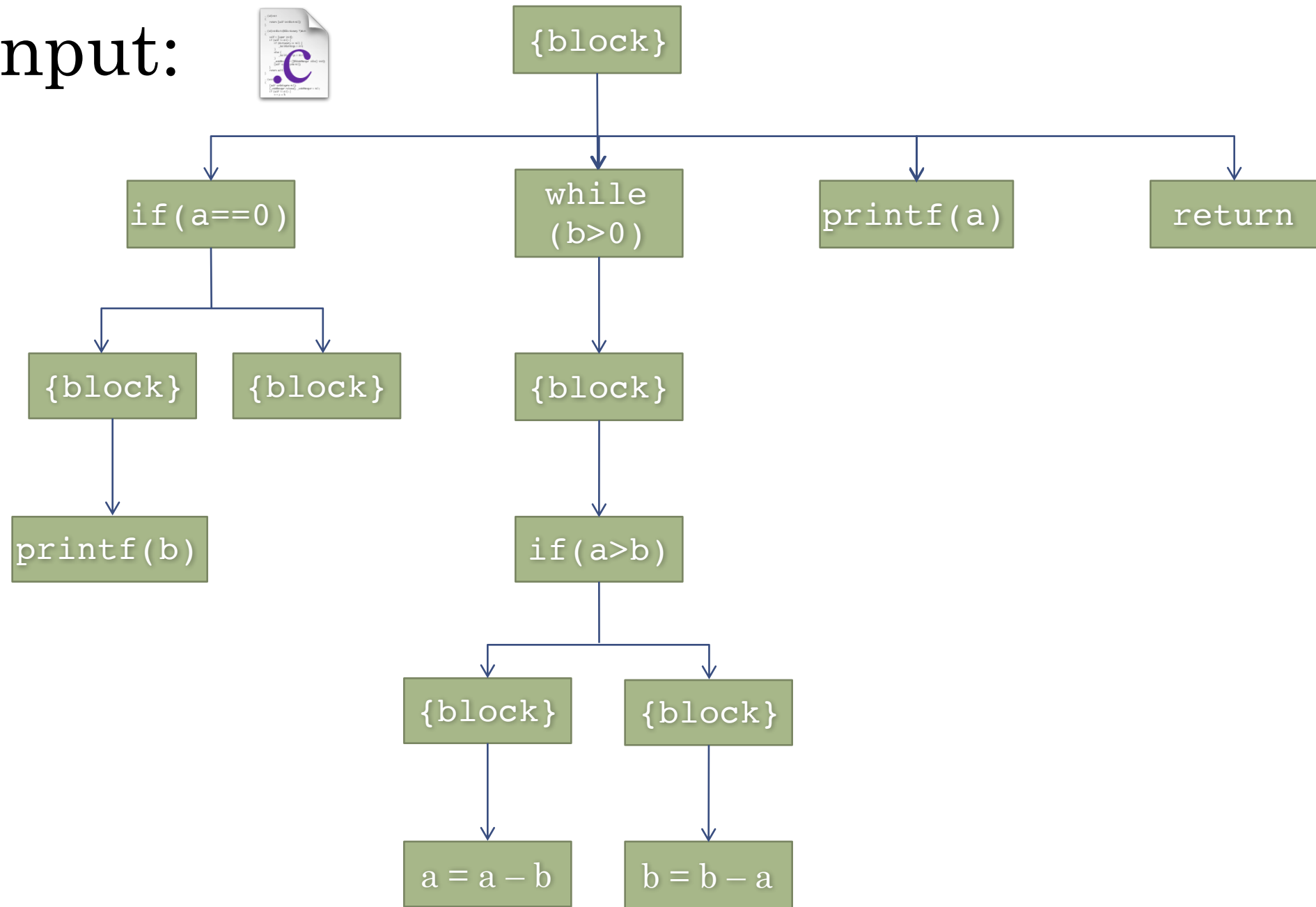
> 55

(looping forever)

```
1 void gcd(int a, int b) {
2     if (a == 0) {
3         printf("%d", b);
4     }
5     while (b > 0) {
6         if (a > b)
7             a = a - b;
8         else
9             b = b - a;
10    }
11    printf("%d", a);
12    return;
13 }
```

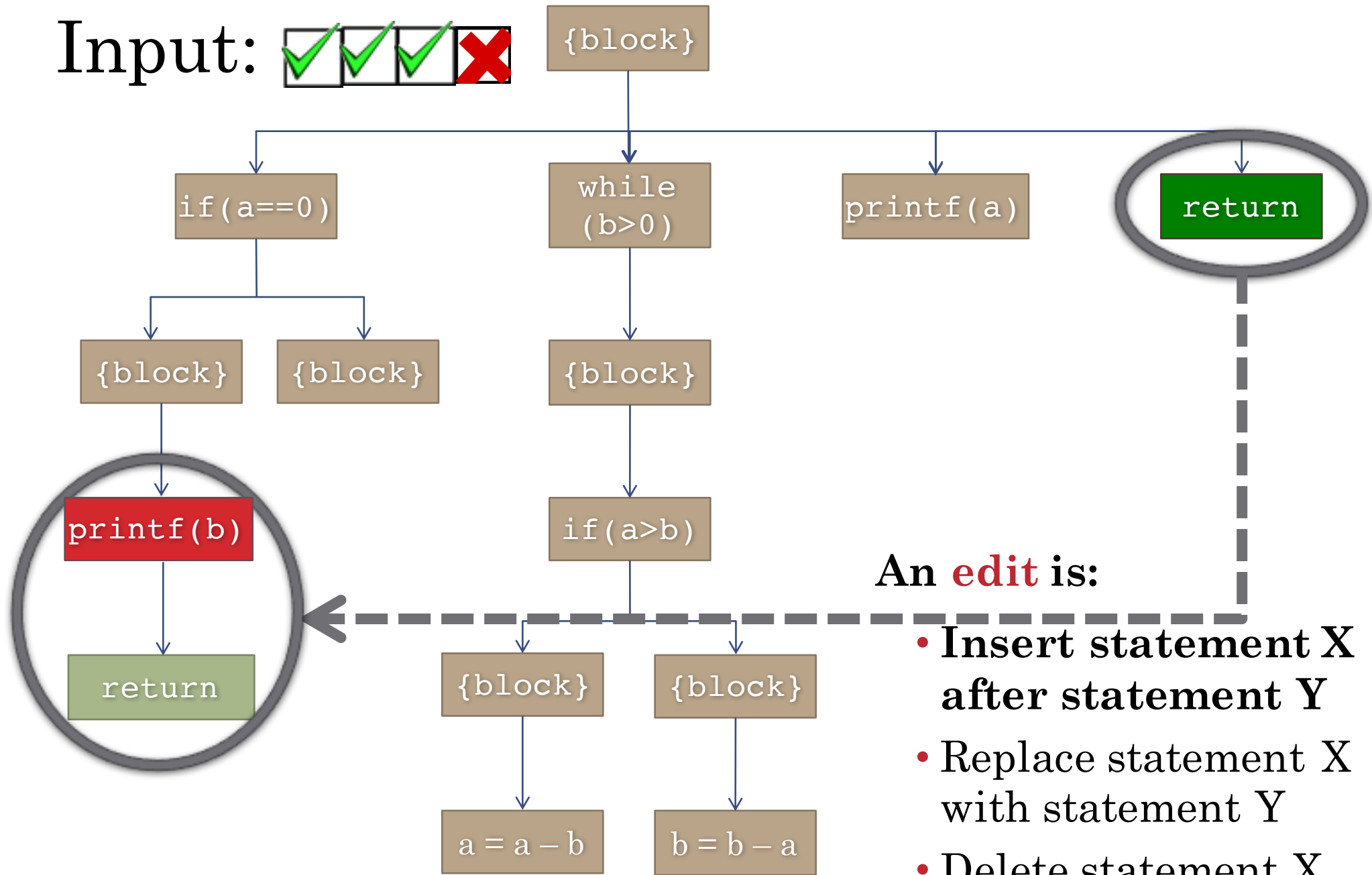
Ack: Claire Le Goues (CMU)

Input:



Ack: Claire Le Goues (CMU)

Input: 



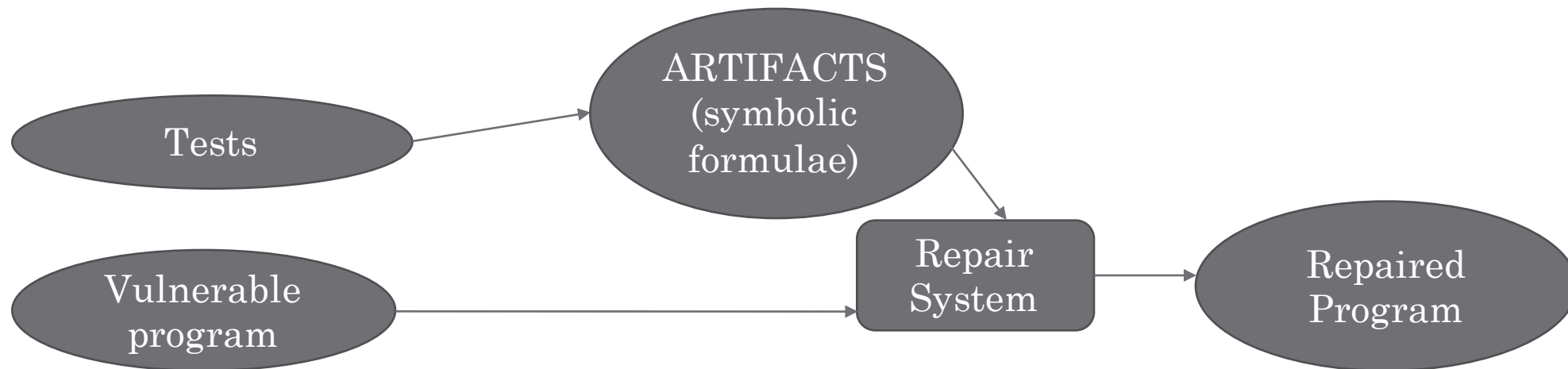
An **edit** is:

- Insert statement X after statement Y
- Replace statement X with statement Y
- Delete statement X

Over-fitting in Repair

Avoid generating programs like

```
if (input1) return output1  
else if (input2) return output2  
else if (input3) return output3  
....
```



Generalize beyond the provided tests using symbolic reasoning.

Comparison

Syntactic Program Repair

Syntax-based Schematic
 for e in **Search-space**{
 Validate e against Tests
 }

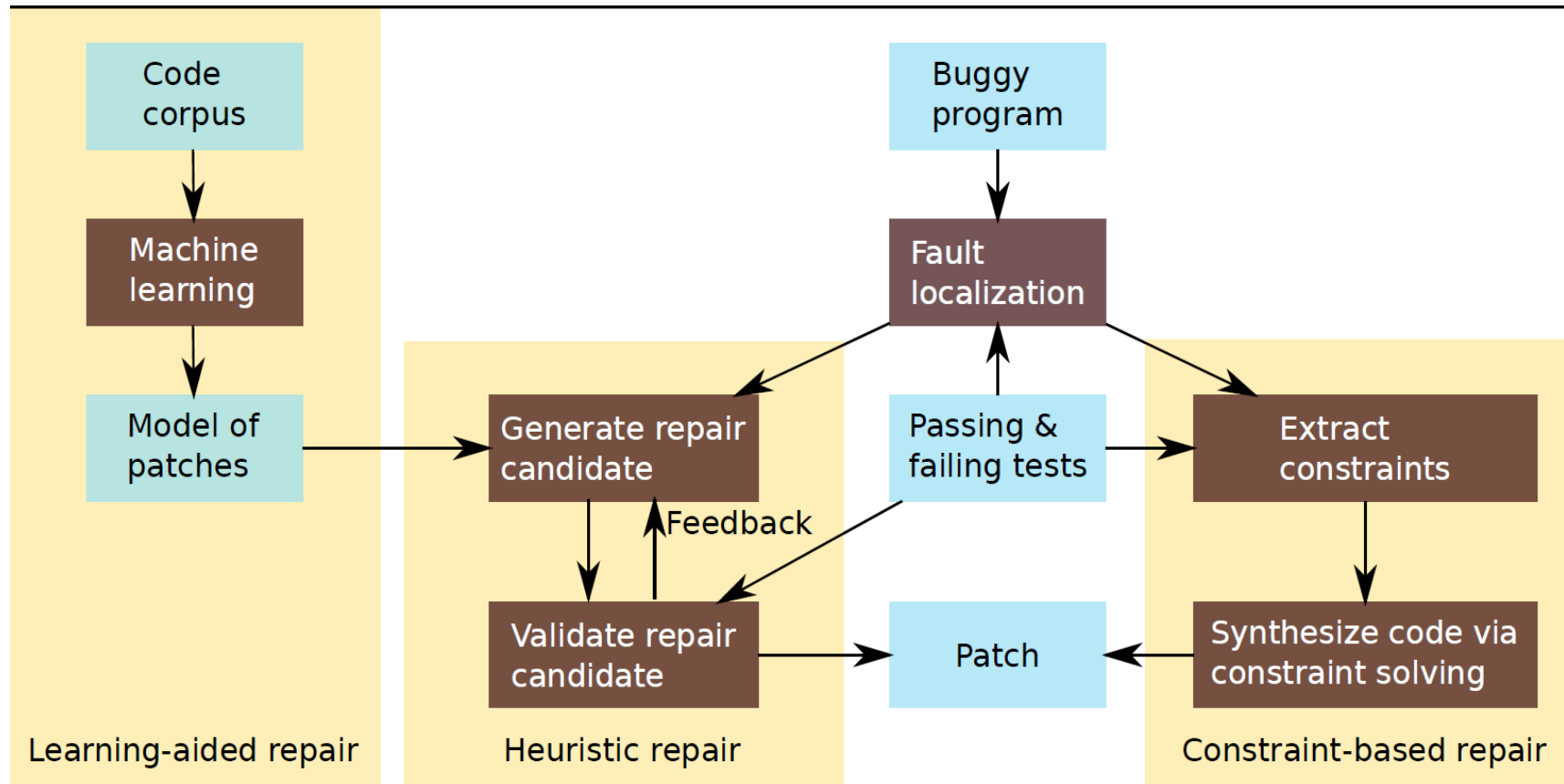
1. Where to fix, which line?
2. Generate patches in the candidate line
3. Validate the candidate patches against correctness criterion.

Semantic Program Repair

Semantics-based Schematic
 for t in **Tests** {
 generate repair constraint Ψ_t
 }
 Synthesize e from $\bigwedge_t \Psi_t$

1. Where to fix, which line(s)?
2. What values should be returned by those lines, e.g. <inp ==1, ret== 0>
3. What are the expressions which will return such values?

State-of-the-art



Ack: Figure by Le Goues(CMU), Pradel (Darmstadt), Roychoudhury (NUS)

```

1 int triangle(int a, int b, int c){
2     if (a <= 0 || b <= 0 || c <= 0)
3         return INVALID;
4     if (a == b && b == c)
5         return EQUILATERAL;
6     if (a == b || b != c) // bug!
7         return ISOSCELES;
8     return SCALENE;
9 }

```

Correct fix
 $(a == b \ || \ b == c \ || \ a == c)$

Traverse all *mutations* of line 6, and check

Hard to generate correct fix since $a == c$ never appears elsewhere in the program.

OR

Generate the constraint

$$f(2,2,3) \wedge f(2,3,2) \wedge f(3,2,2) \wedge \neg f(2,3,4)$$

And get the solution

$$f(a,b,c) = (a == b \ || \ b == c \ || \ a == c)$$

Test id	a	b	c	oracle	Pass
1	-1	-1	-1	INVALID	pass
2	1	1	1	EQUILATERAL	pass
3	2	2	3	ISOSCELES	pass
4	2	3	2	ISOSCELES	fail
5	3	2	2	ISOSCELES	fail
6	2	3	4	SCALENES	fail

Semantic Program Repair

Prof. Abhik Roychoudhury

National University of Singapore

Challenge 1: Search Space Explosion

Buggy program

```
scanf ("%d", &x) ;  
int t = x - 1 ;  
if (t > 0) printf ("1") ;  
else printf ("0") ;
```

Test

$P(1) \longrightarrow 1$

Failing test

Huge search space of candidate patches

$x - 1 \longrightarrow x - 2$

$x - 1 \longrightarrow x + 1$

...

Challenge 2: Overfitting

Buggy program

```
scanf ("%d", &x) ;
int t = x - 1;
if (t > 0) printf ("1") ;
else printf ("0") ;
```

Huge space of plausible patches

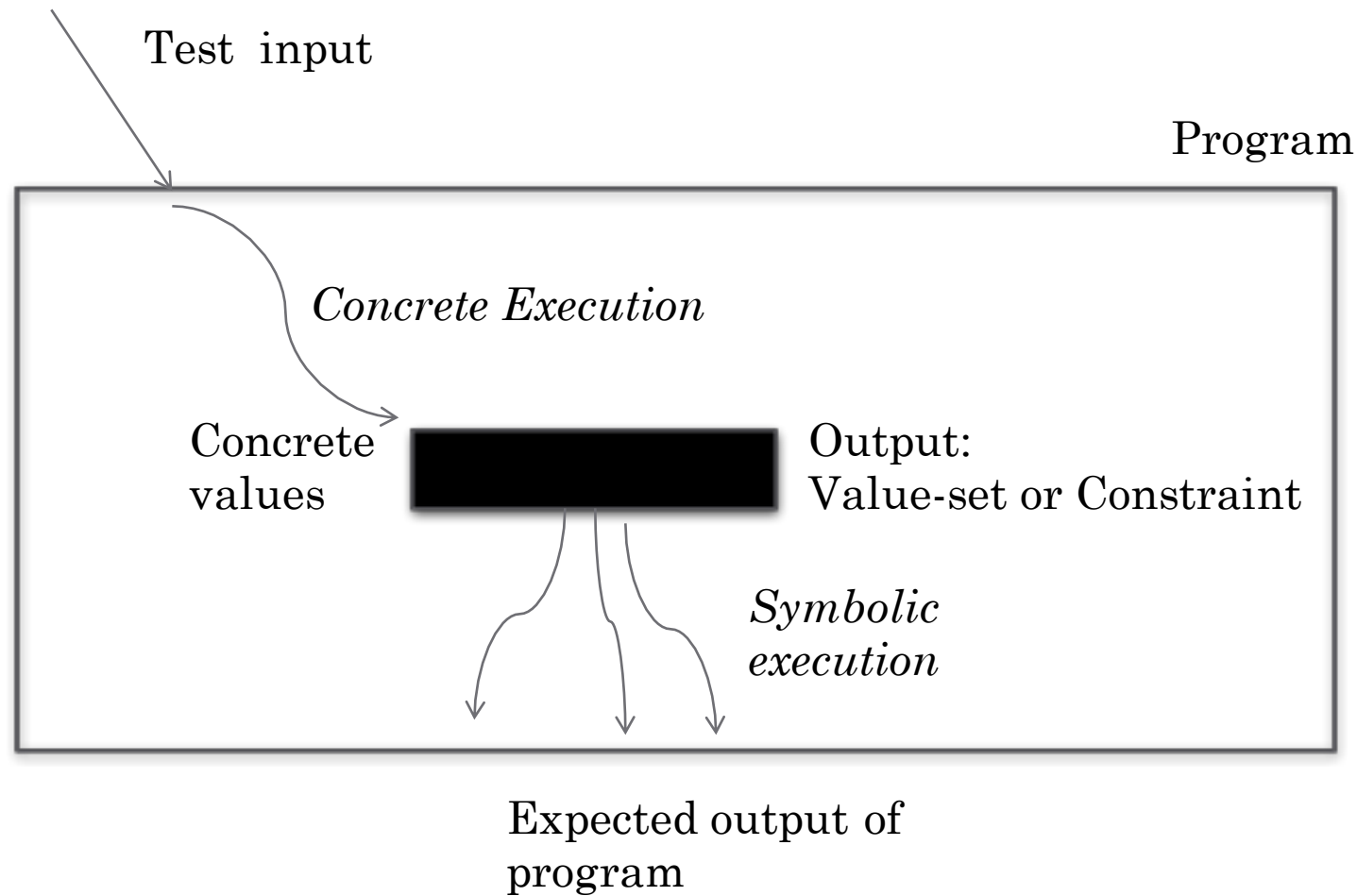
```
x - 1 → 1
x - 1 → x
x - 1 → x + 1
...
```

Test

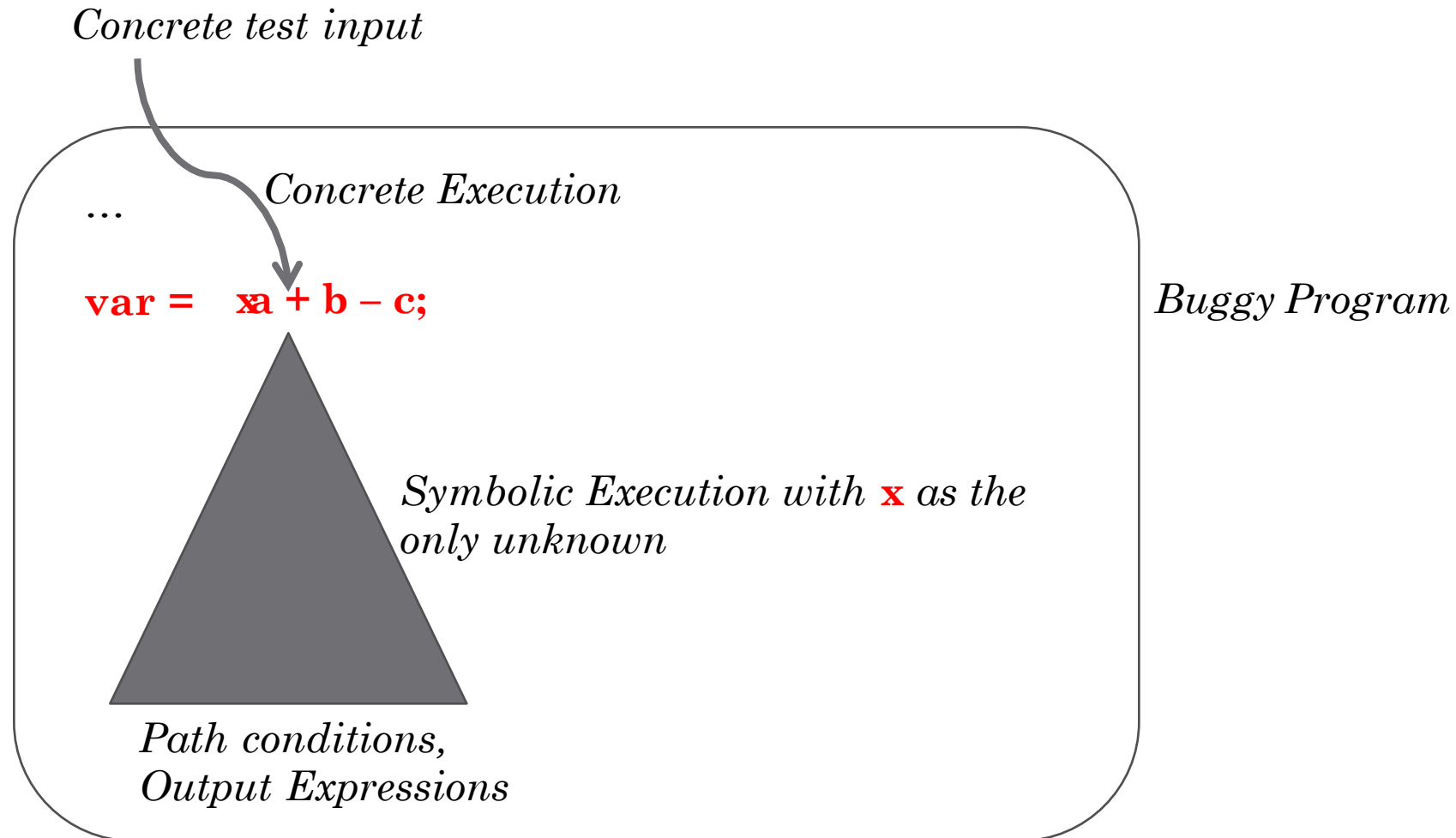
$P(1) \longrightarrow 1$

Failing test

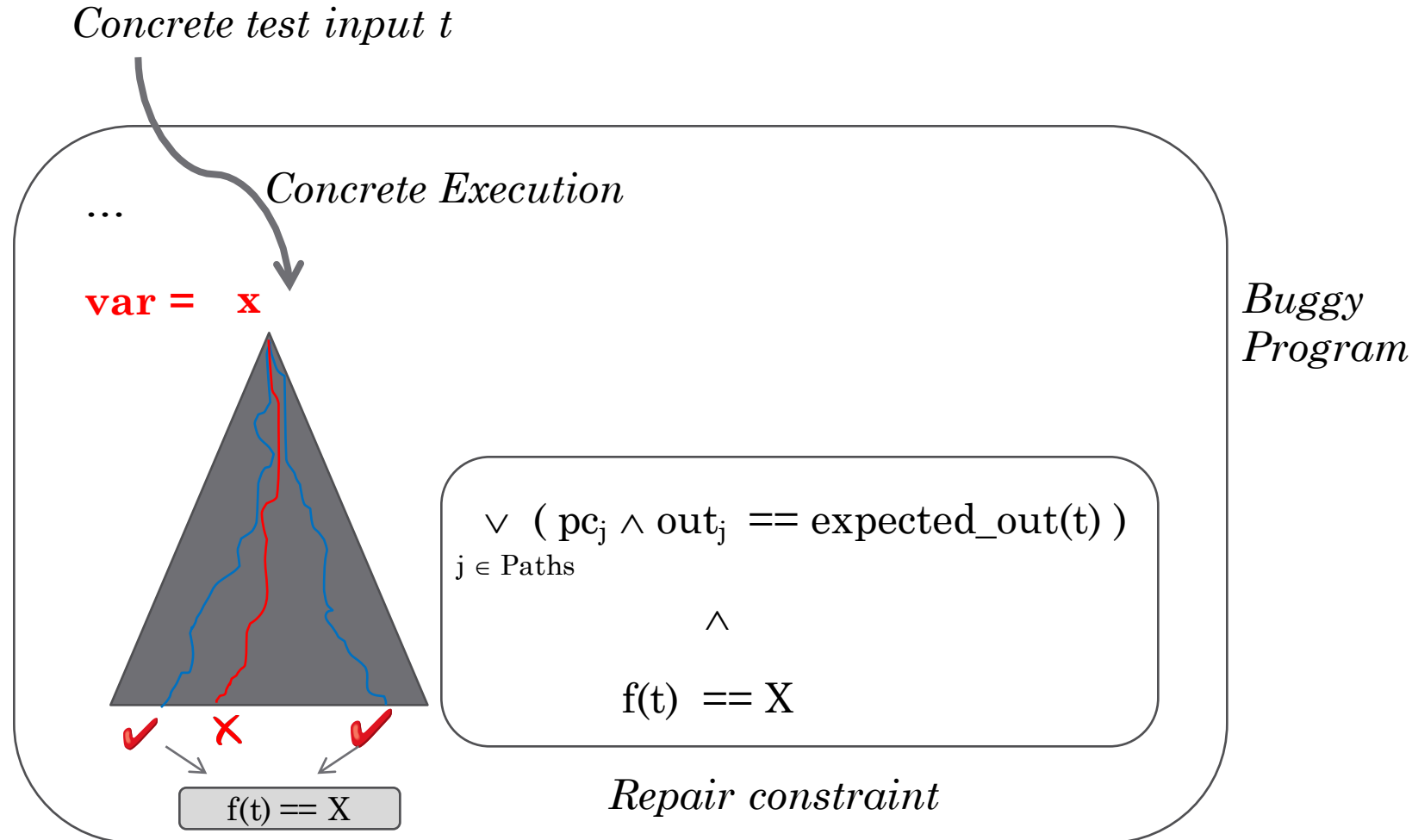
Specification Inference



What it should have been



What it should have been



Example

```

1  int is_upward( int inhibit, int up_sep, int down_sep){
2      int bias;
3      if (inhibit)
4          bias = down_sep; //  bias= up_sep + 100
5      else bias = up_sep ;
6      if (bias > down_sep)
7          return 1;
8      else return 0;
9  }

```

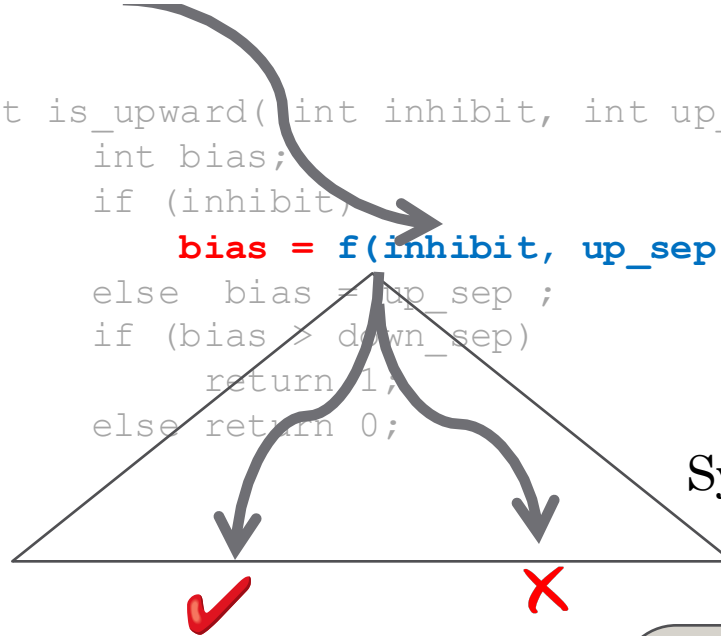
inhibit	up_sep	down_sep	Observed output	Expected Output	Result
1	0	100	0	0	pass
1	11	110	0	1	fail
0	100	50	1	1	pass
1	-20	60	0	1	fail
0	0	10	0	0	pass

Example

Inhibit == 1	up_sep == 11	down_sep == 110
--------------	--------------	-----------------

```

1  int is_upward(int inhibit, int up_sep, int down_sep){
2      int bias;
3      if (inhibit)
4          bias = f(inhibit, up_sep, down_sep) // X
5      else bias = up_sep ;
6      if (bias > down_sep)
7          return 1;
8      else return 0;
9  }
```



Symbolic Execution

$$\begin{aligned}
 & ((X > 110 \wedge 1 == 1) \\
 & \vee (X \leq 110 \wedge 0 == 1)) \\
 & \wedge \\
 & f(1, 11, 110) == X
 \end{aligned}$$

$$\begin{aligned}
 & \vee (pc_j \wedge out_j == expected_out(t)) \\
 & j \in Paths \\
 & \wedge \\
 & f(t) == X
 \end{aligned}$$

Repair constraint

What it should have been

Inhibit == 1	up_sep == 11	down_sep == 110
-----------------	-----------------	--------------------

```

1 int is_upward( int inhibit, int up_sep, int
  down_sep){
2     int bias;
3     if (inhibit)
4         bias = f(inhibit, up_sep, down_sep)
5     else bias = up_sep ;
6     if (bias > down_sep)
7         return 1;
8     else return 0;
9 }

```

Symbolic Execution

$f(1, 11, 110) > 110$



Fix the suspect

- Accumulated constraints
 - $f(1,11, 110) > 110 \wedge$
 - $f(1,0,100) \leq 100 \wedge$
 - ...
- Find a f satisfying this constraint
 - By fixing the set of operators appearing in f
- Candidate methods
 - Search over the space of expressions
 - Program synthesis with fixed set of operators
 - **More efficient!!**
- Generated fix
 - `f(inhibit, up_sep, down_sep) = up_sep + 100`



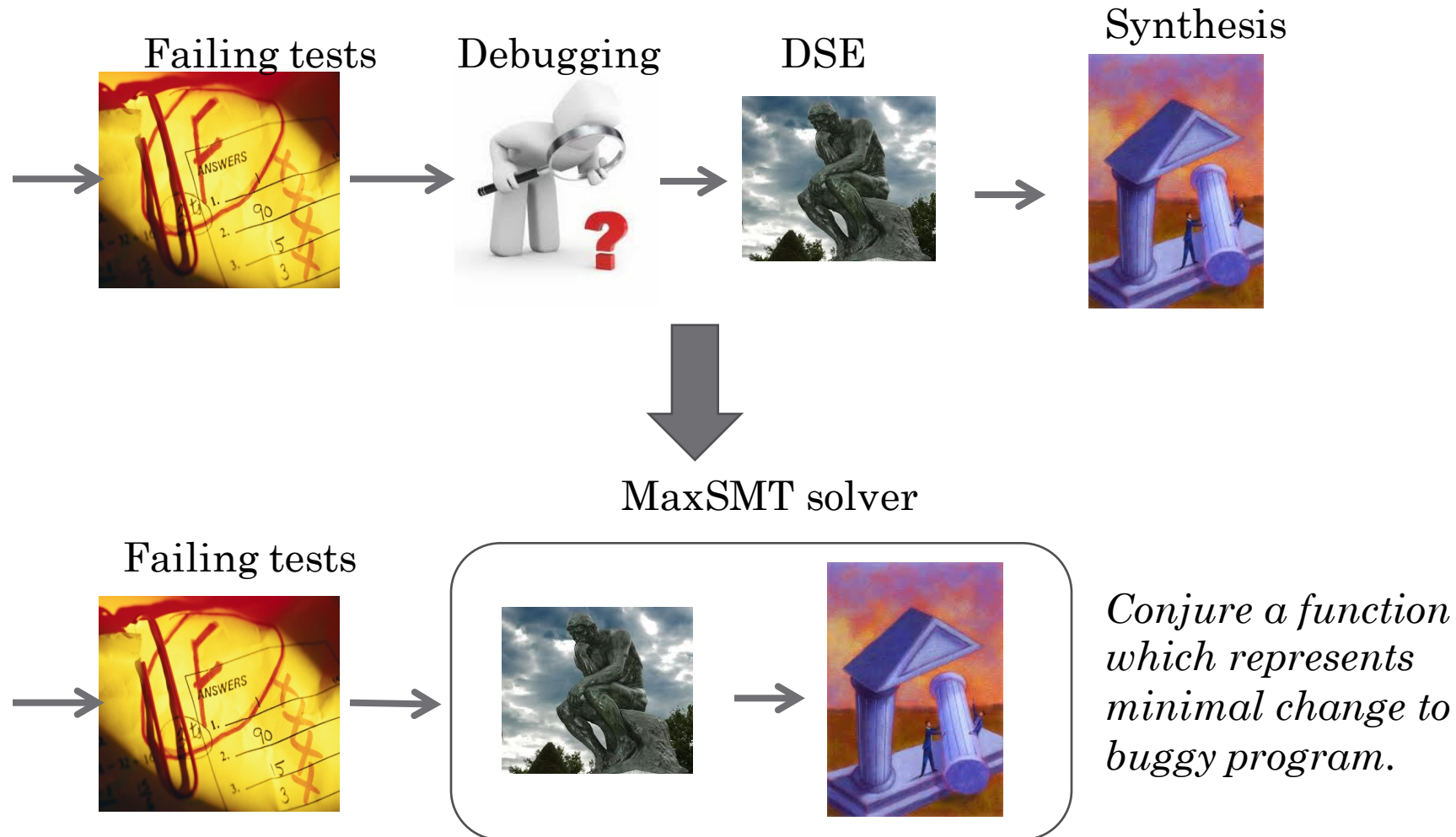
Function synthesis

- Instead of solving

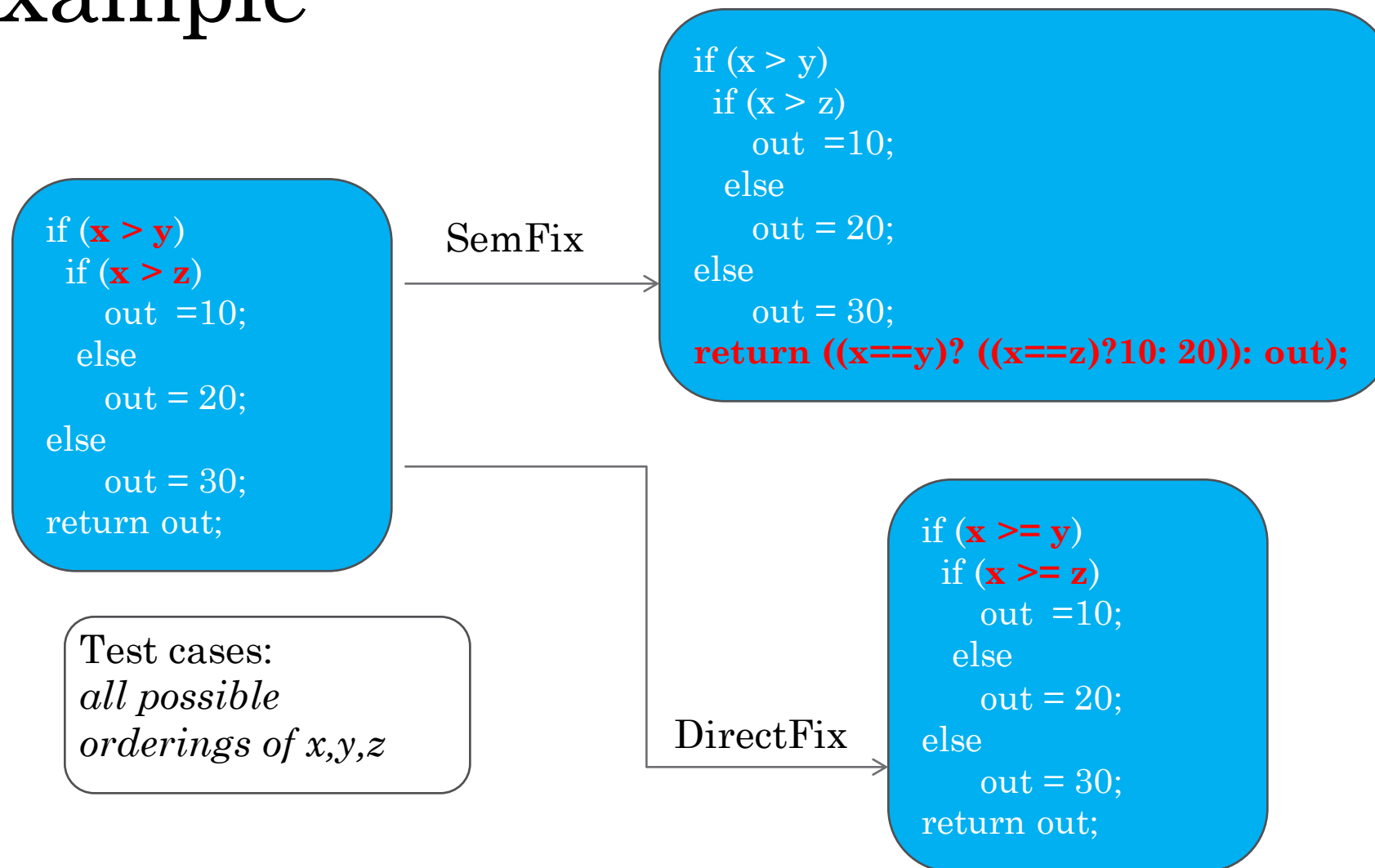
$$\begin{aligned} \text{Repair Constraint:} \\ f(1,11,110) > 110 \wedge f(1,0,100) \leq 100 \\ \wedge f(1,-20,60) > 60 \end{aligned}$$

- Select primitive components to be used by the synthesized program based on complexity
- **Look** for a program that uses only these primitive components and satisfy the repair constraint
 - Done via another constraint solving problem – pgm. synthesis
- **Solving the repair constraint is the key, not how it is solved**
- Enumerate expressions over a given set of components / operators
 - Enforce axioms of the operators
 - If candidate repair contains a constant, solve using SMT

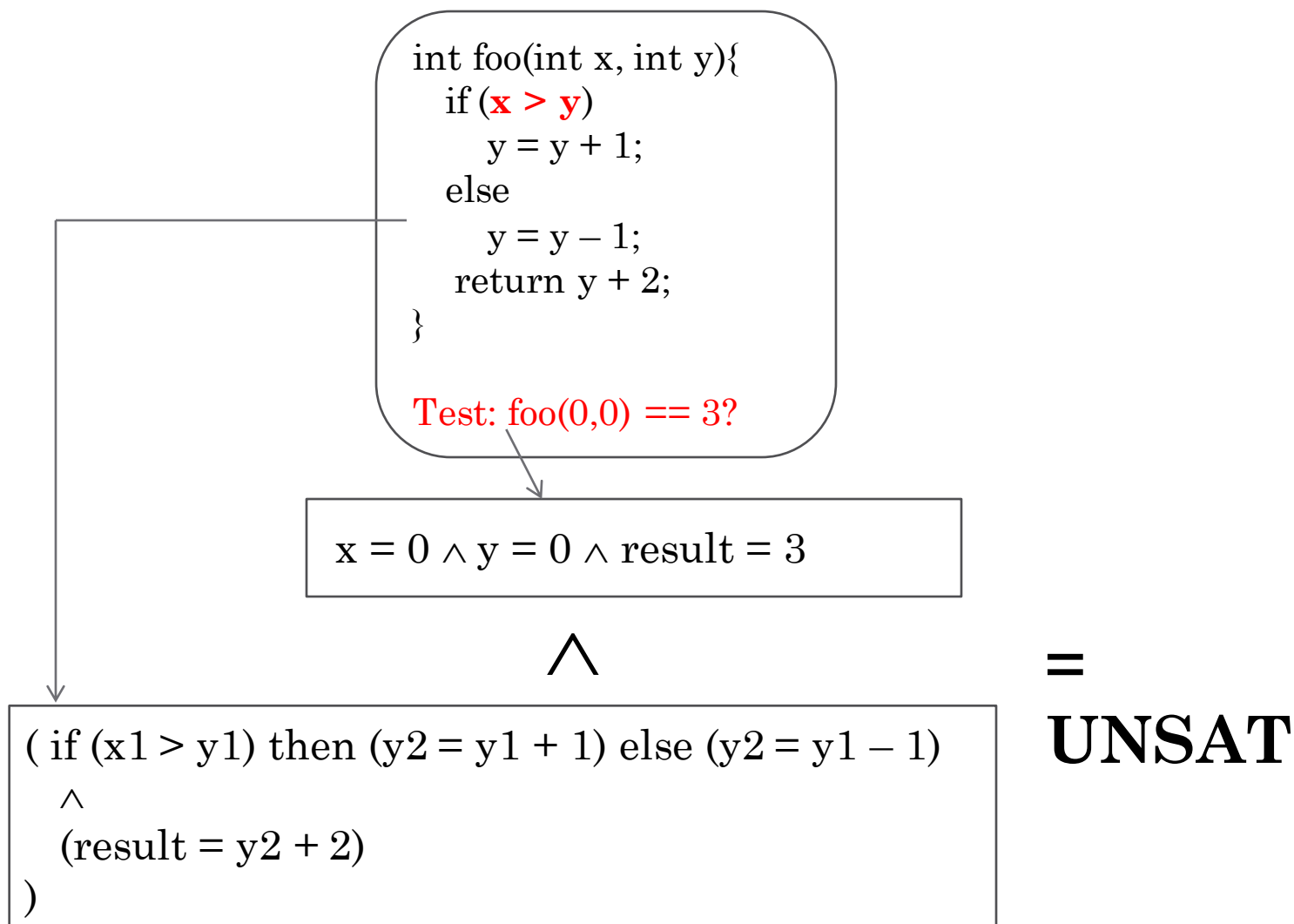
Patch as minimal change



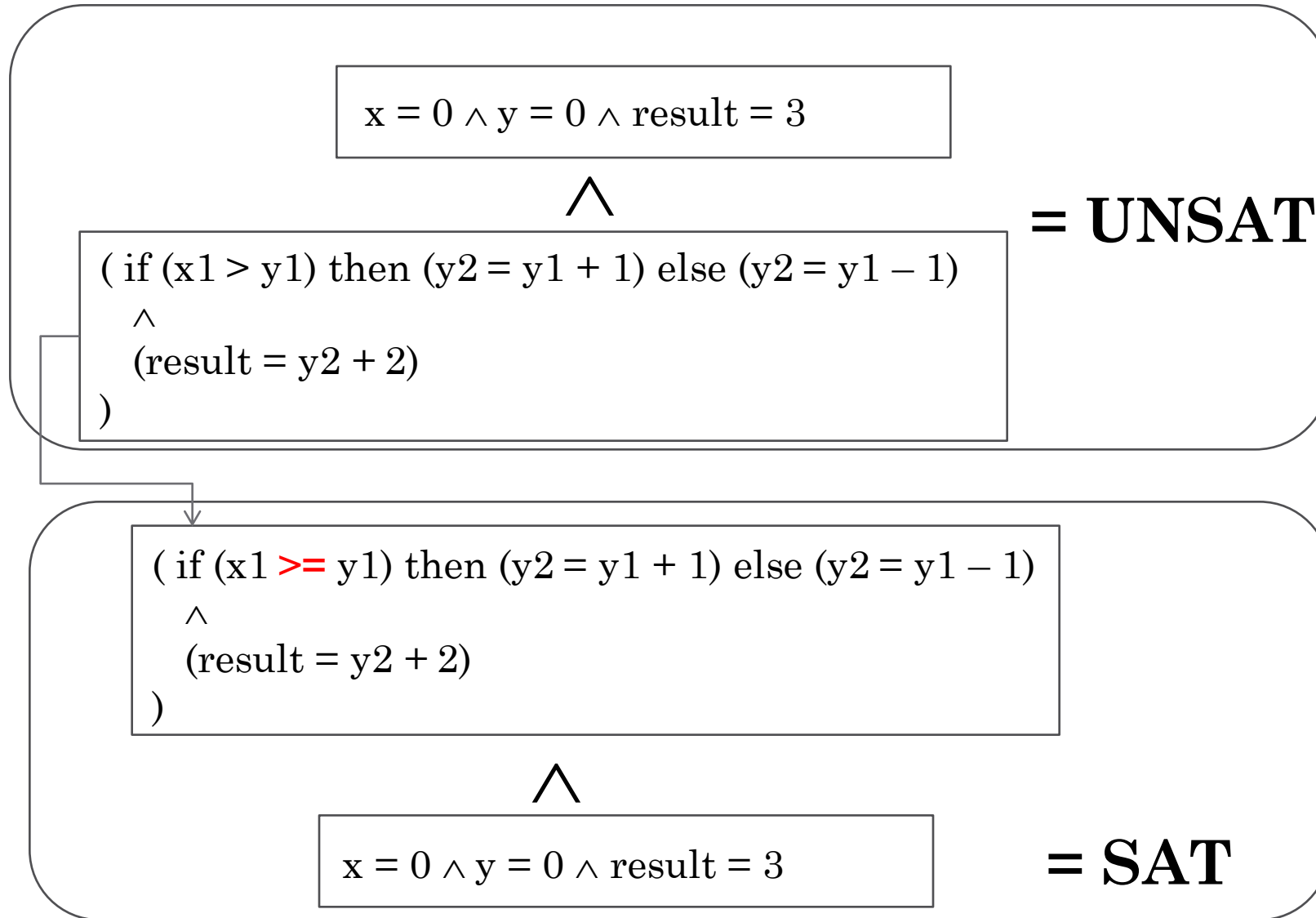
Example



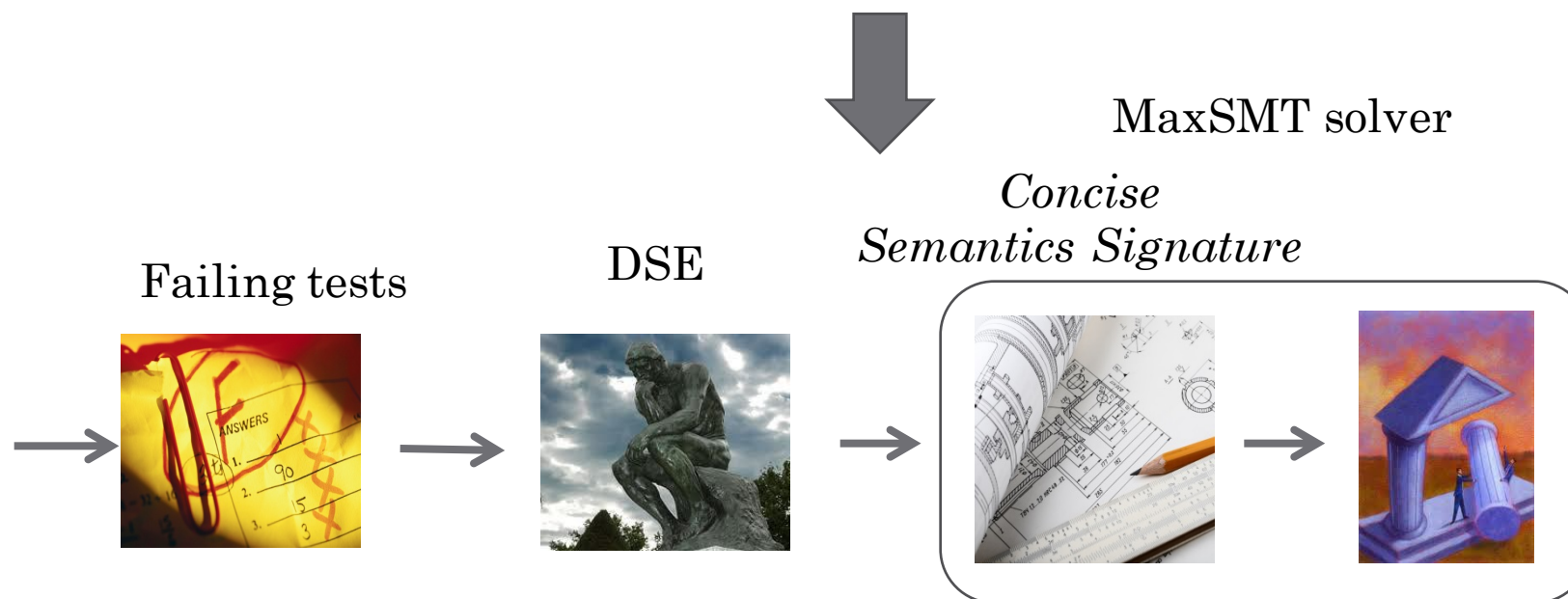
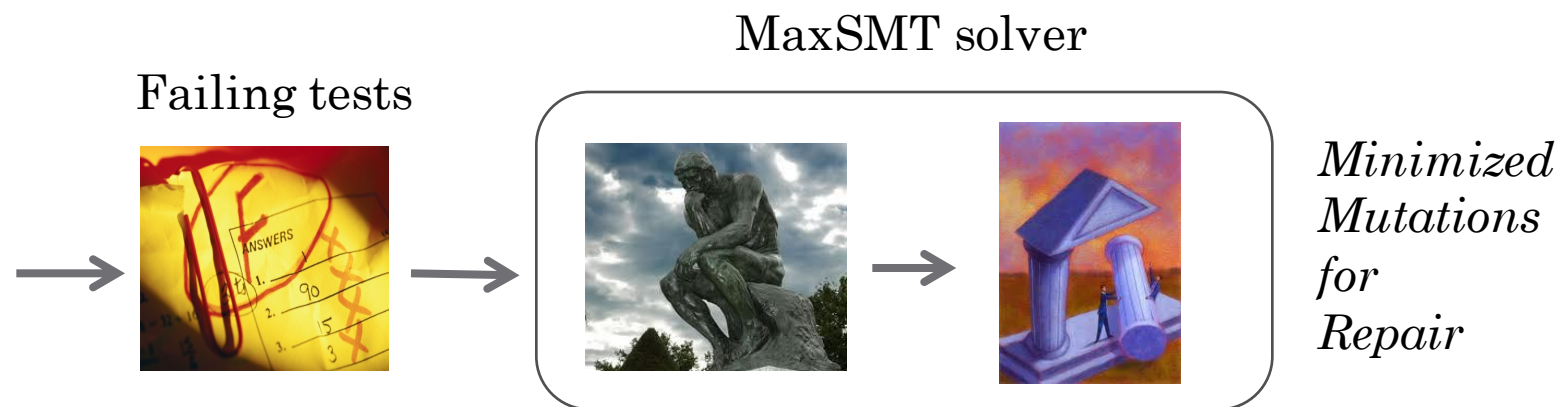
No fault localization



Constraint = Whole Program



Need Concise Constraints



Angelic Values

Syntax-based Schematic

```
for e in SearchSpace{
  Validate e against Tests
}
```

Semantics-based Schematic

```
for t in Tests {
  generate repair constraint  $\Psi_t$ 
}
Synthesize e from  $\bigwedge_t \Psi_t$ 
```

Instead of representing Ψ_t
as a SMT constraint represent it using **values**.

Value that is arbitrarily set during execution to a selected expression and that makes the program pass.
Can be found by solving path condition of failing test case (I, O) :

$$\text{pathcondition}[\alpha] \wedge \text{input} = I \wedge \text{output} = O$$

Angelic Values

Buggy program

```
scanf ("%d", &x) ;
int t =  $\alpha$  ;
if ( $\beta$ ) printf ("1") ;
else printf ("0") ;
```

Test

$P(1) \longrightarrow 1$

Extract value based specification

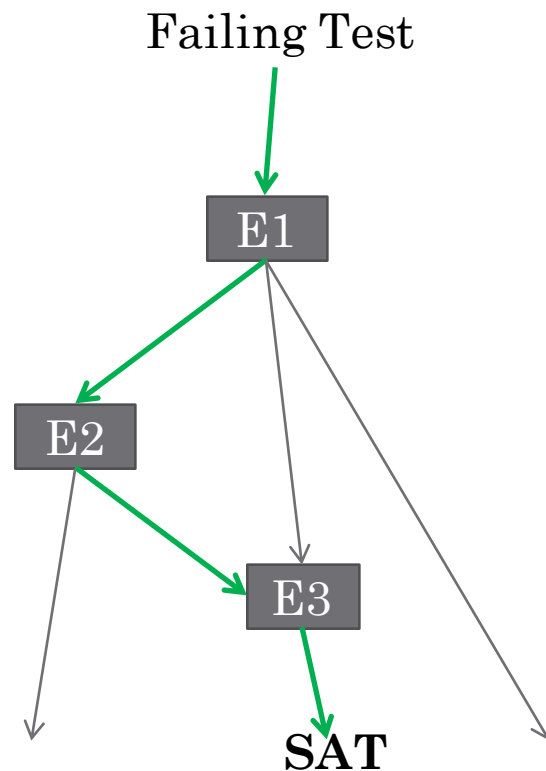
$\langle \alpha = 2, \sigma = \{x \rightarrow 1\} \rangle$

$\langle \beta = \text{true}, \sigma = \{x \rightarrow 1, t \rightarrow 2\} \rangle$

Angelic forest: Patch synthesis specification based on

Angelic values $\{ \langle \text{Symbolic Variable name, Constant, State} \rangle \}_{Paths, Tests}$

Angelic Forest



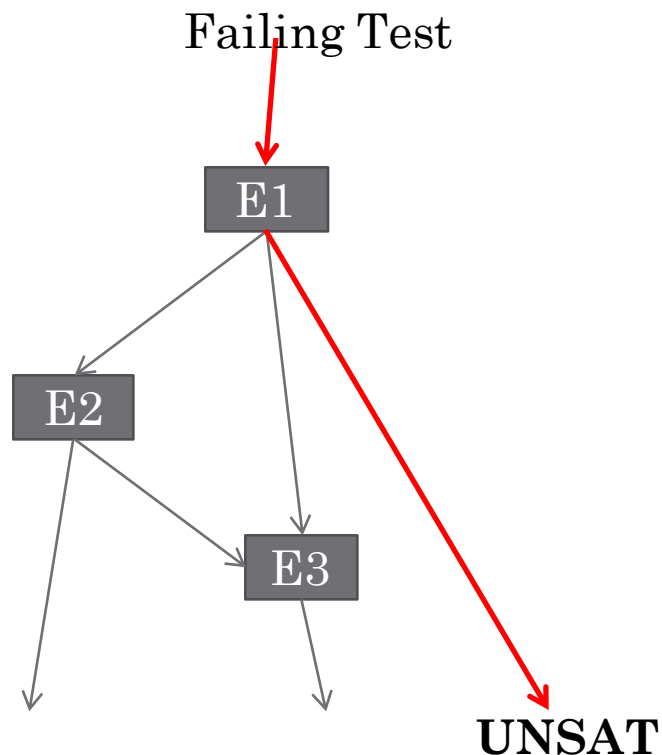
Angelic Paths



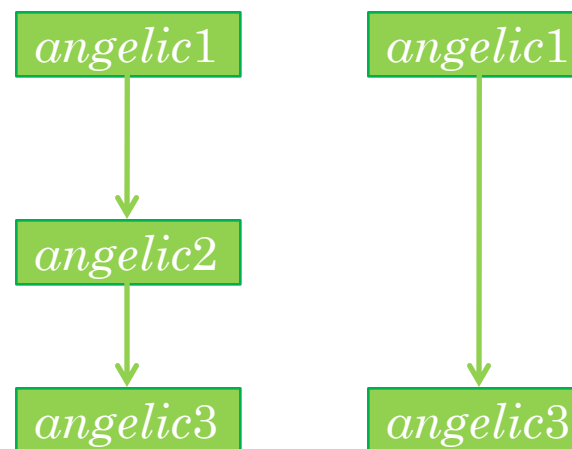
Angelic forest: Patch synthesis specification based on

Angelic values $\{\langle \text{Symbolic Variable name, Constant, State} \rangle\}_{Paths, Tests}$

Angelic Forest



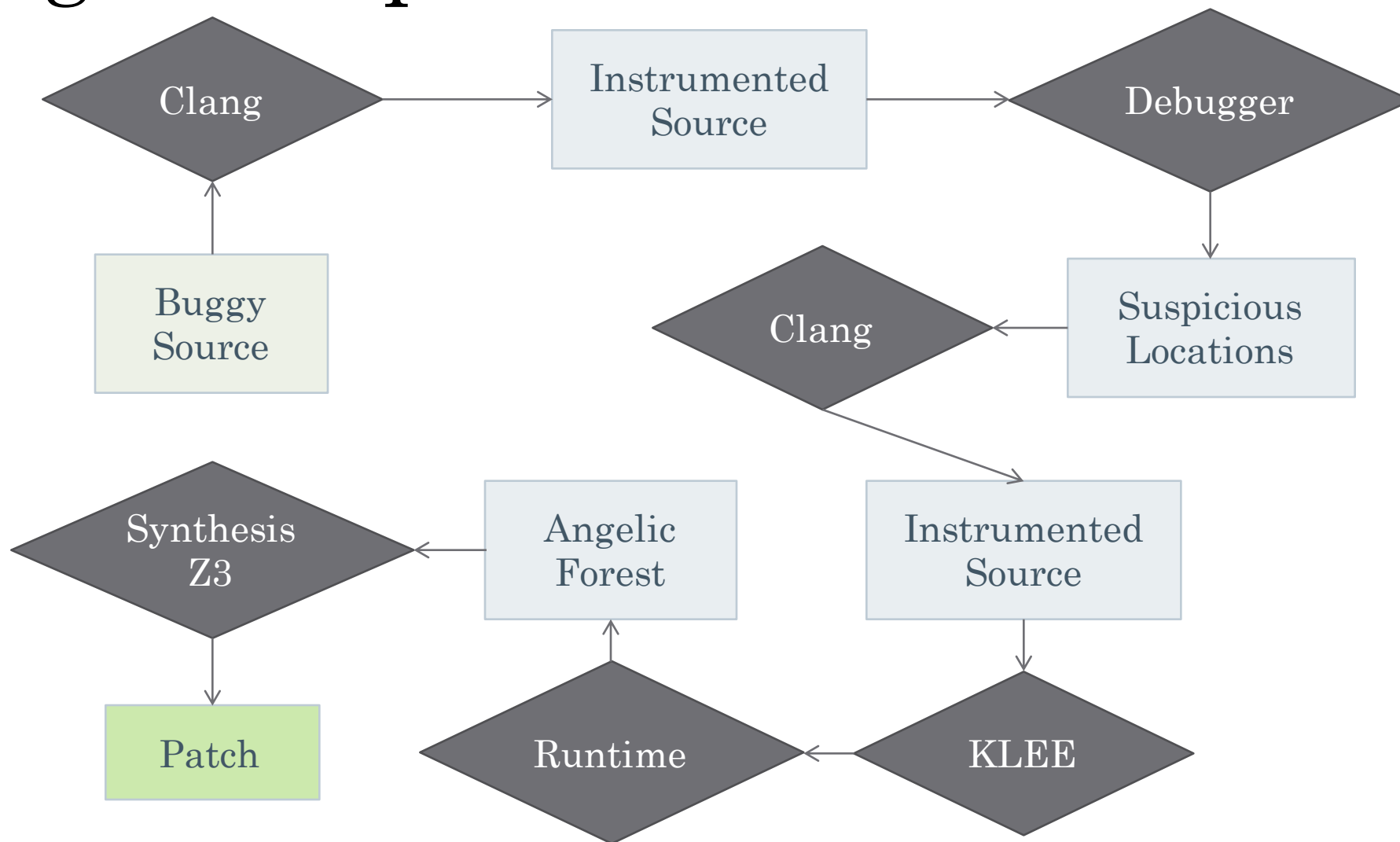
Angelic Paths



Angelic forest: Patch synthesis specification based on

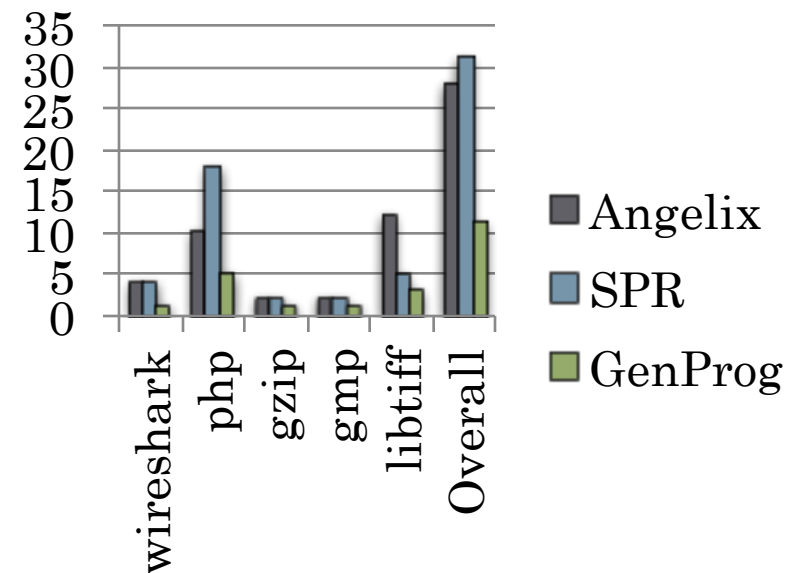
Angelic values $\{\langle \text{Symbolic Variable name, Constant, State} \rangle\}_{Paths, Tests}$

Angelix Implementation



Results

Subject	LoC
wireshark	2814K
php	1046K
gzip	491K
gmp	145K
libtiff	77K



	#Fixes	Del	Del, Per
Angelix	28	5	18%
SPR	31	13	42%

Multiline Results

Defect	Fixed Expressions
Libtiff-4a24508-cc79c2b	2
Libtiff-829d8c4-036d7bb	2
CoreUtils-00743a1f-ec48bead	3
CoreUtils-1dd8a331-d461bfd2	2
CoreUtils-c5ccf29b-a04ddb8d	3

The Heartbleed Bug is a serious vulnerability in the popular OpenSSL cryptographic software library. This weakness allows stealing the information protected, under normal conditions, by the SSL/TLS encryption used to secure the Internet. SSL/TLS provides communication security and privacy over the Internet for applications such as web, email, instant messaging (IM) and some virtual private networks (VPNs).

--- Source: *heartbleed.com*

```

1  if ( hbtype == TLS1 HB REQUEST) {
2      ...
3      memcpy (bp , pl , payload );
4      ...
5  }
```

(a) The buggy part of the Heartbleed-vulnerable OpenSSL

```

1  if ( hbtype == TLS1 HB REQUEST
2      && payload + 18 < s->s3->rrec.length) {
3      ...
4  }
```

(b) A fix generated automatically



```

1  if (1 + 2 + payload + 16 > s->s3->rrec.length)
2      return 0;
3  ...
4  if ( hbtype == TLS1_HB_REQUEST) {
5      ...
6  }
7  else if ( hbtype == TLS1_HB_RESPONSE) {
8      ...
9  }
10 return 0;
```

(c) The developer-provided repair




Research Issues in Program Repair

- [OLD] *Large search space* of candidate patches for general-purpose repair tools.
- -> *What should I use?*
- -> *Which search frameworks could we use?*
- -> *Syntactic Program Repair*
- [NEW] Weak description of intended behavior / *correctness criterion* e.g. tests
- -> *Overfitting of a patch candidate to tests?*
- -> *Extract specification from test executions to reduce overfitting.*
- -> *Do so, while still navigating the search space*
- -> *Semantic Program Repair*

Spec. from reference implementation

User-define condition: $\text{length} = 3 \ \& \ a[0] < a[1] < a[2]$




```

1 int search(int x, int a[], int length) {
2   int i;
3   for (i=0; i<length; i++) {
4     if (x == a[i])
5       return i;
6   }
7   return -1;
8 }

```

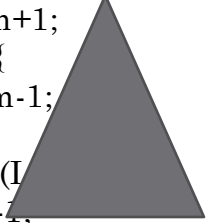
(a) Correct linear search



```

1 int search(int x, int a[], int length) {
2   int L = 0;
3   int R = length-1;
4   do {
5     int m = (L+R)/2;
6     if (x == a[m]) {
7       return m;
8     } else if (x < a[m]) { // bug fix: x > a[m]
9       L = m+1;
10    } else {
11      R = m-1;
12    }
13  } while (L < R);
14  return -1;
15 }

```



(b) Buggy binary search

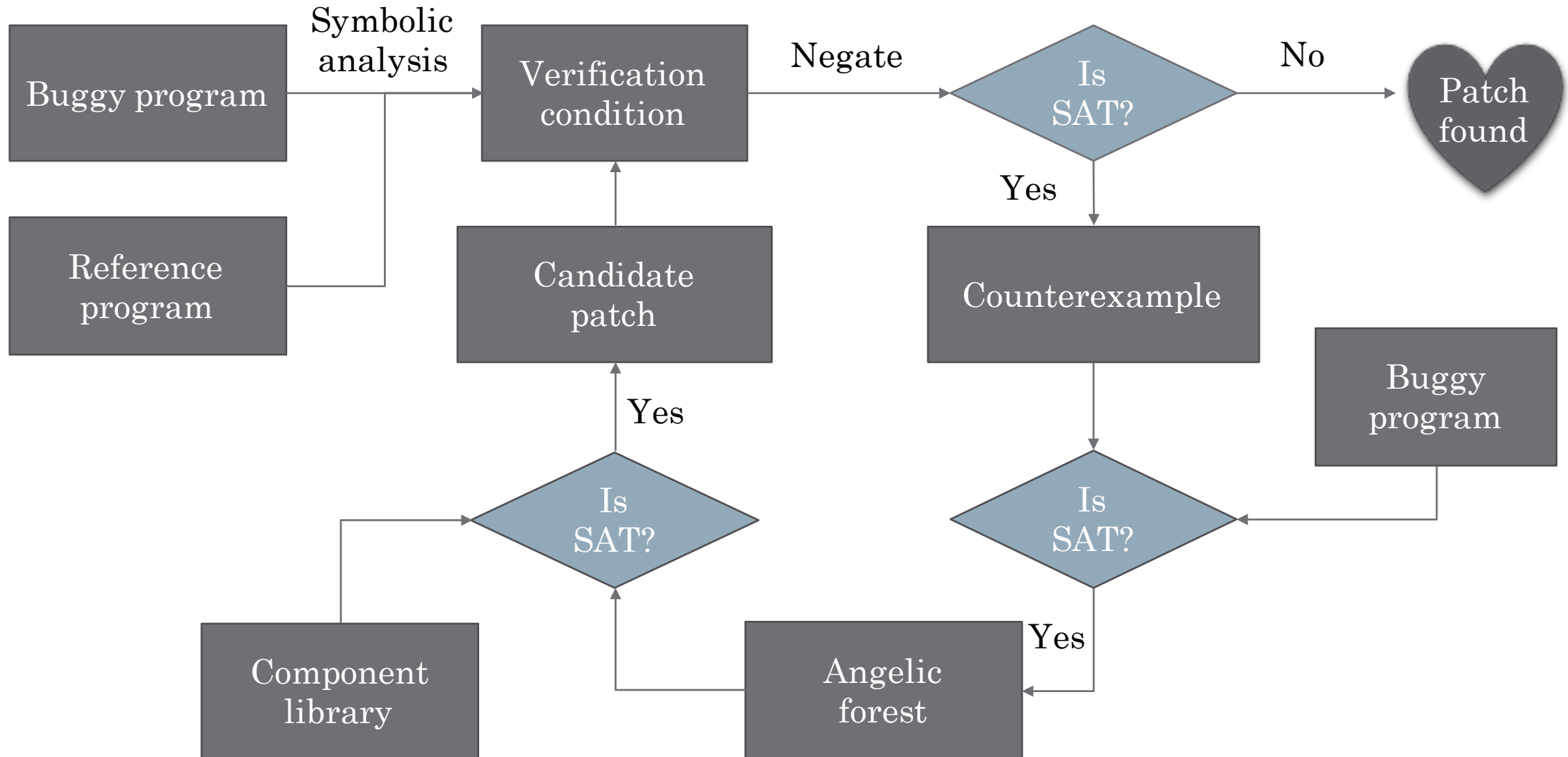


Verification condition



Experiments on embedded Linux Busybox

SemGraft



SemGraft Results

**GNU Coreutils
as reference**

Program	Commit	Bug	Angelix	SemGraft
sed	c35545a	Handle empty match	Correct	Correct
seq	f7d1c59	Wrong output	Correct	Correct
sed	7666fa1	Wrong output	Incorrect	Correct
sort	d1ed3e6	Wrong output	Incorrect	Correct
seq	d86d20b	Don't accepts 0	Incorrect	Correct
sed	3a9365e	Handle s///	Incorrect	Correct

**Linux Busybox
as reference**

Program	Commit	Bug	Angelix	SemGraft
mkdir	f7d1c59	Segmentation fault	Incorrect	Correct
mkfifo	cdb1682	Segmentation fault	Incorrect	Correct
mknod	cdb1682	Segmentation fault	Incorrect	Correct
copy	f3653f0	Failed to copy a file	Correct	Correct
md5sum	739cf4e	Segmentation fault	Correct	Correct
cut	6f374d7	Wrong output	Incorrect	Correct

GNU Coreutils Cut

GNU Coreutils wrongly interprets the command `-b 2-,3-` as `-b 3-` (extract input bytes starting from the third byte):

```
echo -ne '1234 ' | cut -b 2-,3-  
34
```

instead of `-b 2-` (extract input bytes starting from the second byte):

```
echo -ne '1234 ' | cut -b 2-,3-  
234
```

Developer tests:

```
echo -ne '1234 ' | cut -b 2-,3-  
echo -ne '1234 ' | cut -b 3-,2-
```

GNU Coreutils cut

Automatic patch based on developer tests

```
if (! rhs_specified ){  
    if ( eol_range_start == 0 || eol_range_start == 3 )  
        eol_range_start = initial ;  
    field_found = true ;  
}
```

Developer patch

```
if (! rhs_specified ){  
    if ( eol_range_start == 0 || initial < eol_range_start )  
        eol_range_start = initial ;  
    field_found = true ;  
}
```

Parameterized test to improve automated repair and apply SemGraft

```
echo -ne '1234 ' | cut -b  $\sigma^-$ ,  $\beta^-$ 
```

Recap: Comparison

Syntactic Program Repair

Syntax-based Schematic
 for e in **Search-space**{
 Validate e against Tests
}

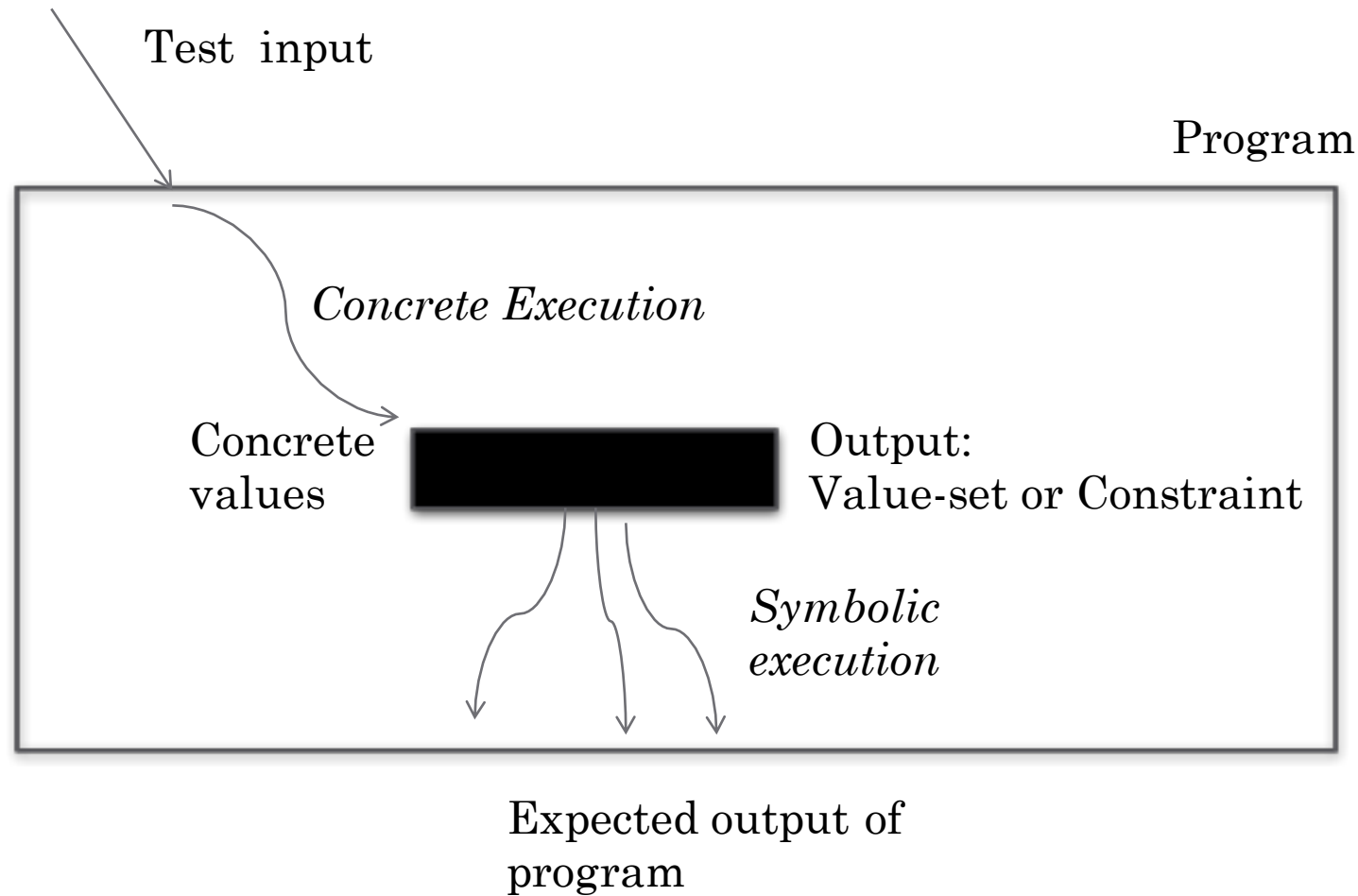
1. Where to fix, which line?
2. Generate patches in the candidate line
3. Validate the candidate patches against correctness criterion.

Semantic Program Repair

Semantics-based Schematic
 for t in **Tests** {
 generate repair constraint Ψ_t
}
Synthesize e from $\bigwedge_t \Psi_t$

1. Where to fix, which line(s)?
2. What values should be returned by those lines, e.g. `<inp == 1, ret == 0>`
3. What are the expressions which will return such values?

Specification Inference



Revisiting Program Synthesis

From input-output examples

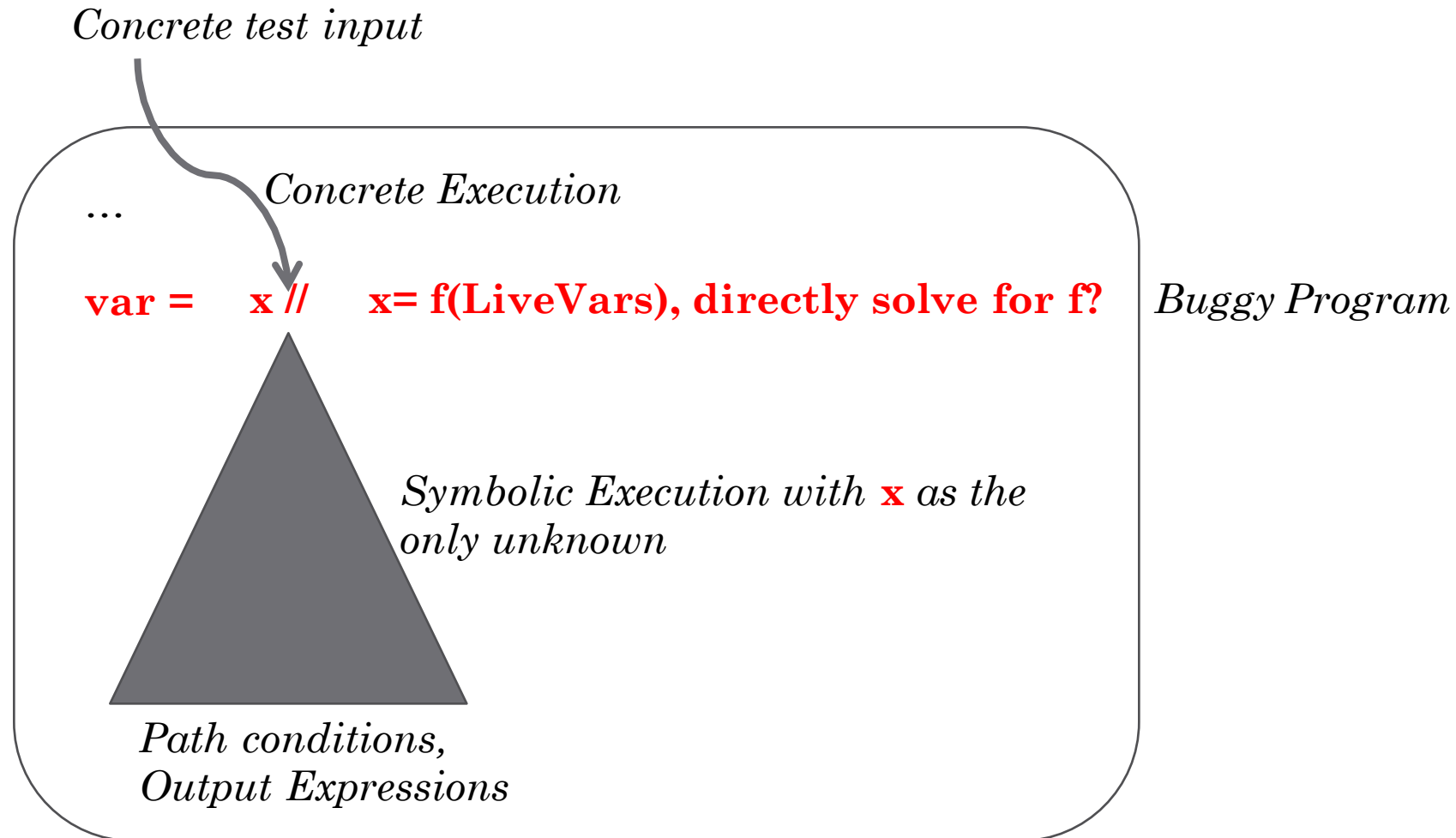
$$\exists p \in P. \bigwedge_{(\sigma, o) \in T} \llbracket p \rrbracket_{\sigma} = o$$

where P is a set of well-formed programs to choose from (candidate patches)

T is a given set of tests

Program Repair involves solving for such program fragments from input-output examples or input-output constraints, amounting to second order reasoning.

Repair via 2nd order reasoning



First order Symbolic Execution

```
size_t search (data , len , pred ) {  
    size_t i;  
    for (i = 0; i < len; i++){  
        if ( pred ( data [i])) return i;  
    }  
    return len;  
}  
int positive (int x) { return x > 0; }
```

Symbolic Inputs α, β, γ

```
search((int[]){ $\alpha, \beta, \gamma$ }, 3, positive)
```

First order Symbolic Execution

```

size_t search (data , len , pred ) {
    size_t i;
    for (i = 0; i < len; i++){
        if ( pred ( data [i])) return i;
    }
    return len;
}

int positive (int x) { return x > 0; }

```

Symbolic Execution results of `search((int[]) { α , β , γ }, 3, positive)`

Path Condition	Input	Output
$\alpha > 0$	{1,0,0}	0
$\alpha \leq 0 \wedge \beta > 0$	{0,1,0}	1
$\alpha \leq 0 \wedge \beta \leq 0$	{0,0,1}	2
$\alpha \leq 0 \wedge \beta \leq 0 \wedge \gamma \leq 0$	{0,0,0}	3

(Our) Second order reasoning

- Allow for existentially quantified second order variables.
- Restrict their interpretation to a language e.g. linear integer arithmetic

*Term = Var | Constant | Term + Term | Term - Term | Constant * Term*

- **SAT**
 - $\rho(0) > 0 \wedge \rho(1) \leq 0$
 - Satisfying solution $\rho = \lambda x. 1 - x$
- **UNSAT**
 - $\rho(0) > 0 \wedge \rho(1) \leq 0 \wedge \rho(2) > 0$
 - All functions in LIA are monotonic.

Second order Symbolic Execution

```

size_t search (data , len , pred ) {
    size_t i;
    for (i = 0; i < len; i++){
        if ( pred ( data [i])) return i;
    }
    return len;
}

```

Symbolic Execution results of `search((int[]) {0,1,2}, 3, ρ)`

Path Condition	ρ	Output
$\rho(0)$	$\lambda x. true$	0
$\neg \rho(0) \wedge \rho(1)$	$\lambda x. x > 0$	1
$\neg \rho(0) \wedge \neg \rho(1) \wedge \rho(2)$	$\lambda x. x > 1$	2
$\neg \rho(0) \wedge \neg \rho(1) \wedge \neg \rho(2)$	$\lambda x. false$	3

Syntactic Program Repair

Buggy Program:

```
scanf("%d", &x);  
for(i = 0; i < 10; i++){  
    int t = x - i;  
    if (t > 0) printf("1");  
    else printf("0");  
}
```

Sample Test:

$P(5) \rightarrow$ "1110000000" expected "1111111000"

Generate and validate based repair tools:

Enumerate and test $P[x - i \rightarrow x + i]$, $P[x - i \rightarrow x - 1]$, ...

First order Semantic Program Repair

Buggy Program:

```
scanf("%d", &x);  
for(i = 0; i < 10; i++){  
    int t =  $\alpha$ ;  
    if (t > 0) printf("1");  
    else printf("0");  
}
```

Sample Test:

$P(5) \rightarrow$ "1110000000" expected "1111111000"

Synthesis Specification:

$\exists e \in \text{Term}. \bigvee_i \pi_i [\alpha \rightarrow e] \wedge \text{output} = \text{expected}$

Background theory LIA

Second order Program Repair

Buggy Program:

```
scanf("%d", &x);
for(i = 0; i < 10; i++) {
    int t =  $\rho(i, x)$ ;
    if (t > 0) printf("1");
    else printf("0");
}
```

Sample Test:

$P(5) \rightarrow$ "1110000000" expected "1111111000"

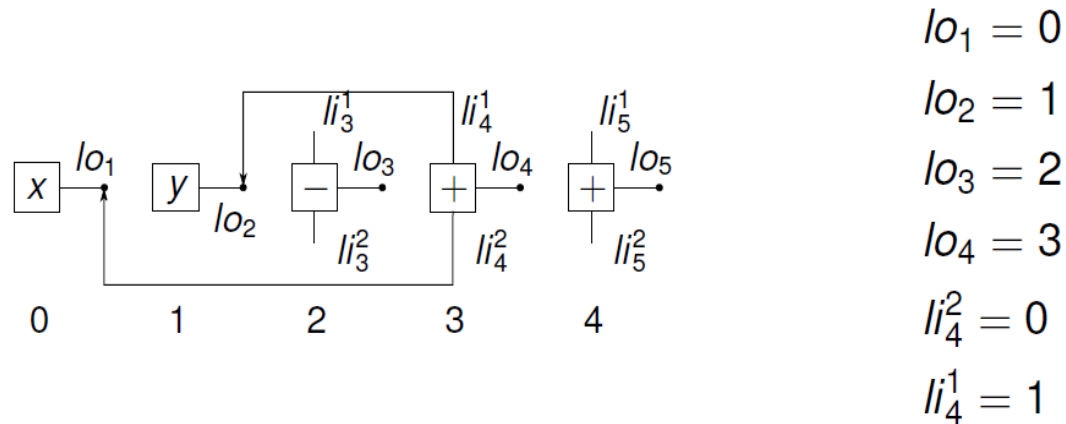
Synthesis Specification:

$$\exists \rho. \bigvee_i \pi_i \wedge \text{output} = \text{expected}$$

Solve for ρ directly

Term = *Var* | *Constant* | *Term* + *Term* |
Term − *Term* | *Constant* * *Term*

(Old)Encoding for synthesis in 1st order



$$\phi_{range} := \bigwedge_{i \in [1, C]} \left(0 \leq lo_i < C \wedge \bigwedge_{j \in [1, N_i]} 0 \leq li_j^i < C \right)$$

$$\phi_{cons} := \bigwedge_{i, j \in [1, C], i \neq j} lo_i \neq lo_j$$

$$\phi_{acyc} := \bigwedge_{i \in [1, C], j \in [1, N_i]} lo_i > li_j^i$$

$$\phi_{conn} := \bigwedge_{i, j \in [1, C], k \in [1..N_i]} lo_i = li_j^k \Rightarrow out_i = in_j^k$$

(Recap) Second order reasoning

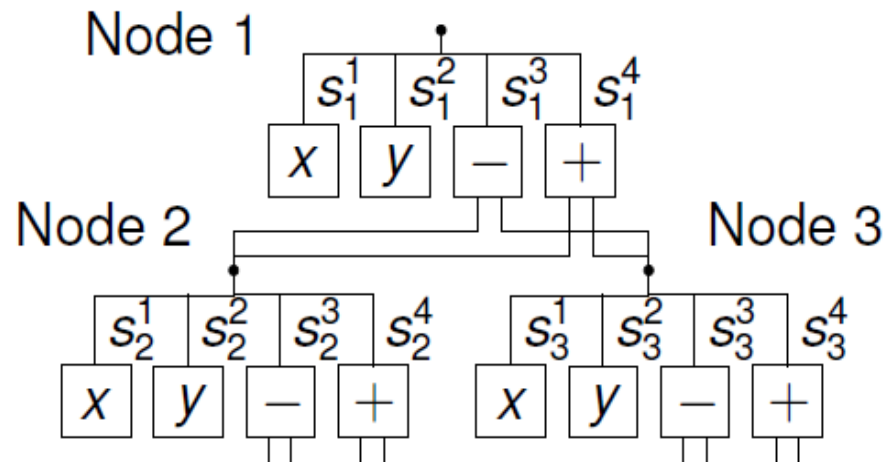
- Allow for existentially quantified second order variables.
- Restrict their interpretation to a language e.g. linear integer arithmetic

$Term = Var \mid Constant \mid Term + Term \mid Term - Term \mid Constant * Term$

- *Example SAT*
 - $\rho(0) > 0 \wedge \rho(1) \leq 0$
 - Satisfying solution $\rho = \lambda x. 1 - x$

Devise a propositional encoding to capture the set of interpretations

(New) Propositional Logic encoding



$$s_1^1 \mapsto x$$

$$s_1^3 \wedge s_2^1 \wedge s_3^2 \mapsto x - y$$

$$s_1^4 \wedge s_2^1 \mapsto \{x + T\}_{T \in \text{Term}}$$

$$\psi_{\text{node}} := \bigwedge_{j \in [1, C]} s_i^j \Rightarrow \text{out}_i = F_j(\text{out}_{i_1}, \text{out}_{i_2}, \dots, \text{out}_{i_k})$$

$$\psi_{\text{choice}} := \text{exactlyOne}(s_i^1, s_i^2, \dots, s_i^C)$$

Application in Repair: results

```
... error_severity(1);
    return;
}
//  $\rho(\text{ent} \rightarrow \text{fts\_info}, \text{ent} \rightarrow \text{fts\_errno}, \text{prev\_depth})$ 
else if (ent->fts_info == FTSSLNONE) {
    if (symlink_loop(ent->fts_accpath))
...

```

find in GNU Coreutils

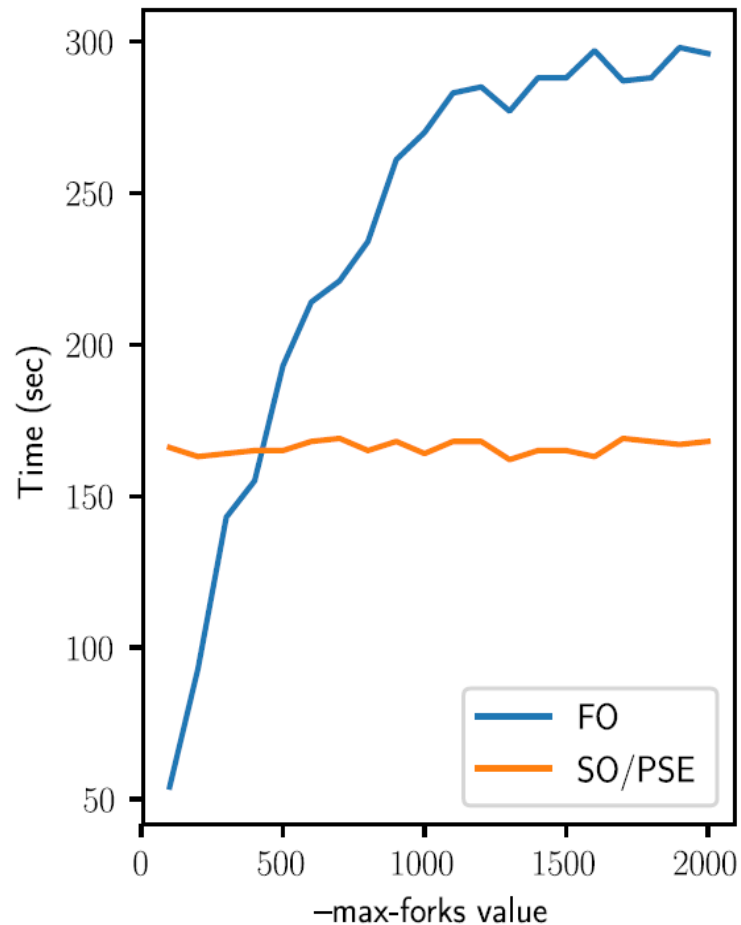
2000 paths in traditional first
order Symbolic Execution

```

 $\rho_1 := (4 \leq \text{ent} \rightarrow \text{fts\_info})$ 
 $\rho_2 := !(\text{ent} \rightarrow \text{fts\_errno} == \text{prev\_depth})$ 
 $\rho_3 := ((4 < \text{ent} \rightarrow \text{fts\_info}) \ \&\& \ (\text{prev\_depth} \leq \text{ent} \rightarrow \text{fts\_errno}))$ 
 $\rho_4 := !(0 == \text{ent} \rightarrow \text{fts\_errno})$ 
 $\rho_5 := ((\text{ent} \rightarrow \text{fts\_info} == \text{ent} \rightarrow \text{fts\_errno}) \ || \ (9 \leq \text{prev\_depth}))$ 
 $\rho_6 := (\text{ent} \rightarrow \text{fts\_info} == (7 + \text{prev\_depth}))$ 
 $\rho_7 := ((\text{prev\_depth} + \text{ent} \rightarrow \text{fts\_errno}) == (\text{ent} \rightarrow \text{fts\_info} - 6))$ 
 $\rho_8 := ((\text{ent} \rightarrow \text{fts\_info} < \text{prev\_depth}) \ || \ (6 == \text{ent} \rightarrow \text{fts\_info}))$ 
 $\rho_9 := (\text{ent} \rightarrow \text{fts\_info} < (4 + \text{ent} \rightarrow \text{fts\_errno}))$ 
 $\rho_{10} := (\text{ent} \rightarrow \text{fts\_info} \leq (\text{ent} \rightarrow \text{fts\_errno} + 6))$ 
 $\rho_{11} := !(\text{ent} \rightarrow \text{fts\_info} == 6)$ 
 $\rho_{12} := (0 \leq \text{prev\_depth})$ 
 $\rho_{13} := !(4 < \text{ent} \rightarrow \text{fts\_info})$ 
 $\rho_{14} := !(1 \leq \text{prev\_depth})$ 
 $\rho_{15} := ((\text{ent} \rightarrow \text{fts\_errno} < \text{prev\_depth}) \ || \ (\text{ent} \rightarrow \text{fts\_info} \leq 1))$ 
 $\rho_{16} := ((\text{ent} \rightarrow \text{fts\_errno} < 32) \ || \ (\text{prev\_depth} == \text{ent} \rightarrow \text{fts\_info}))$ 

```

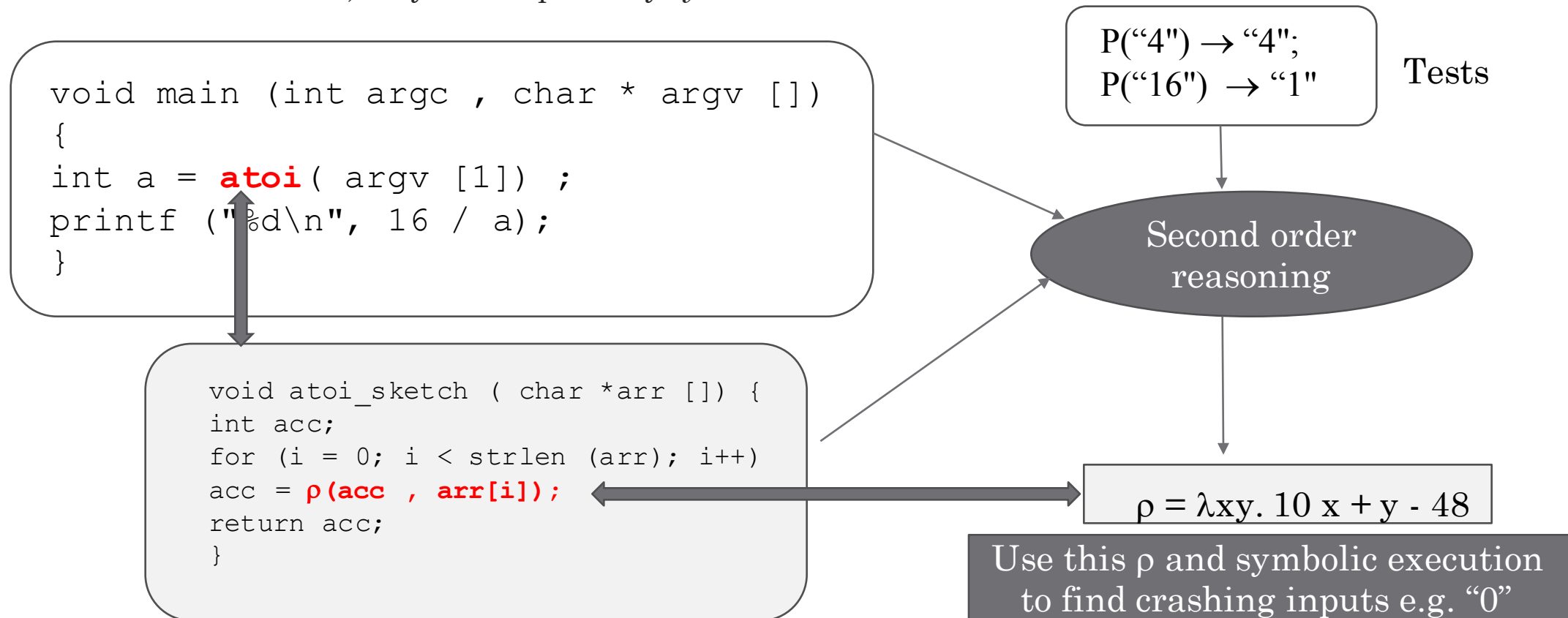
Comparison: 1st and 2nd order logic



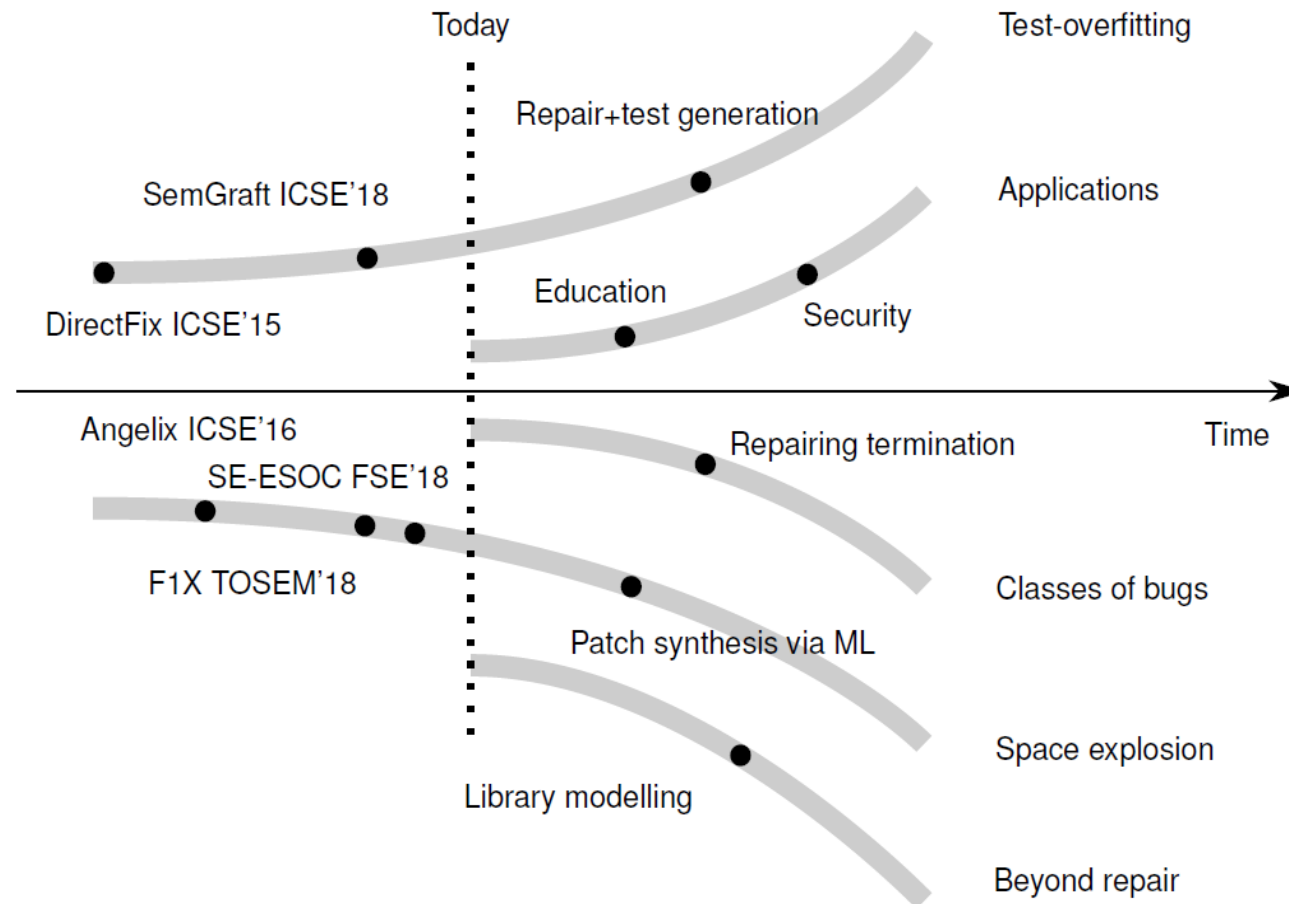
Time taken by second order symbolic execution is independent of the maximum number of paths explored.

Other applications

- Modeling libraries for symbolic execution of application program.
 - Do not manually provide libraries for symbolic analysis.
 - Instead, they can be partially *synthesized*.



Future work in Semantic Repair



Briefly: Novel applications outside security

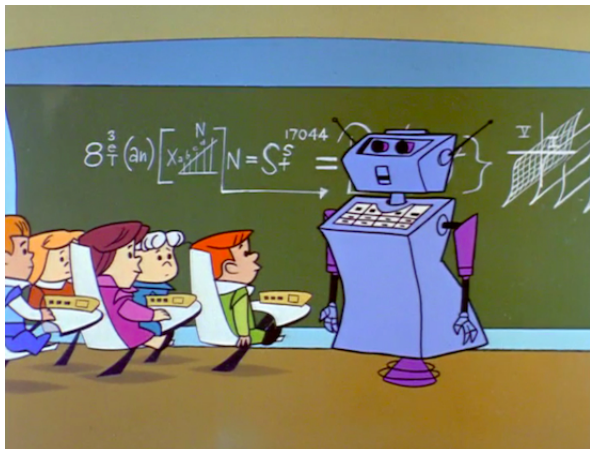


Use program repair in **intelligent tutoring systems** to give the students' individual attention.

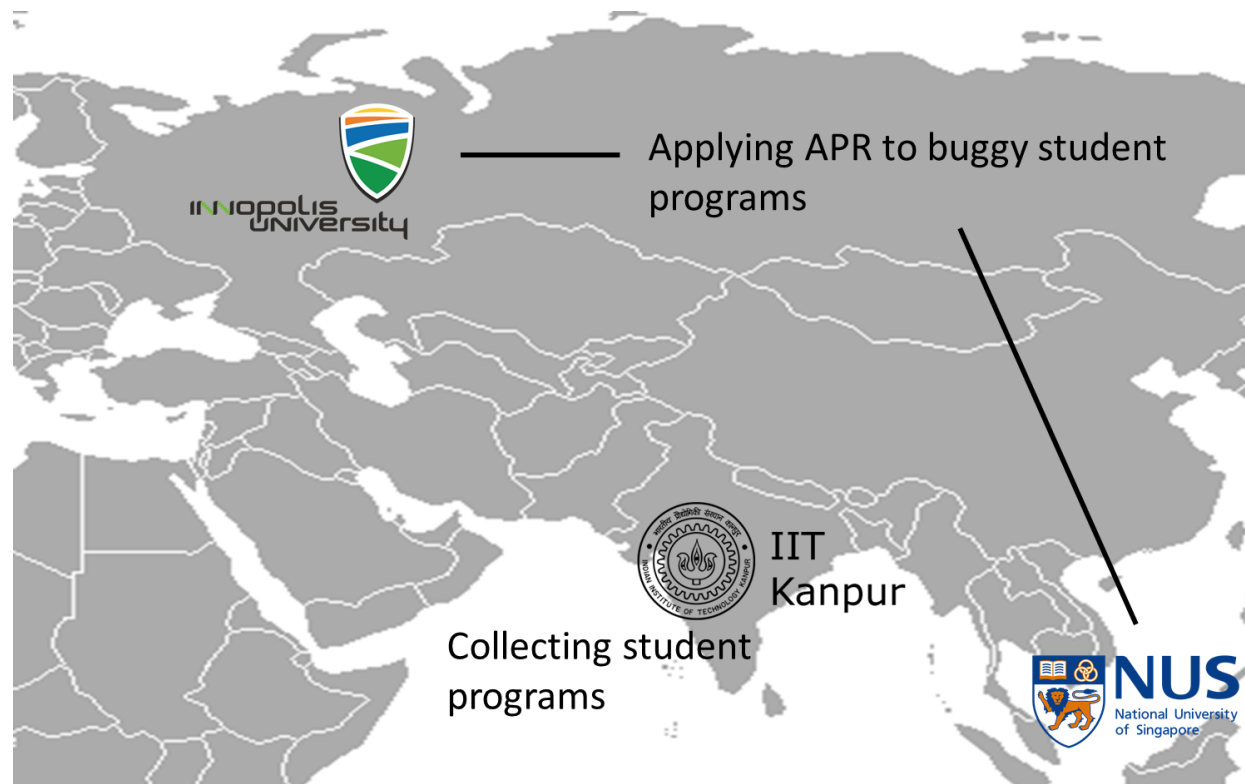
Study in IIT-Kanpur (FSE17)



Application in Education



Intelligent tutoring

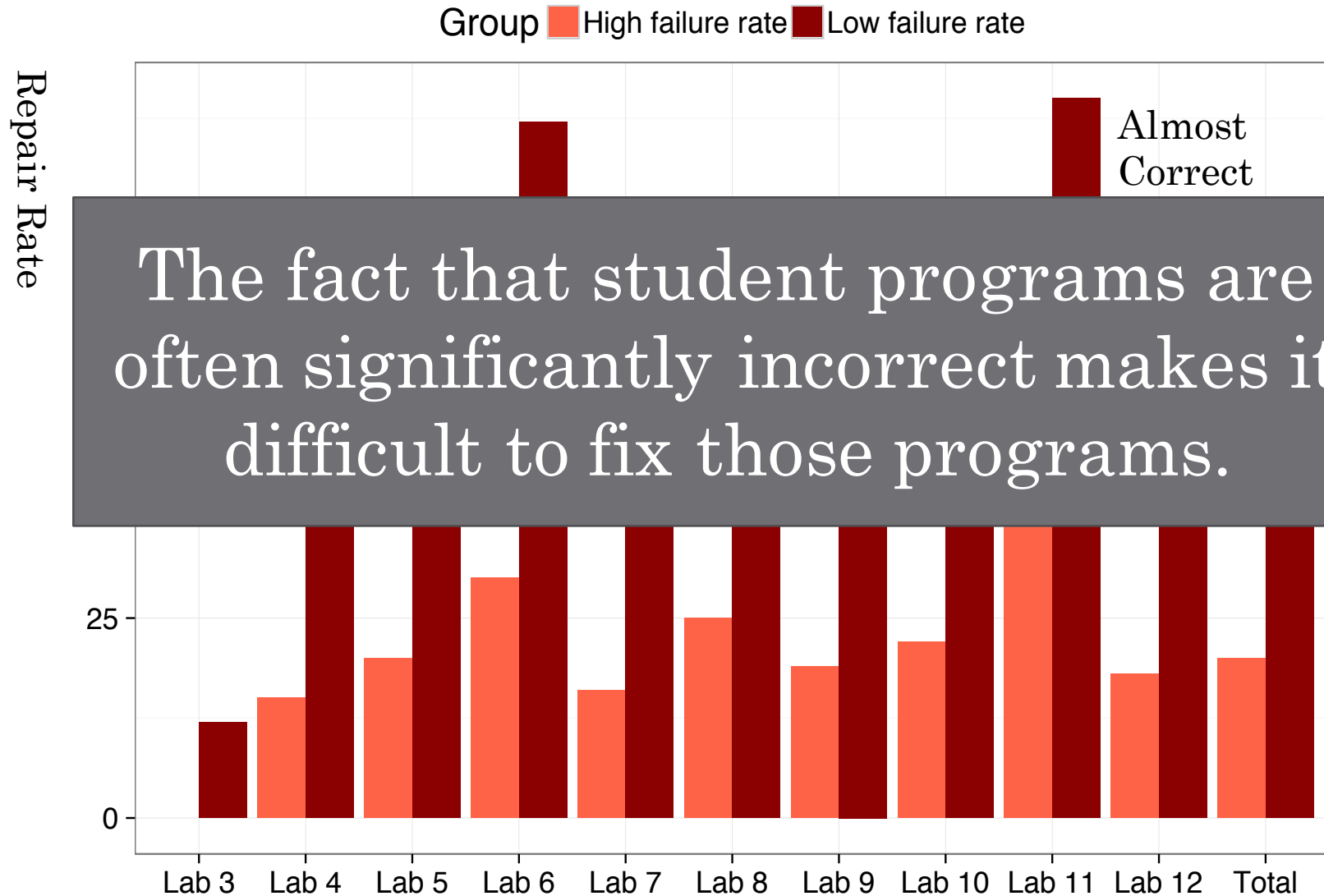


Dataset Preparation

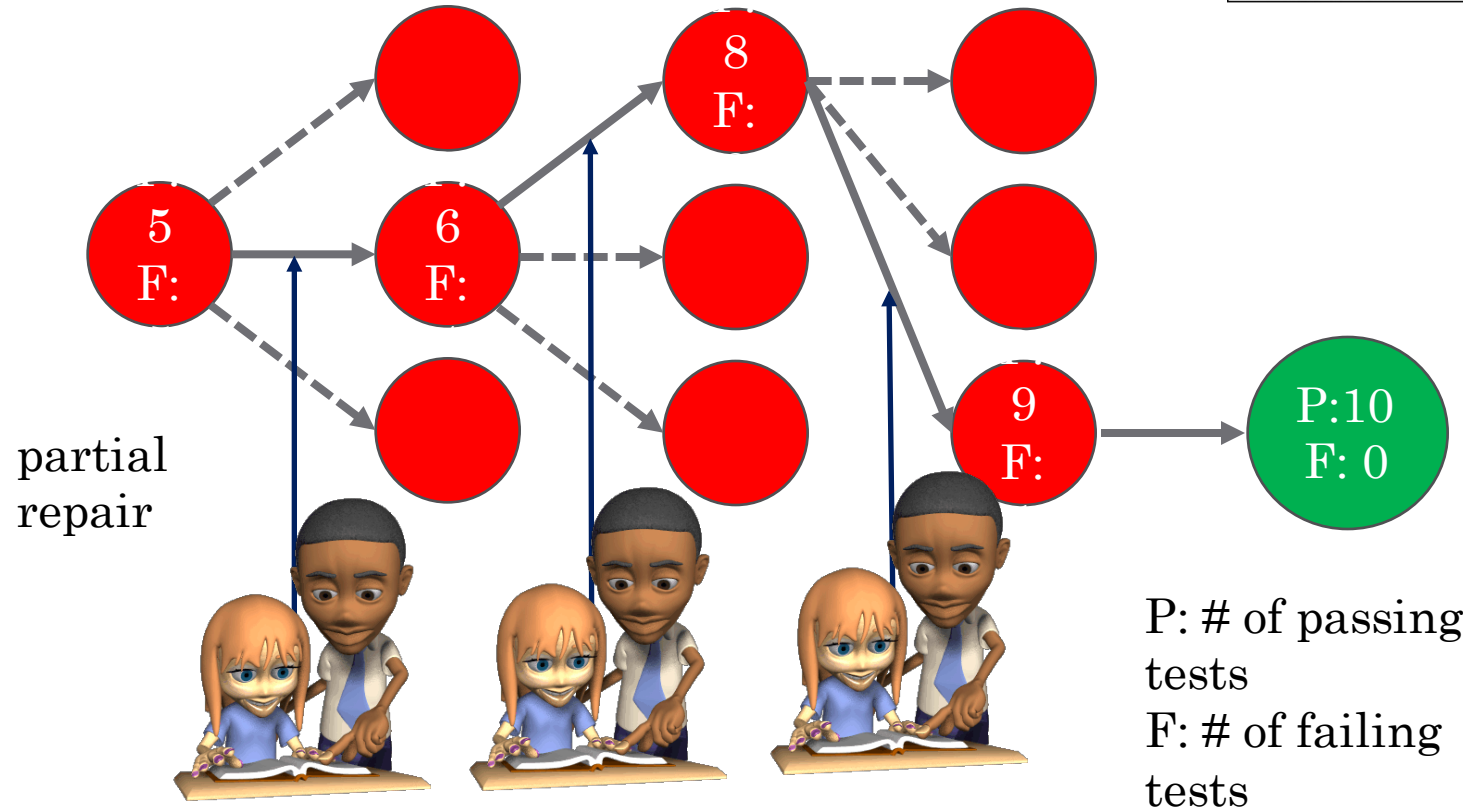
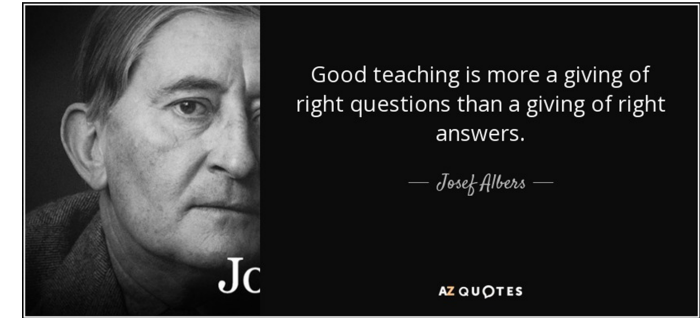
- Lab: Programming assignments

Lab	# Prog	Topic
Lab 3	63	Simple Expressions, printf, scanf
Lab 4	117	Conditionals
Lab 5	82	Loops, Nested Loops
Lab 6	79	Integer Arrays
Lab 7	71	Character Arrays (Strings) and Functions
Lab 8	33	Multi-dimensional Arrays (Matrices)
Lab 9	48	Recursion
Lab 10	53	Pointers
Lab 11	55	Algorithms (sorting, permutations, puzzles)
Lab 12	60	Structures (User-Defined data-types)

Almost Incorrect vs Almost Correct

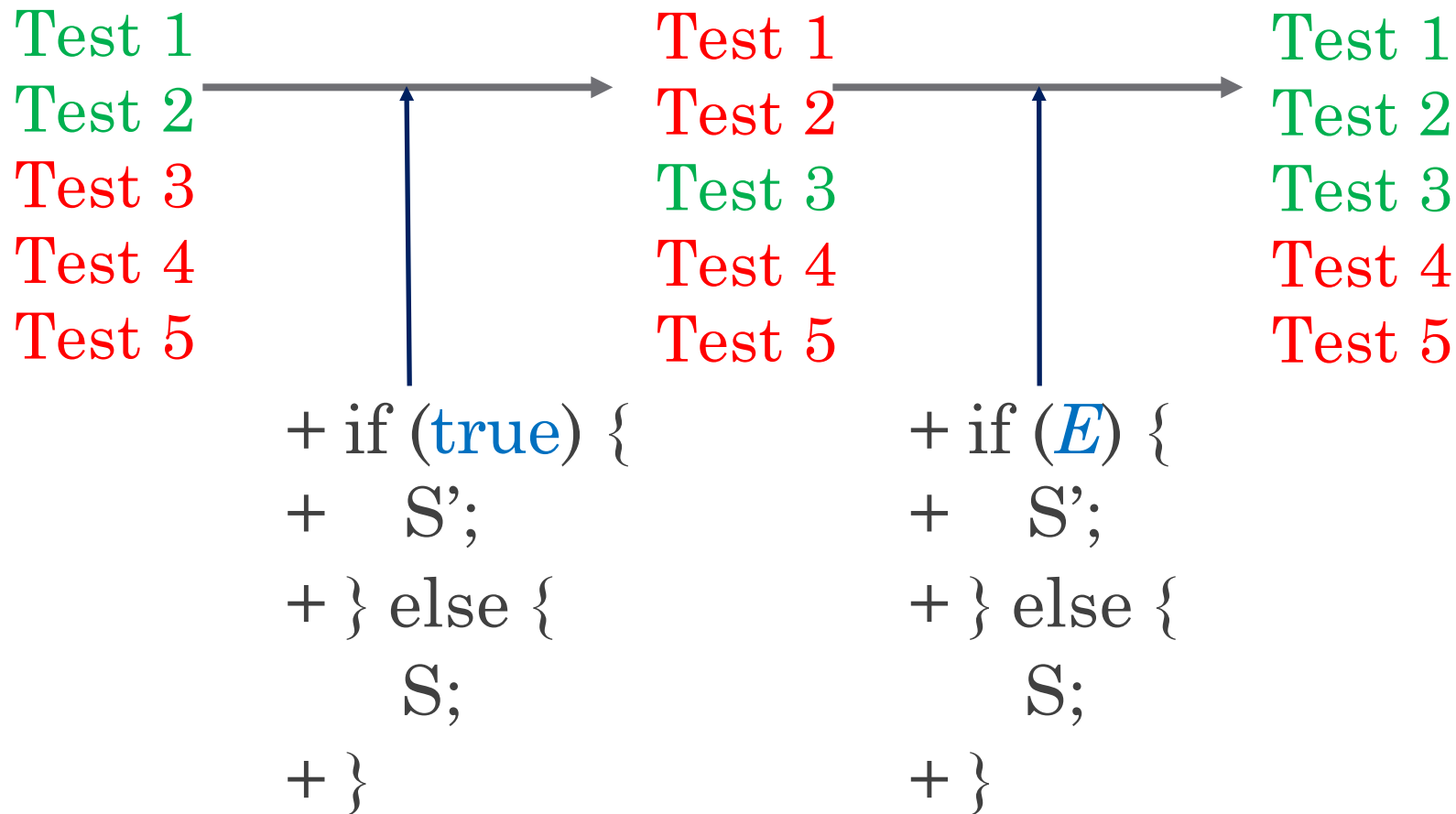


Tailoring Repair Policy



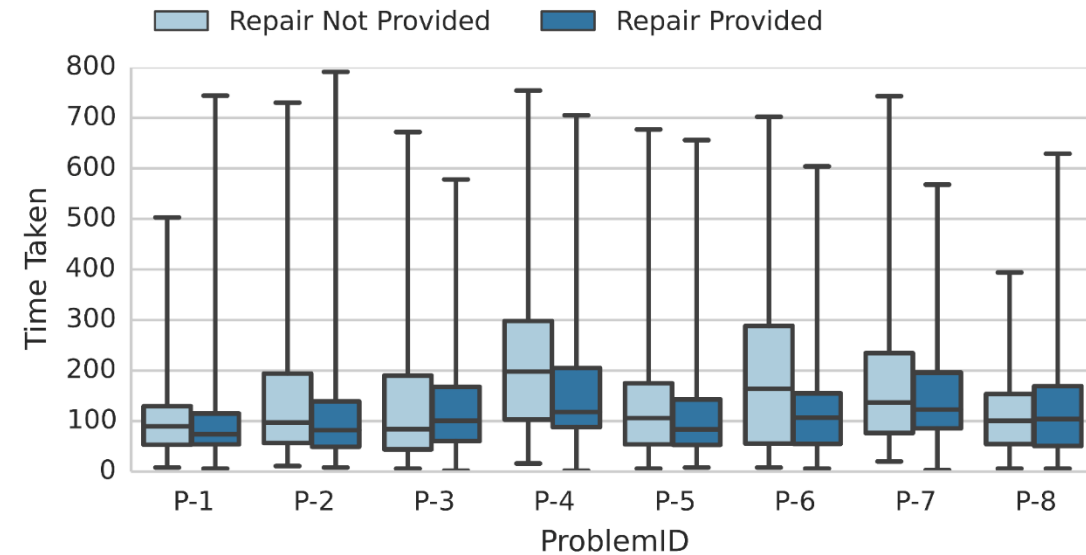
Partial Repair: (all previously passing tests) + (at least one previously failing test)

Two-Step Repair



User Study: Graders – Time Taken

- **43** buggy student submissions from dataset
 - Across **8** unique problems
- **37** TA graders volunteered for study
 - Each TA gets all **43** submissions to grade
 - With repair hints for half the submissions
- Task: Grade the buggy program
 - With marks on closeness to correct solution



Wrap up: Community Response

- Angelix (angelix.io) — program repair tool based on symbolic execution:
 - The first constraint-based repair systems that scales to large programs;
 - Repaired Heartbleed vulnerability in OpenSSL; 46 stars on GitHub, 16 forks, 6 contributors;
 - Used by researchers from over 80 institutions; Used in intelligent tutoring system at IIT Kanpur.
- program-repair.org community website:
 - ~300 unique visitors per month;
 - ~100 researchers subscribed;
 - Contributors from ~10 institutions.
- **The community is growing, please join and contribute!**



Relevant Research Results

Symbolic execution with second order existential constraints

Sergey Mechtaev, Alberto Griggio, Alessandro Cimatti, Abhik Roychoudhury
ACM Symposium on Foundations of Software Engineering (FSE) 2018.

Semantic Program Repair Using a Reference Implementation ([PDF](#))

Sergey Mechtaev, Manh-Dung Nguyen, Yannic Noller, Lars Grunske, Abhik Roychoudhury
ACM/IEEE 40th International Conference on Software Engineering (ICSE) 2018.

Angelix: Scalable Multiline Program Patch Synthesis via Symbolic Analysis ([pdf](#))

Sergey Mechtaev, Jooyong Yi, Abhik Roychoudhury
ACM/IEEE International Conference on Software Engineering (ICSE) 2016.

DirectFix: Looking for Simple Program Repairs ([PDF](#))

Sergey Mechtaev, Jooyong Yi, Abhik Roychoudhury
ACM/IEEE International Conference on Software Engineering (ICSE) 2015.

SemFix: Program Repair via Semantic Analysis ([pdf](#))

Hoang D.T. Nguyen, Dawei Qi, Abhik Roychoudhury, Satish Chandra
ACM/IEEE International Conference on Software Engineering (ICSE) 2013.

<http://www.comp.nus.edu.sg/~abhik/projects/Repair/index.html>

ACKNOWLEDGEMENT: National Cyber Security Research program from NRF
Singapore <http://www.comp.nus.edu.sg/~tsunami/>

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Van Thuan Pham, PhD. 2017

Sergey Mechtaev, PhD. 2018 -> Lecturer University College London

Shin Hwei Tan, PhD. 2018 -> Asst Prof, SUSTech, Shenzhen. China

Jooyong Yi, past post-doc -> Asst Prof. Innopolis

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